## Static Program Analysis

## Yue Li and Tian Tan



# Static Program Analysis CFL-Reachability and IFDS

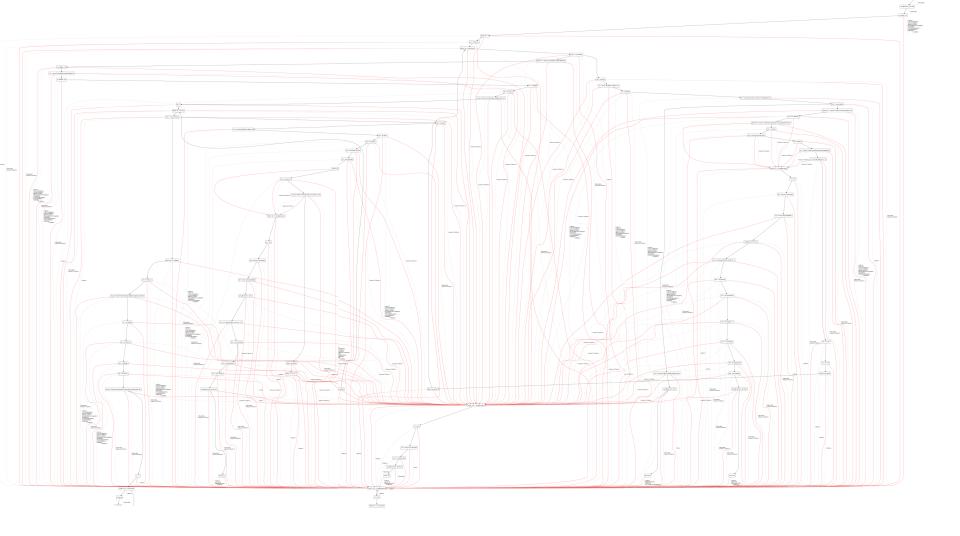
Nanjing University

Yue Li

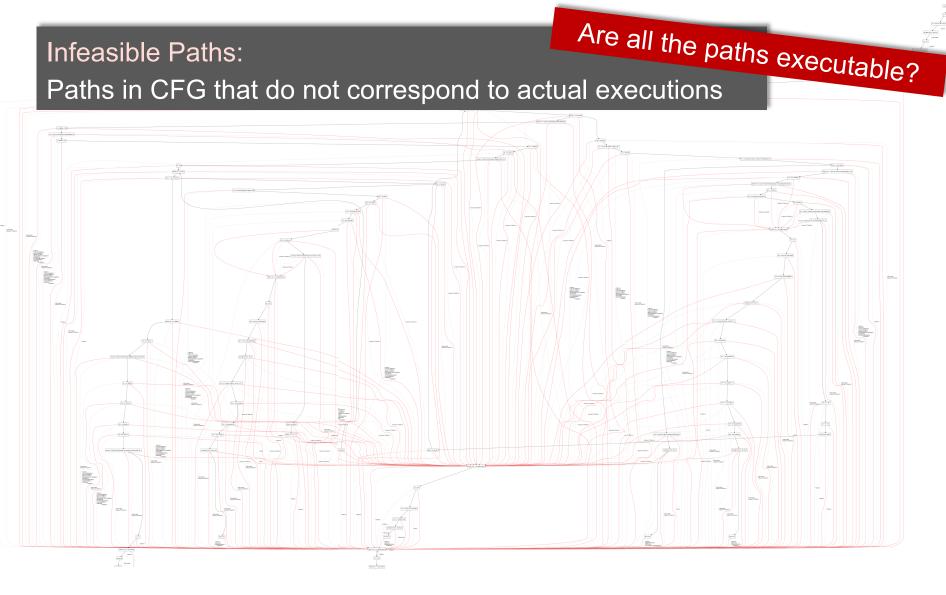
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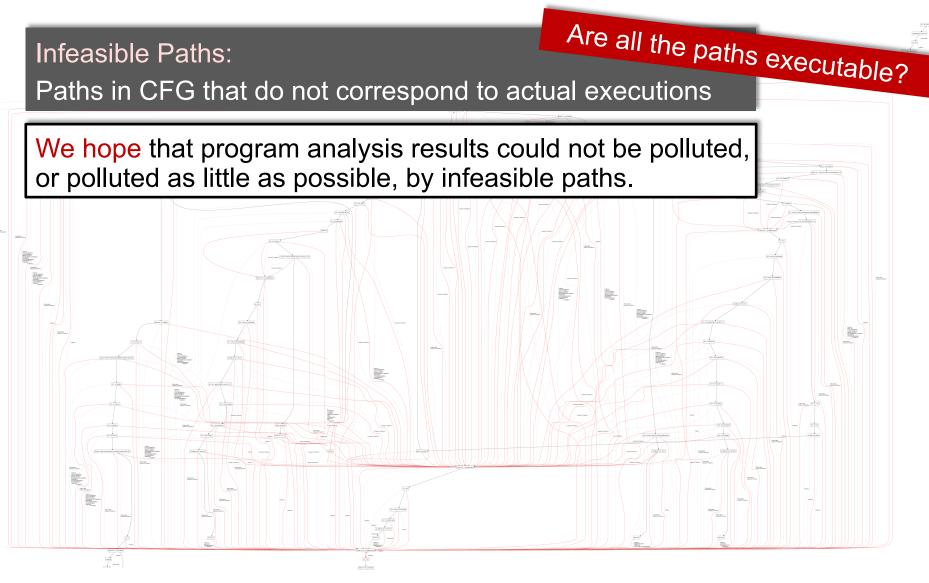
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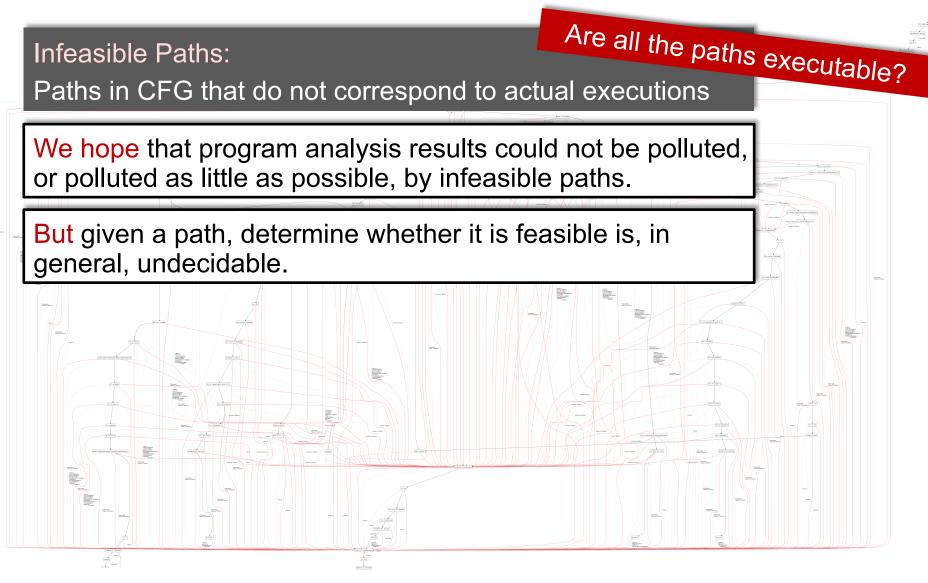
- 1. Feasible and Realizable Paths
- 2. CFL-Reachability
- 3. Overview of IFDS
- 4. Supergraph and Flow Functions
- 5. Exploded Supergraph and Tabulation Algorithm
- 6. Understanding the Distributivity of IFDS

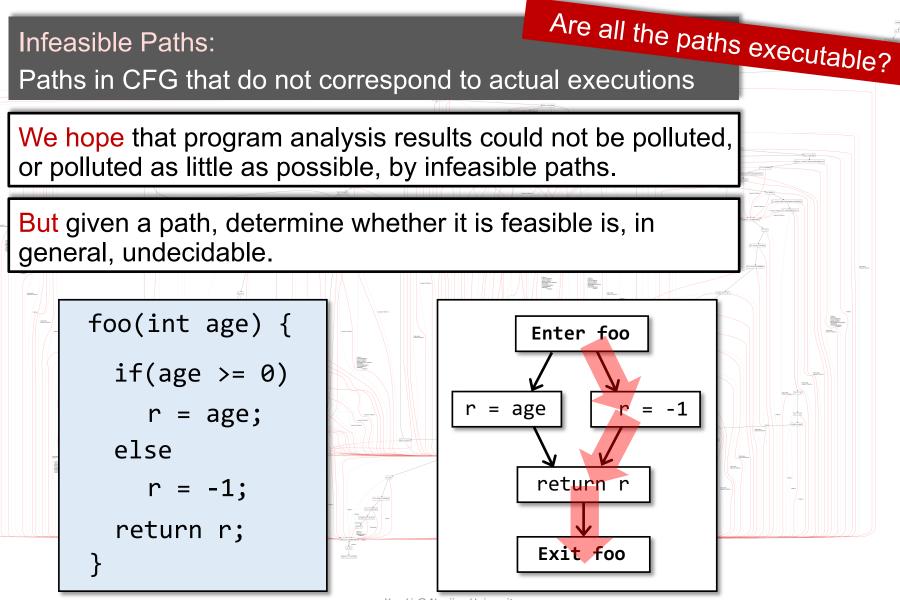


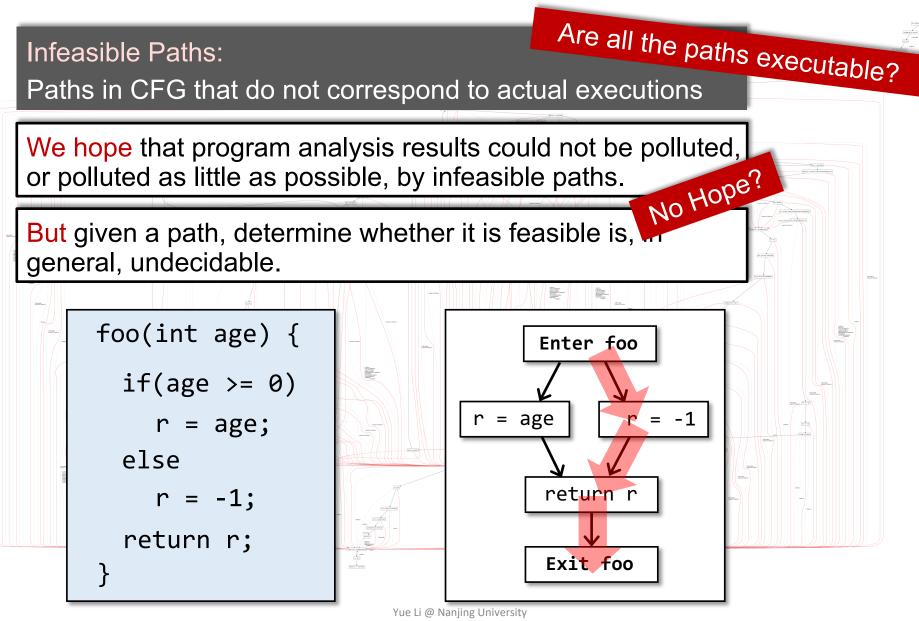




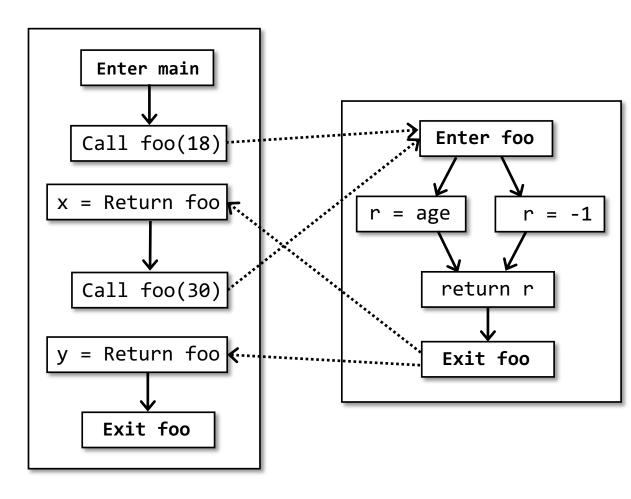


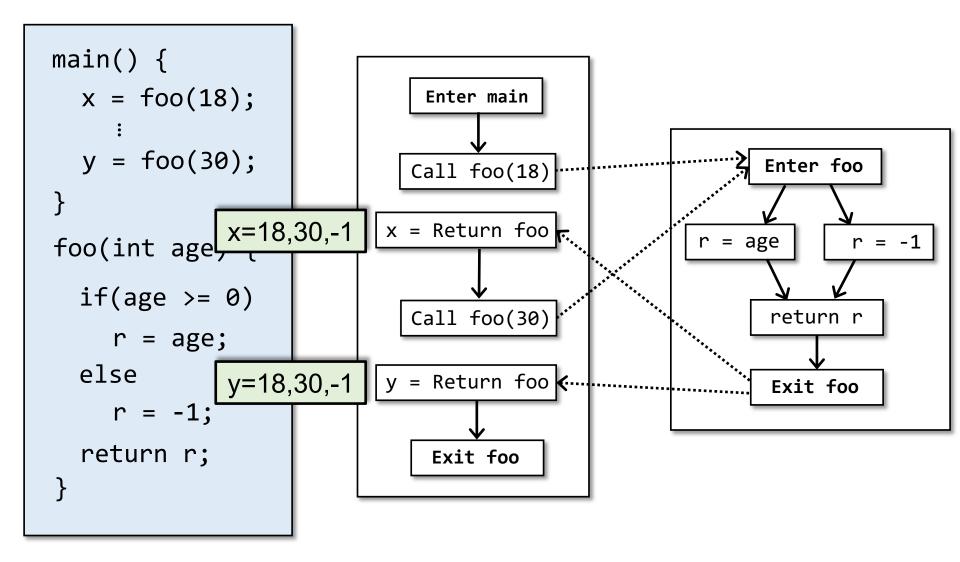


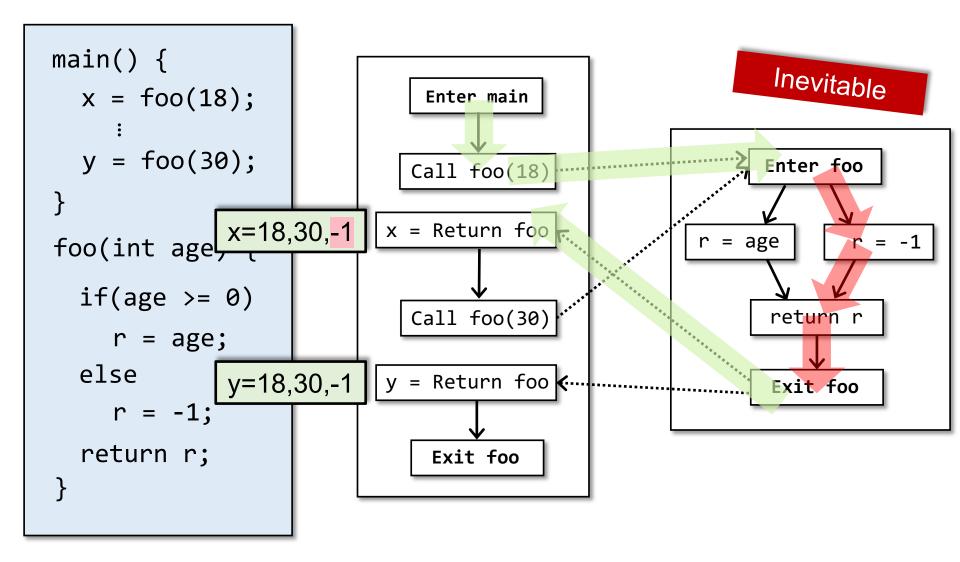


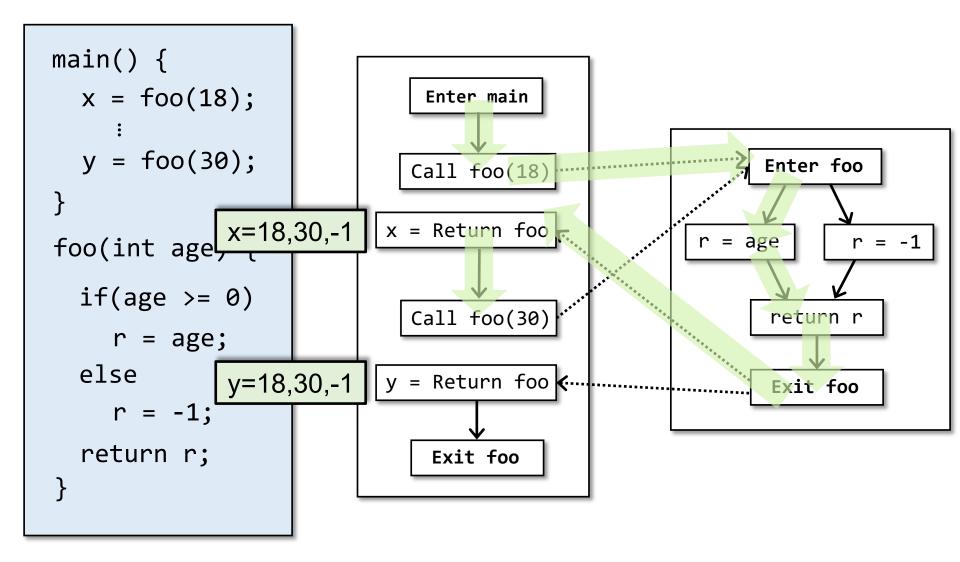


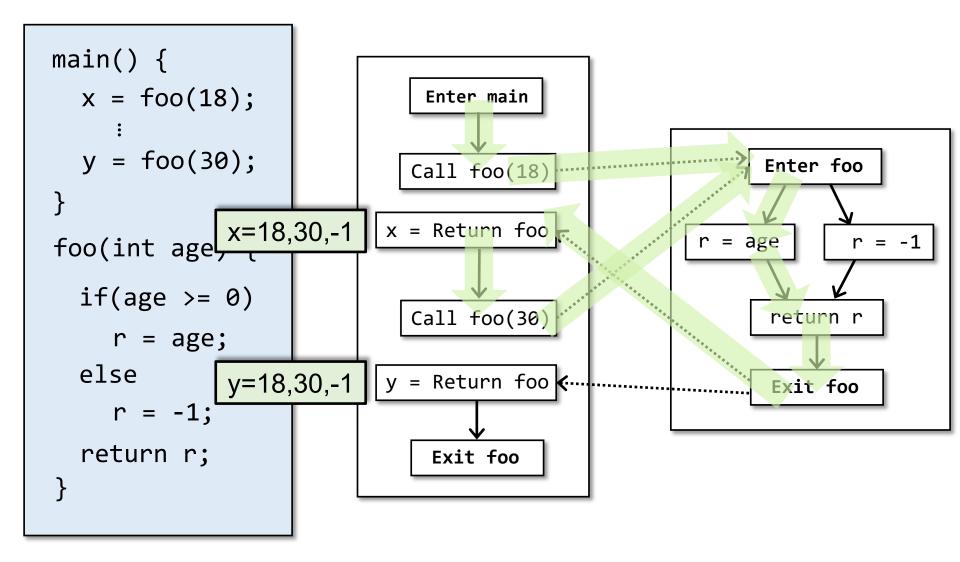
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main() {
  x = foo(18);
  y = foo(30);
}
foo(int age) {
  if(age >= 0)
    r = age;
  else
    r = -1;
  return r;
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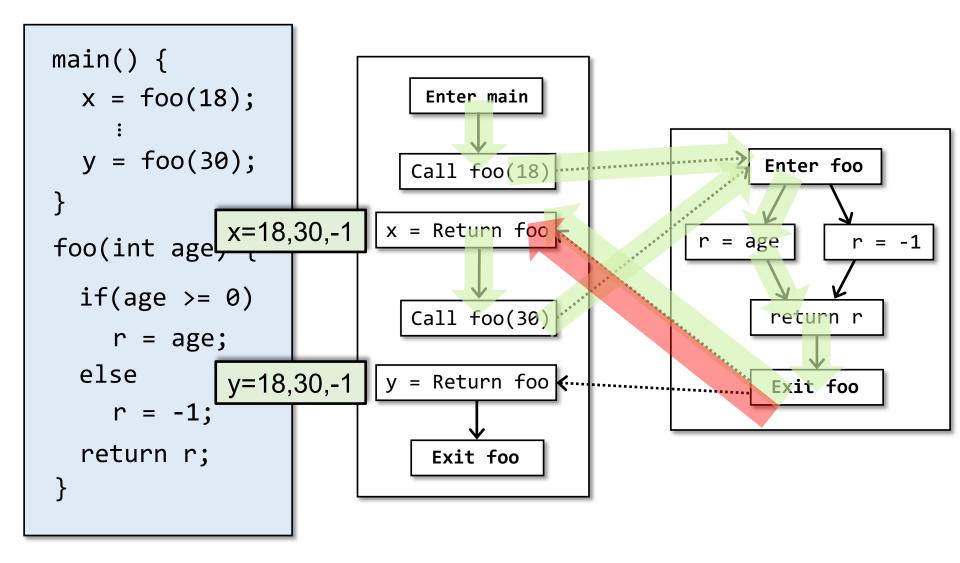


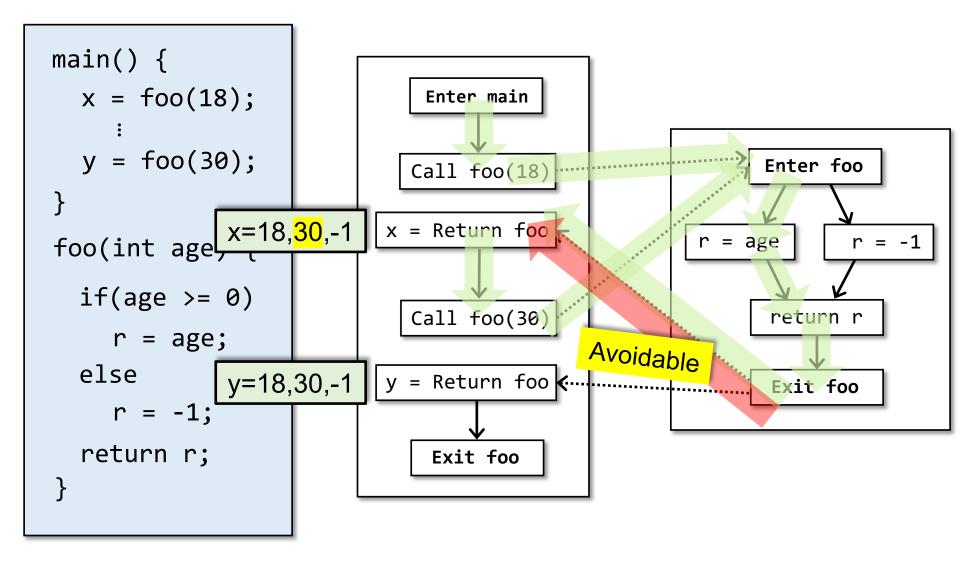












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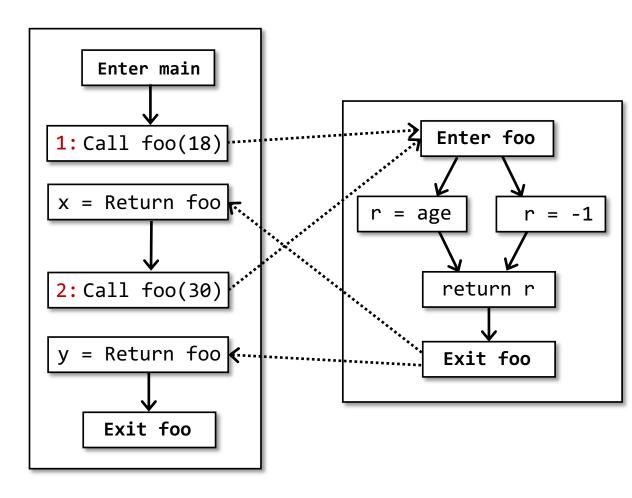
- Realizable paths may not be executable, but unrealizable paths must not be executable.
- Our goal is to recognize realizable paths so that we could avoid polluting analysis results along unrealizable paths.

#### **Realizable Paths**

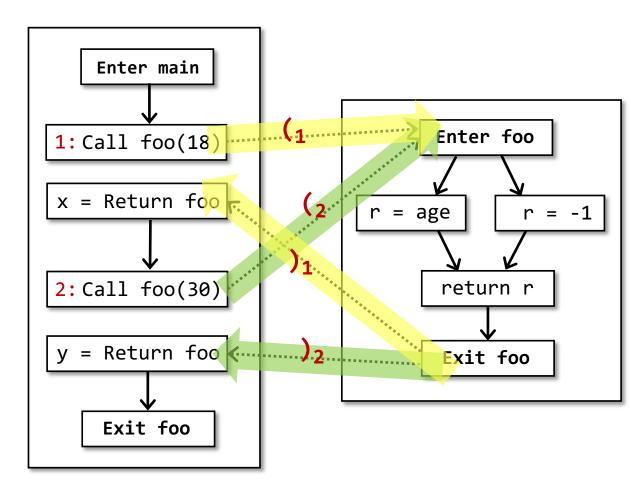
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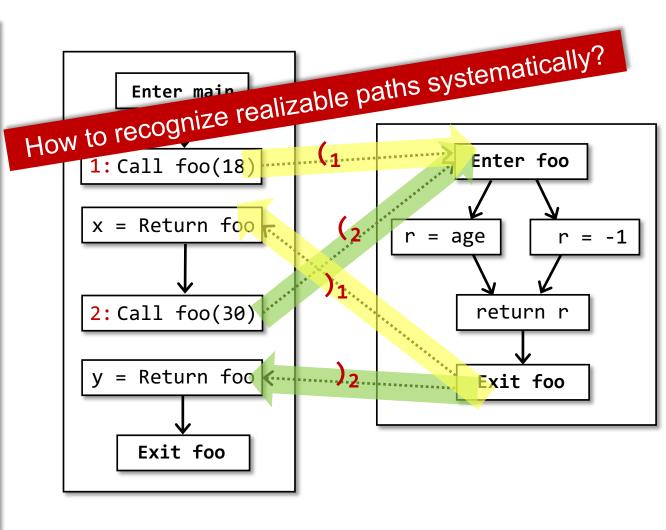
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- A context-free language is a language generated by a context-free grammar (CFG).

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CFG is a formal grammar in which every production is of the form:  $S \rightarrow \alpha$ where S is a single nonterminal and  $\alpha$  could be a string of terminals

and/or nonterminals, or empty.

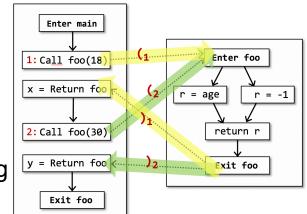
•  $S \rightarrow aSb$ 

•  $S \rightarrow \varepsilon$ 

Context-free means S could be replaced by  $aSb/\epsilon$  anywhere, regardless of where S occurs.

Partially Balanced-Parenthesis Problem via CFL

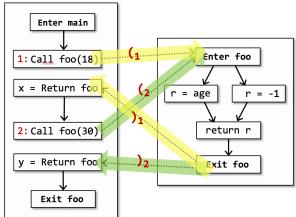
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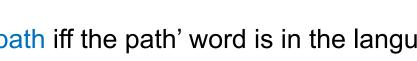
A path is a realizable path iff the path' word is in the language *L(realizable)* 



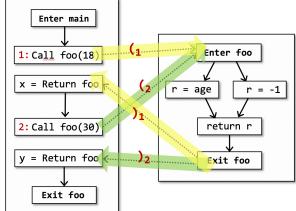
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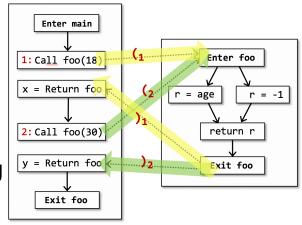
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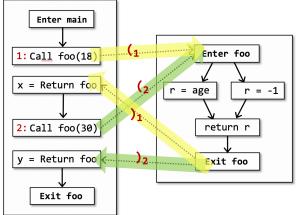
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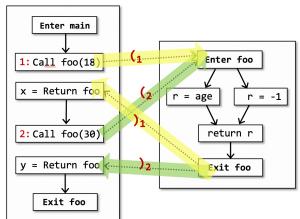
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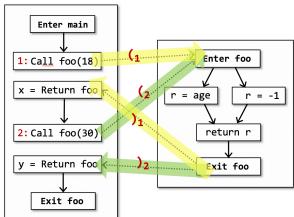
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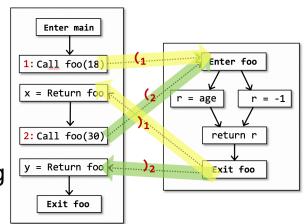
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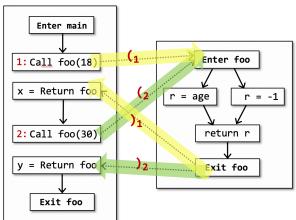


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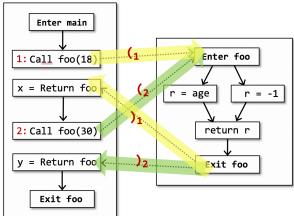
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 $\rightarrow$  matched realizable eq (1(2e))(2)

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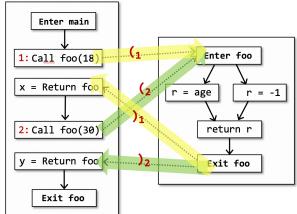
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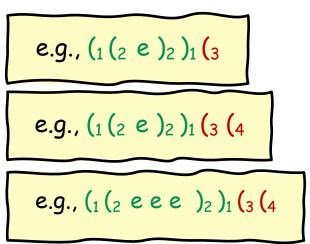
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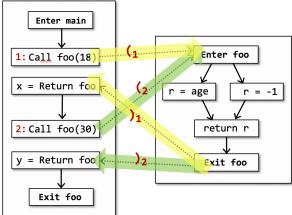
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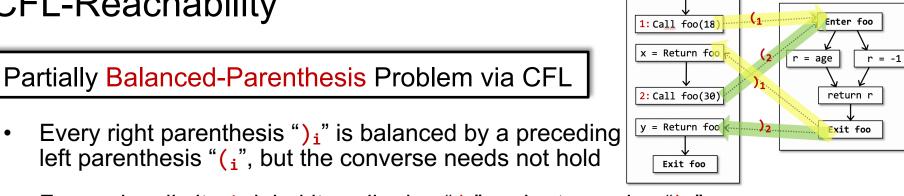




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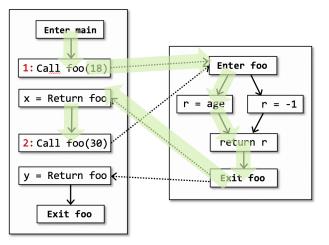
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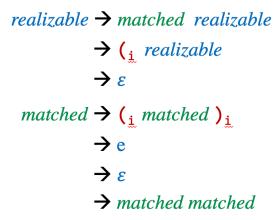
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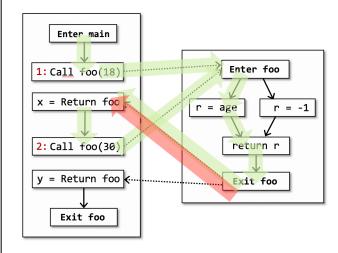
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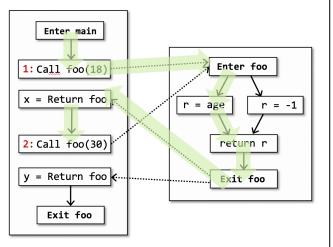
**CFL-Reachability** 



#### L(realizable):

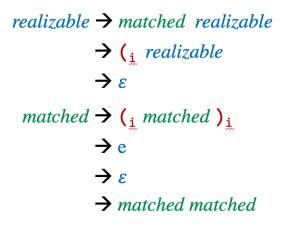


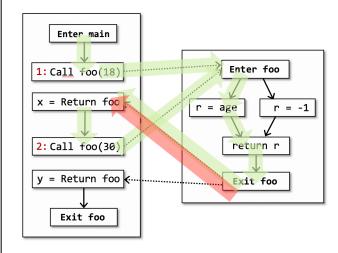


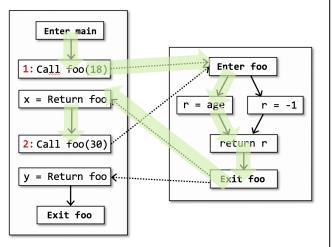


 $e(_1eee)_1e \in L(realizable)$ 

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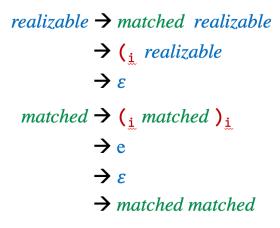


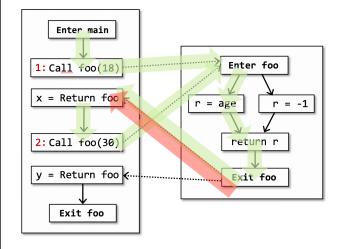




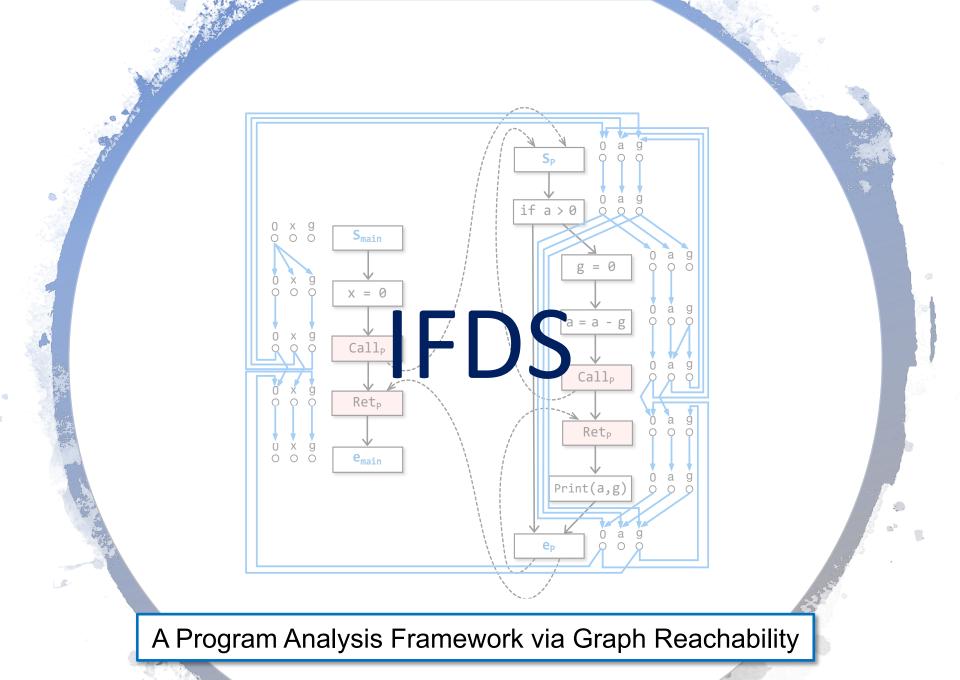
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#### L(realizable):





 $e(_1eee)_1e(_2eee)_1$  $\notin L(realizable)$ 



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"Precise Interprocedural Dataflow Analysis via Graph Reachability"

Thomas Reps, Susan Horwitz, and Mooly Sagiv, POPL'95

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IFDS is for interprocedural data flow analysis with distributive flow functions over finite domains.

Provide meet-over-all-realizable-paths (MRP) solution.

Path function for path p, denoted as  $pf_p$ , is a composition of flow functions for all edges (sometimes nodes) on p.



$$pf_{p} = f_{n} \circ \ldots \circ f_{2} \circ f_{1}$$

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pecall
$$pf_p = f_n \circ \dots \circ f_2 \circ f_1$$
 $MOP_n = \bigsqcup_{p \in Paths(start, n)} pf_p(\bot)$ 

For each node n,  $MOP_n$  provides a "meet-over-all-paths" solution where Paths(start, n) denotes the set of paths in CFG from the start node to n.

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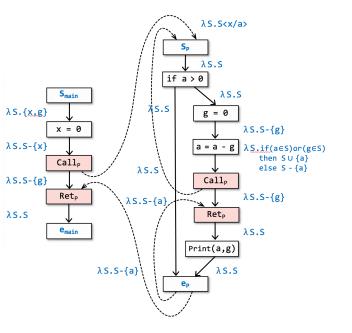
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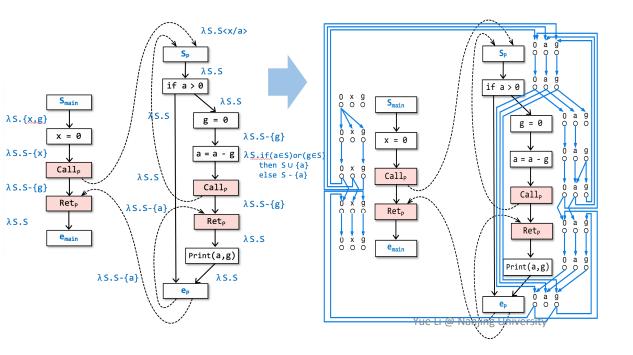
$$MRP_n \sqsubseteq MOP_n$$

Given a program P, and a dataflow-analysis problem Q

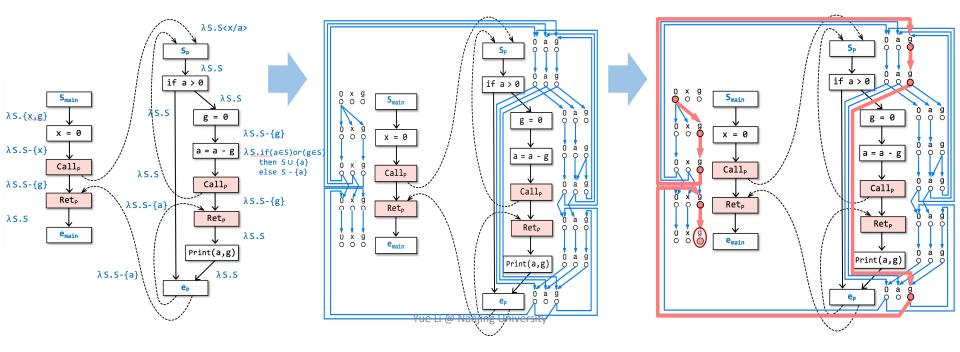
 Build a supergraph G\* for P and define flow functions for edges in G\* based on Q



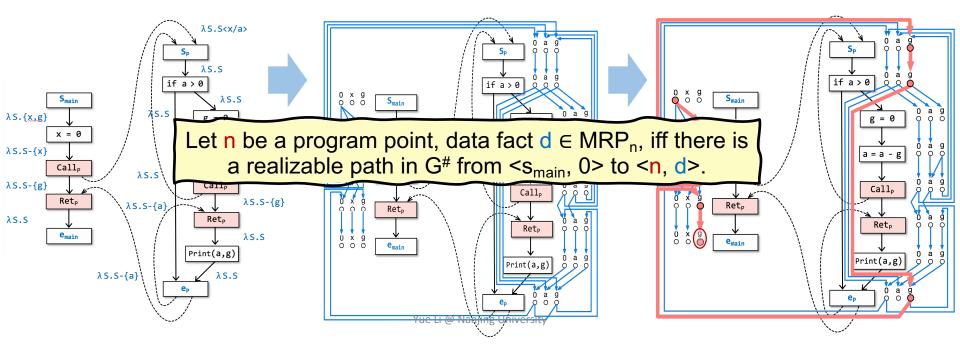
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- Build exploded supergraph G<sup>#</sup> for P by transforming flow functions to representation relations (graphs)



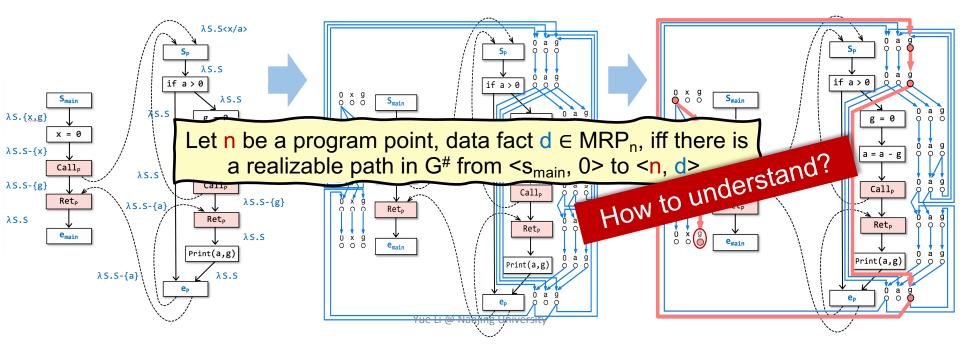
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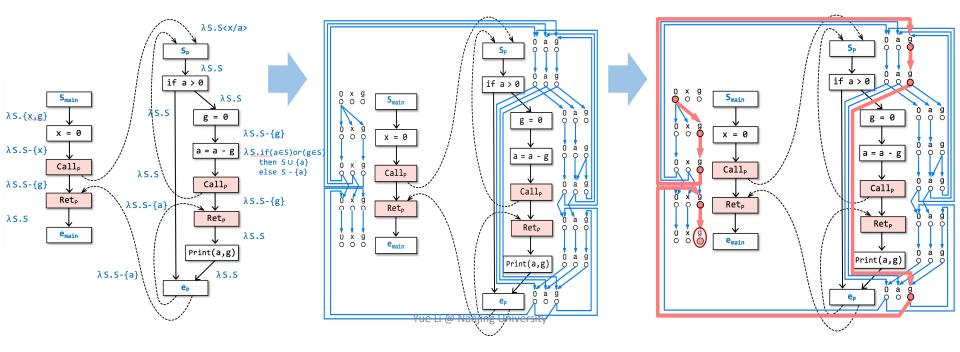
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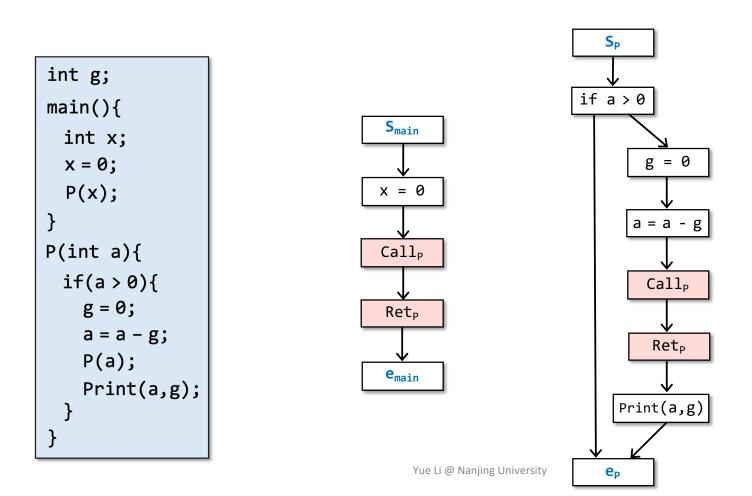
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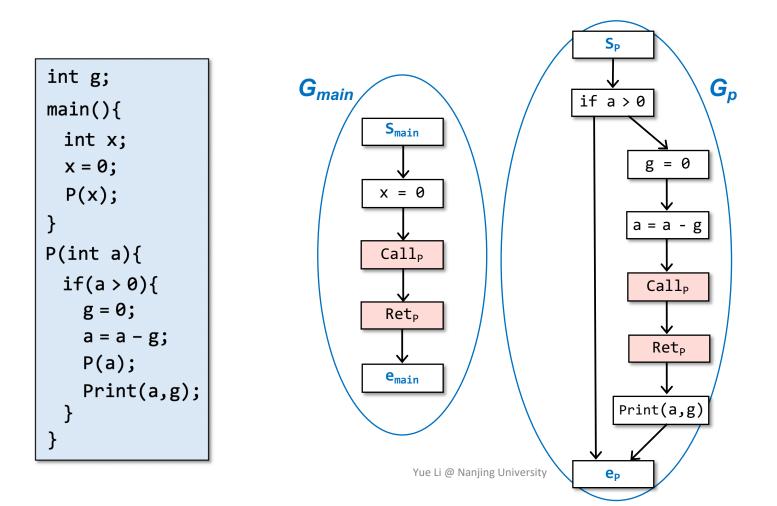


In IFDS, a program is represented by  $G^* = (N^*, E^*)$  called a supergraph.



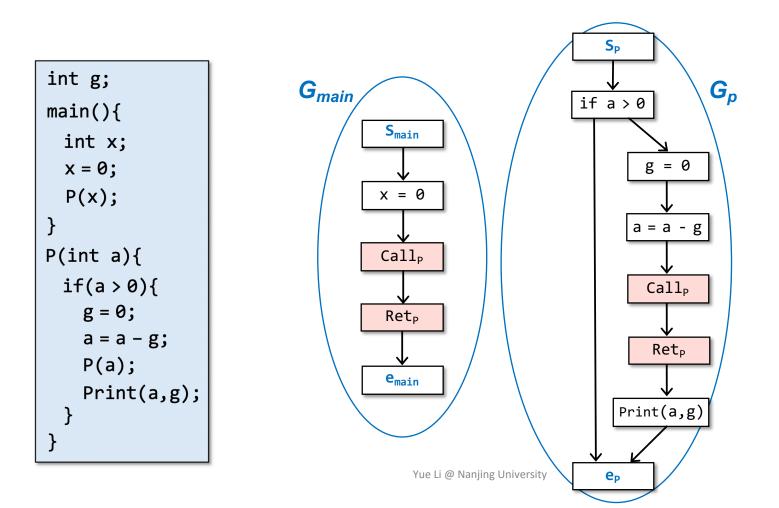
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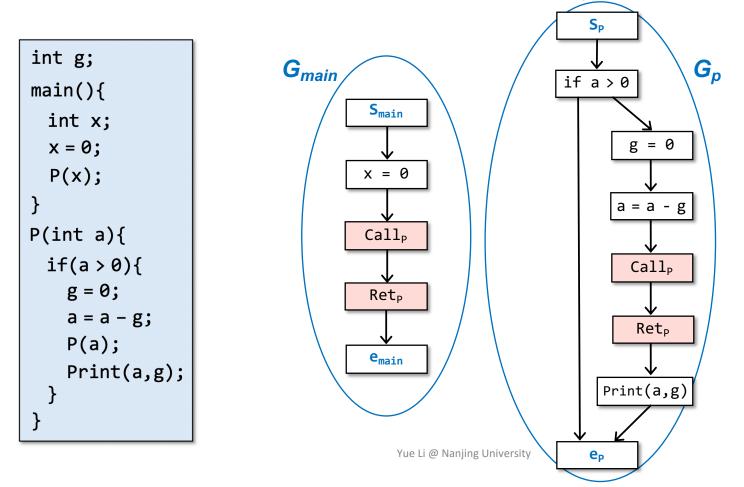
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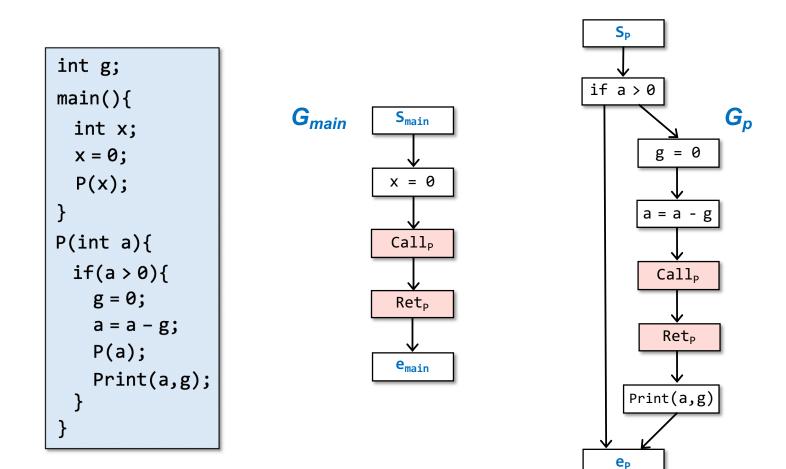
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- Each flowgraph  $G_p$  has a unique start node  $s_p$ , and a unique exit node  $e_p$
- A procedure call is represented by a call node  $Call_p$ , and a return-site node  $Ret_p$



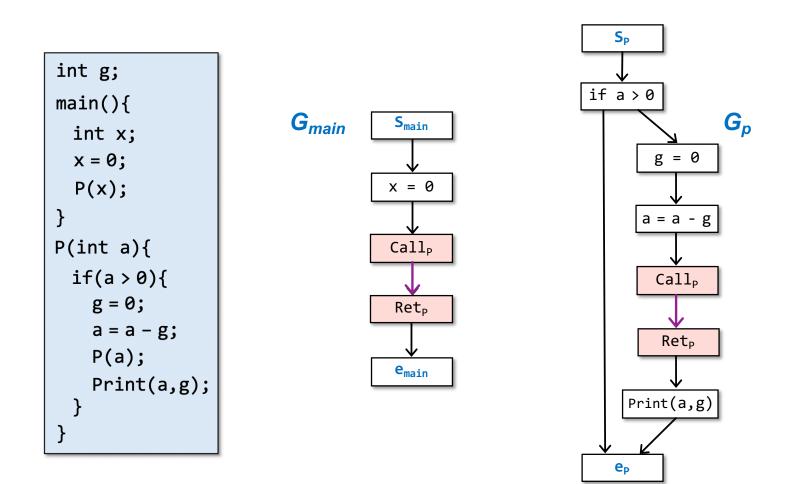


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*G*\* has three edges for each procedure call:

# Supergraph

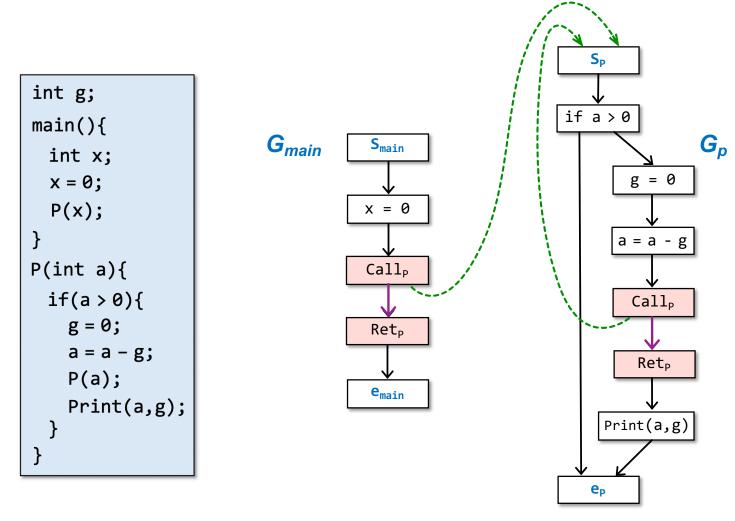
An intraprocedural call-to-return-site edge from Call<sub>p</sub> to Ret<sub>p</sub>



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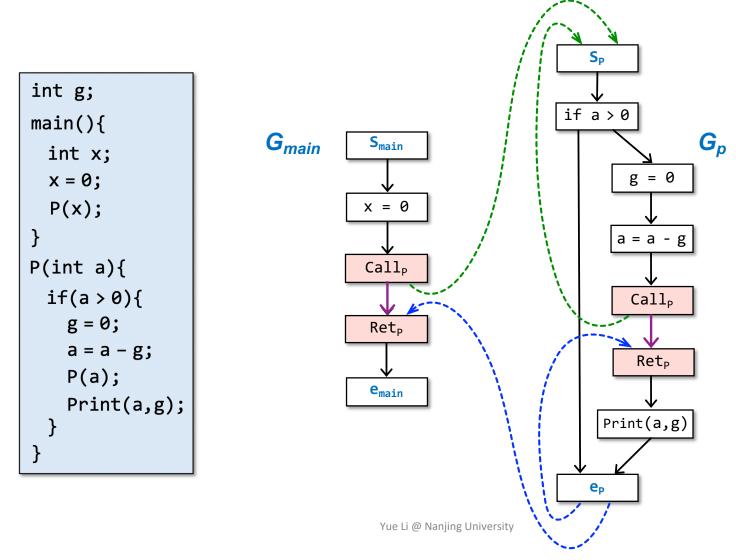
- An intraprocedural call-to-return-site edge from Call<sub>p</sub> to Ret<sub>p</sub>
- An interprocedural call-to-start edge from  $Call_p$  to  $s_p$  of the called procedure



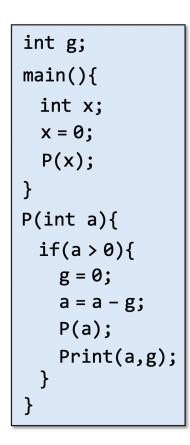
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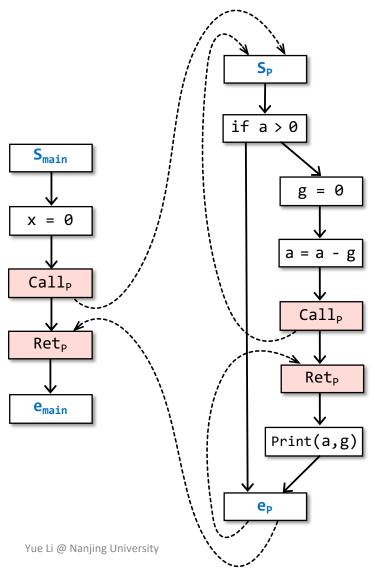
# Supergraph

- An intraprocedural call-to-return-site edge from Call<sub>p</sub> to Ret<sub>p</sub>
- An interprocedural call-to-start edge from  $Call_p$  to  $s_p$  of the called procedure
- An interprocedural exit-to-return-site edge from  $e_p$  of the called procedure to  $Ret_p$

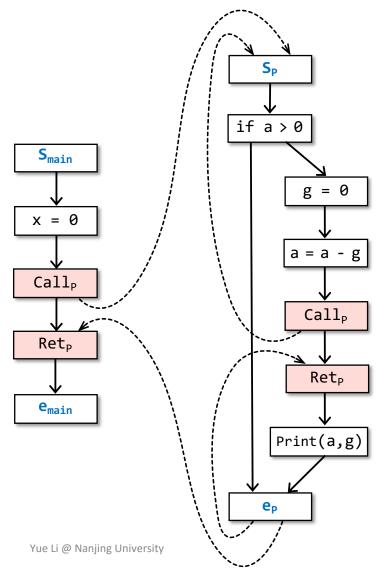


"Possibly-uninitialized variables": for each node  $n \in N^*$ , determine the set of variables that may be uninitialized before execution reaches n.





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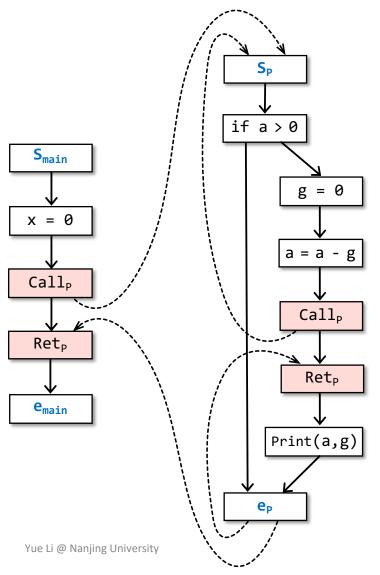
e.g.,  $\lambda \mathbf{X} \cdot \mathbf{X+1}$ 

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Sp if a > 0S<sub>main</sub> g = 0 x = 0a = a - g Call<sub>P</sub> Call<sub>P</sub> Ret<sub>P</sub> **Ret**<sub>P</sub>  $\bm{e}_{\texttt{main}}$ Print(a,g) **e**<sub>P</sub> Yue Li @ Nanjing University

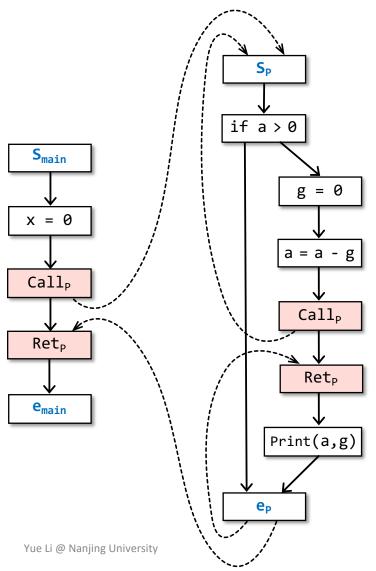
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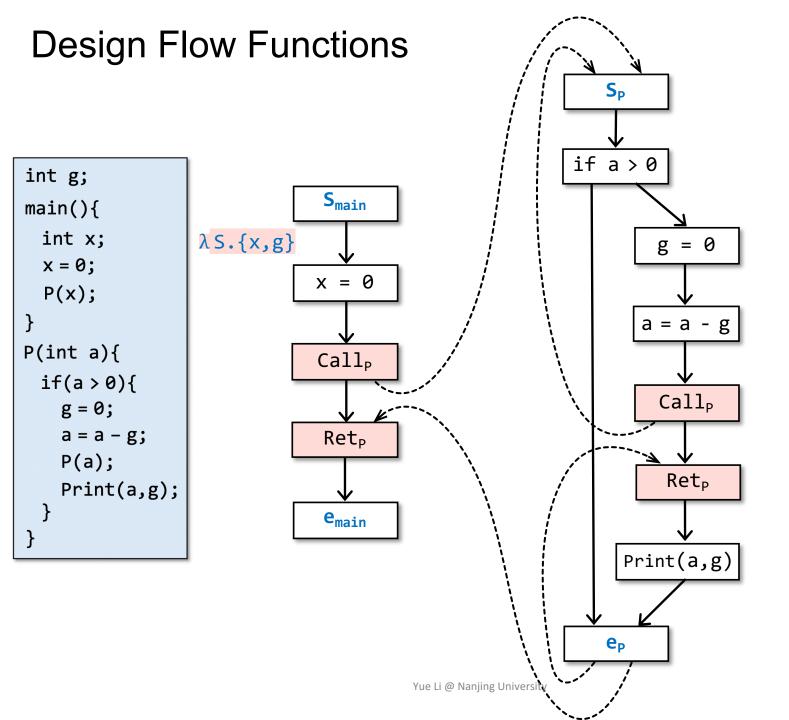
 $\lambda e_{param} \cdot e_{body}$ e.g.,  $\lambda \times \cdot \times +1$ ( $\lambda \times \cdot \times +1$ )3

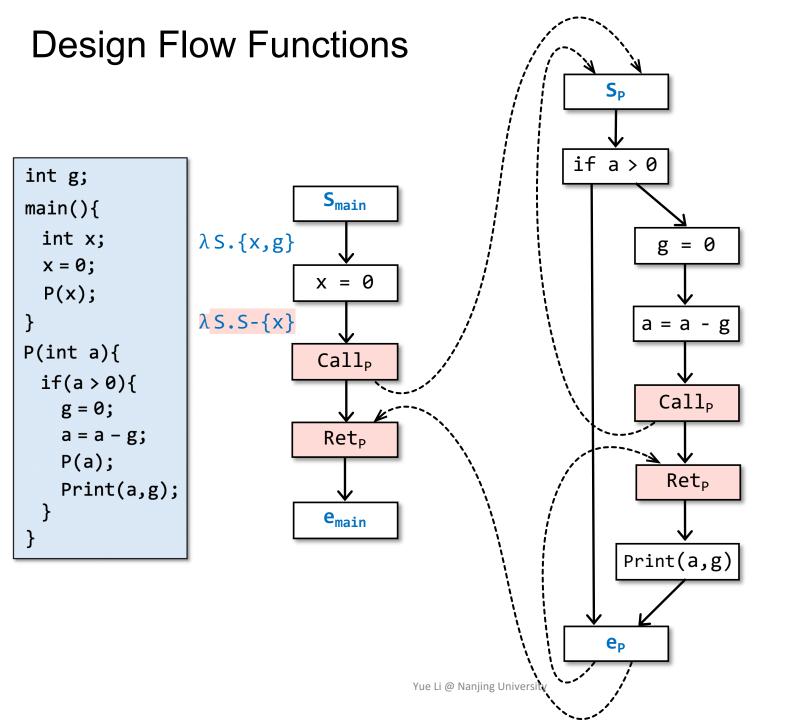


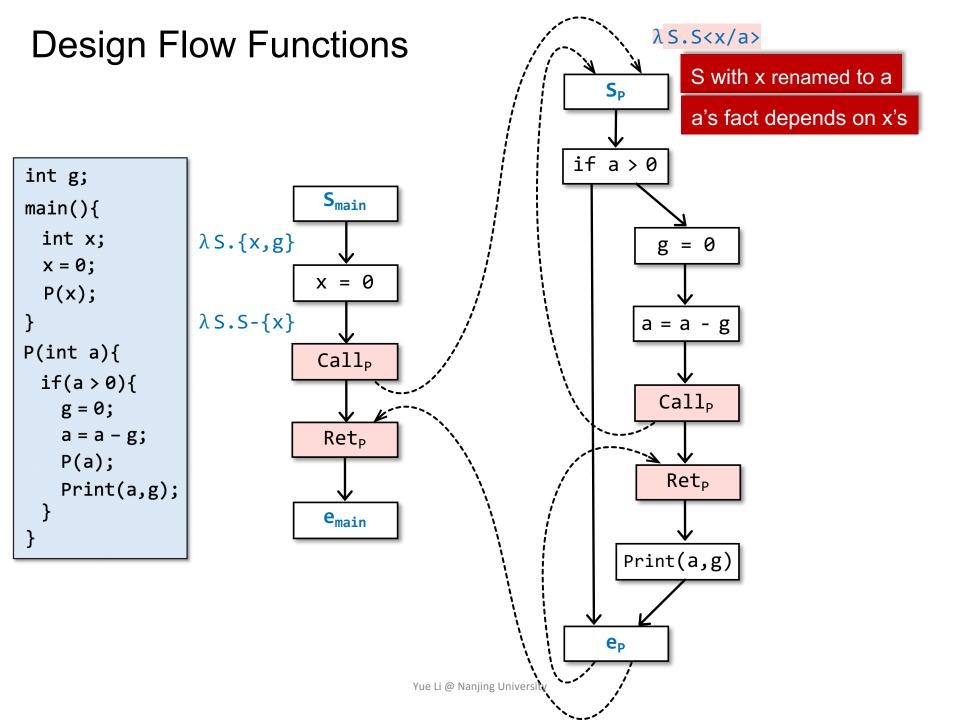
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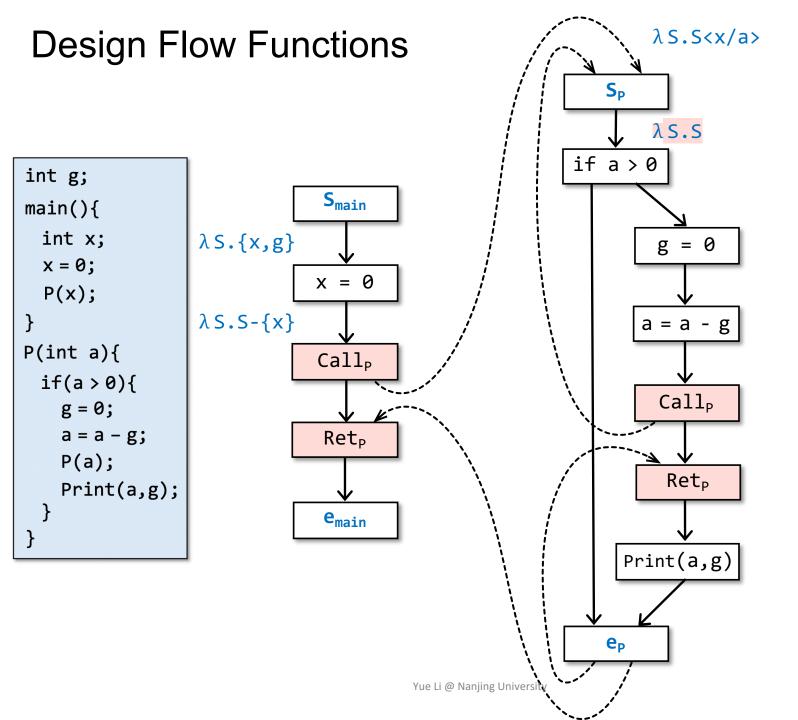
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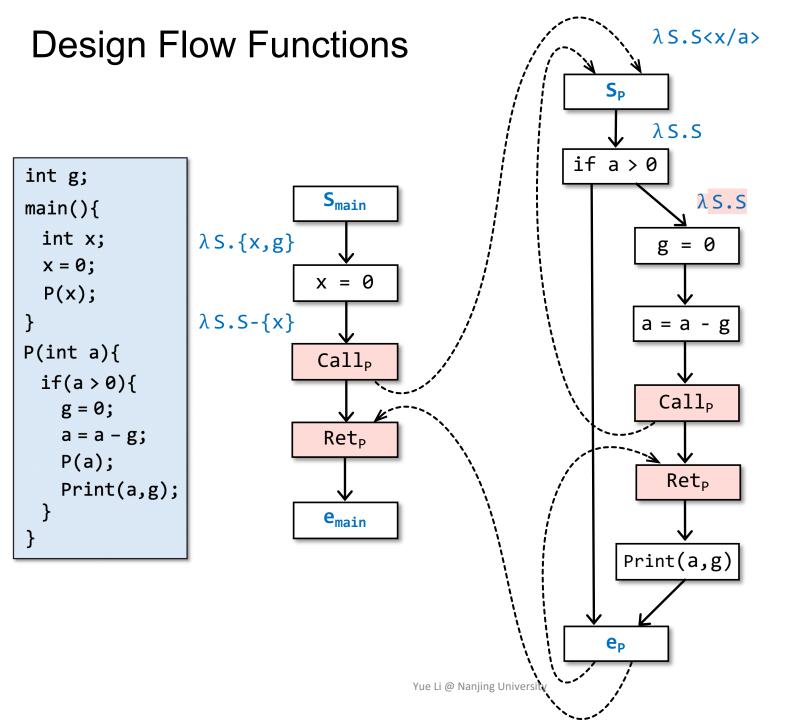


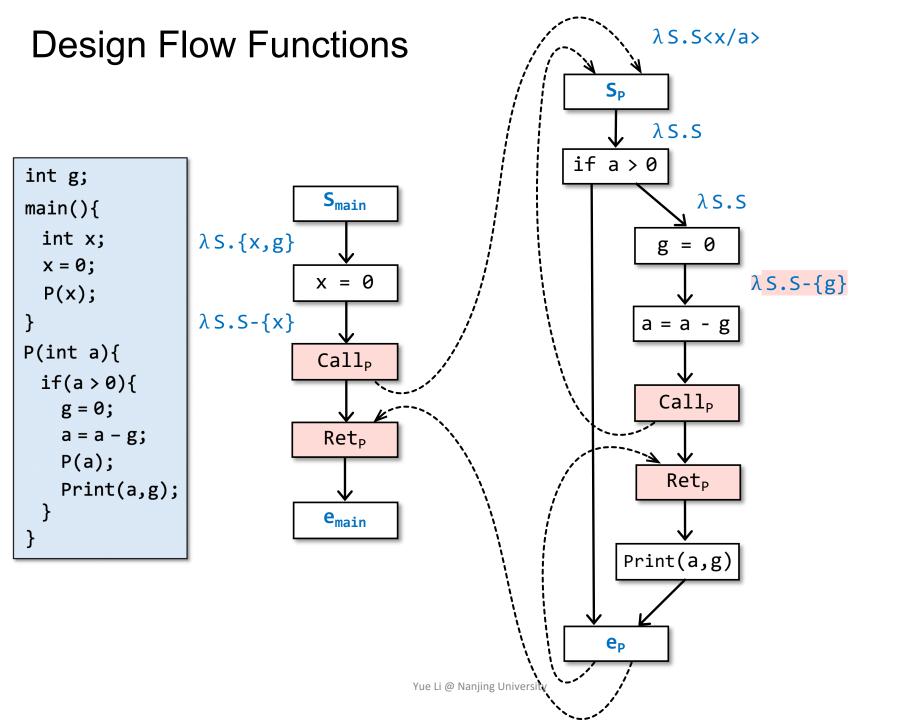


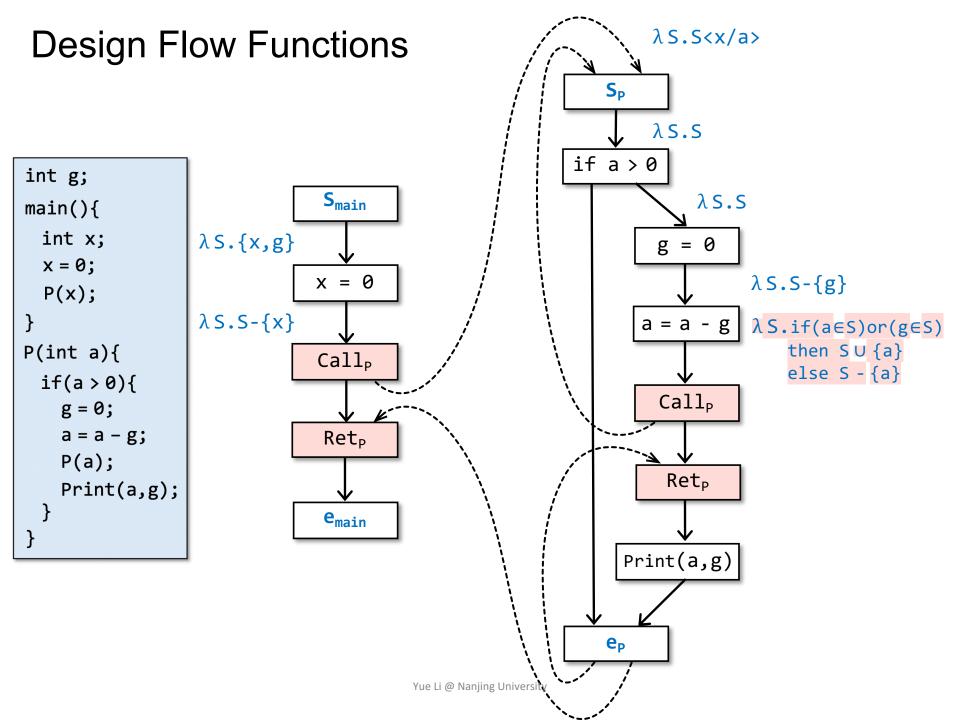


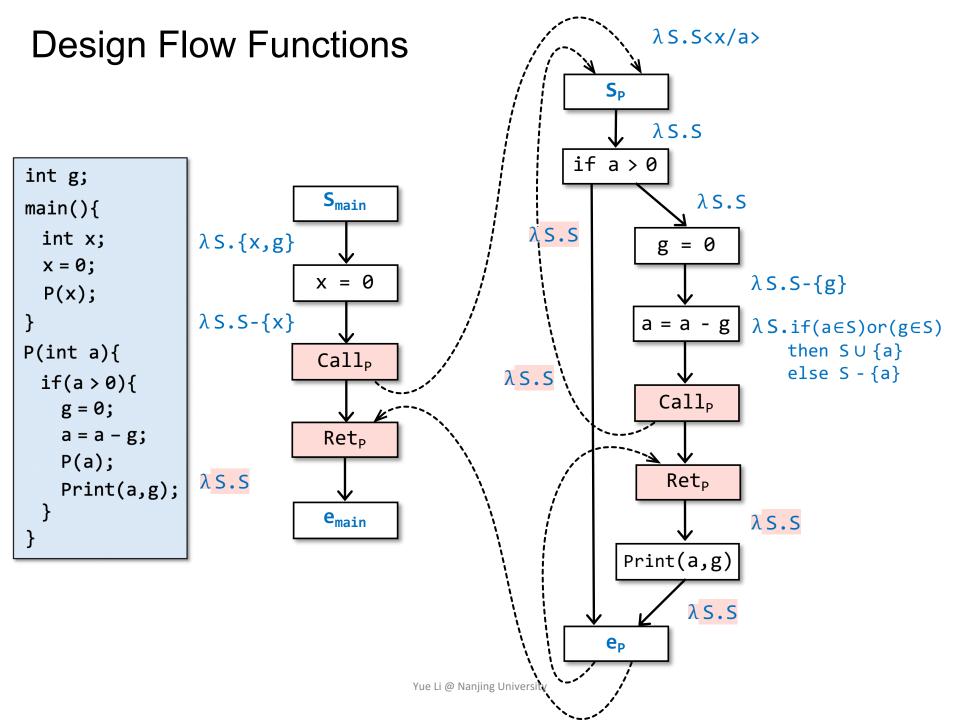


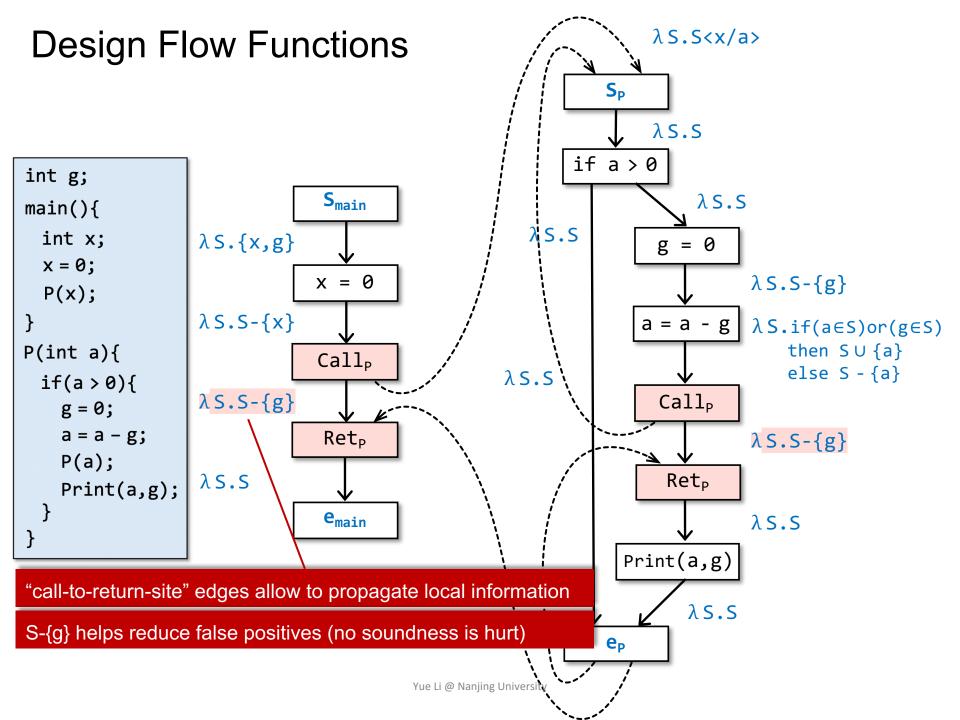


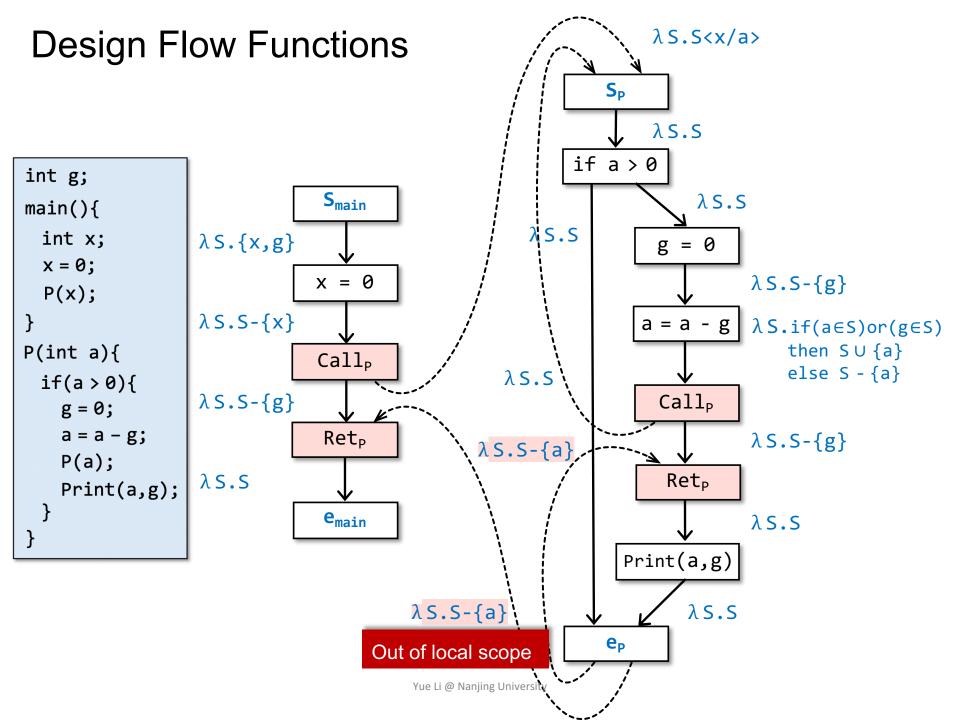


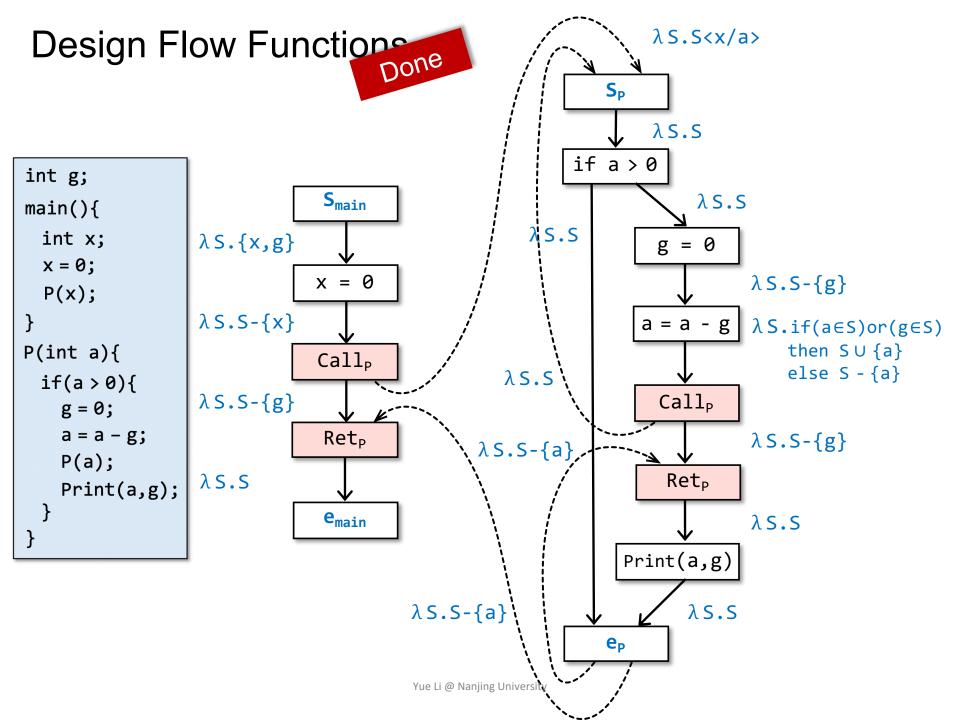








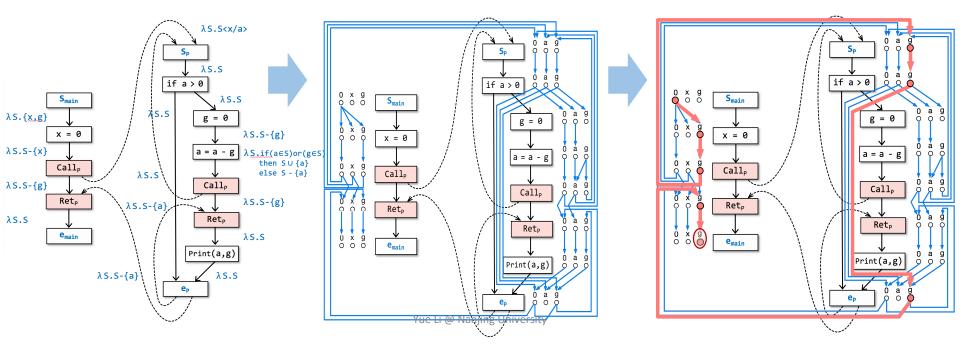




## **Overview of IFDS**

Given a program P, and a dataflow-analysis problem Q

- Build a supergraph G\* for P and define flow functions for edges in G\* based on Q
- Build exploded supergraph G<sup>#</sup> for P by transforming flow functions to representation relations (graphs)
- Q can be solved as graph reachability problems (find out MRP solutions) via applying Tabulation algorithm on G<sup>#</sup>



- Build exploded supergraph G<sup>#</sup> for a program by transforming flow functions to representation relations (graphs)
- Each flow function can be represented as a graph with 2(D+1) nodes (at most (D+1)<sup>2</sup> edges), where D is a finite set of dataflow facts

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λS.S	λS.{a}	λ <b>S.(S-</b> {a})∪{b}	λS.ifa∈S thenS∪{b} elseS-{b}
0 a b	0 a b	0 a b c	0 a b c
0 0 0	0 0 0	0 0 0 0	0 0 0 0
0 0 0	0 0 0	OOOOO	0 0 0 0
0 a b	0 a b	Yue Li Olanjing University C	0 a b c

x g 0 0 0

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                                 	0 0 0 0 a b	OOOOO Yue Li @Wanjing University C	0 0 0 0 0 a b c

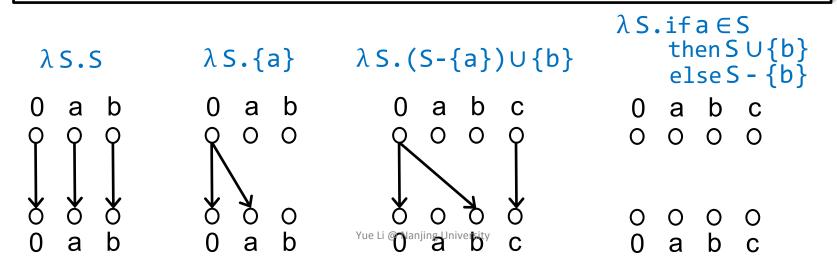
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	0 0 0 0 a b	OOOOOO Yue Li Manjing University C	0 0 0 0 0 a b c

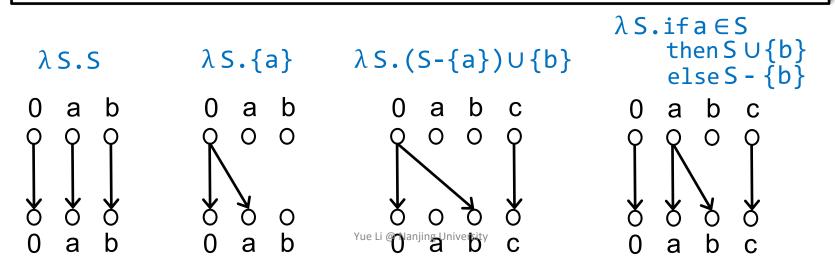
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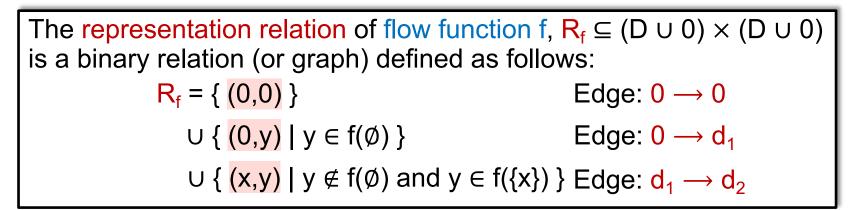
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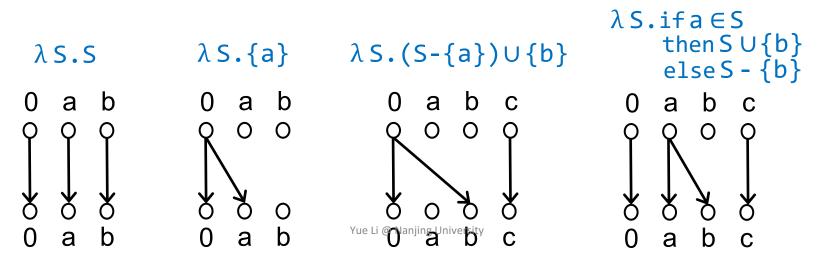
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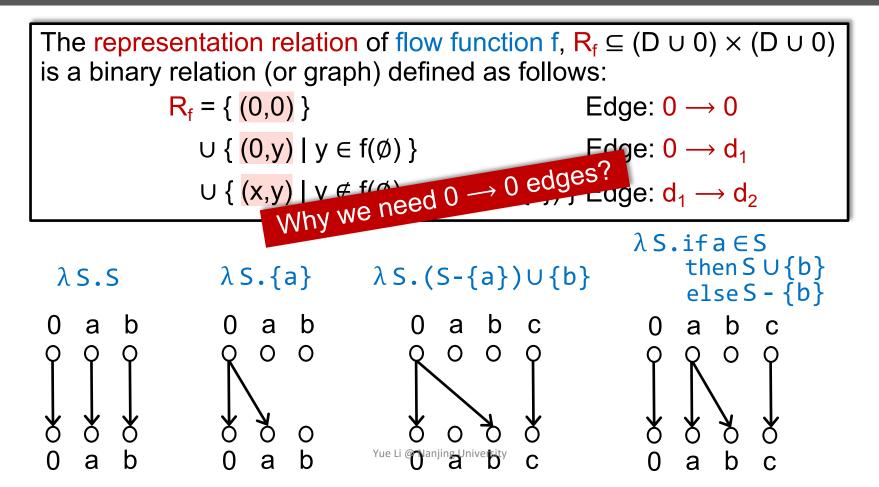
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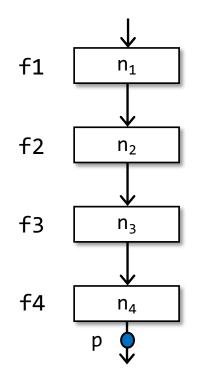
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In traditional data flow analysis, to see whether data fact a holds at program point p, we check if a is in  $OUT[n_4]$  after the analysis finishes

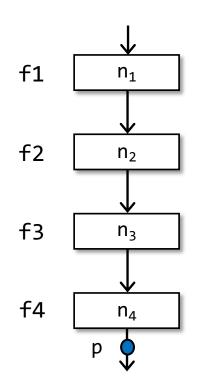
 $OUT[n_4] = f4 \circ f3 \circ f2 \circ f1(IN[n1])$ 



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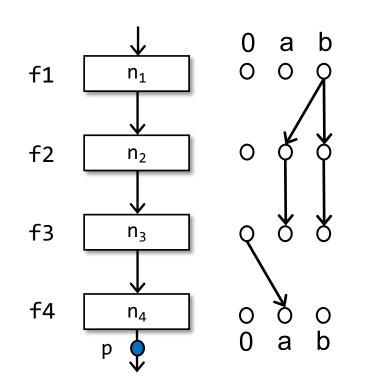
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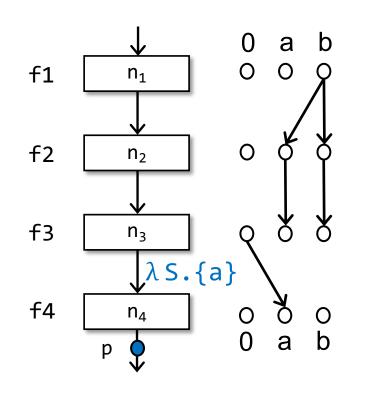


For the same case, in IFDS, whether data fact a holds at p depends on if there is a path from  $<s_{main}$ , 0> to  $<n_4,a>$ , and the "reachability" is retrieved by connecting the edges (finding out a path) on the "pasted" representation relations

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 $\lambda$  S. {a} says a holds at p regardless of input S; however, without edge  $0 \rightarrow 0$ ,

the representation relation for each edge cannot be connected or "pasted" together, like flow functions cannot be composed together in traditional data flow analysis.

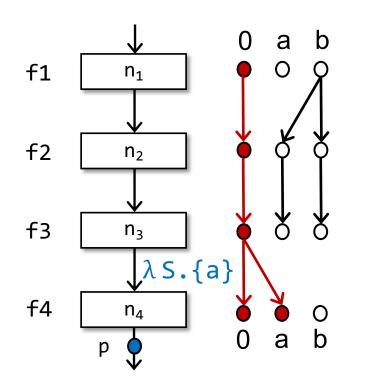
Thus IFDS cannot produce correct solutions via such disconnected representation relations.

## So We Need the "Glue Edge" $0 \rightarrow 0!$

In traditional data flow analysis, to see whether data fact a holds at program point p, we check if a is in  $OUT[n_4]$  after the analysis finishes

 $OUT[n_4] = f4 \circ f3 \circ f2 \circ f1(IN[n1])$ 

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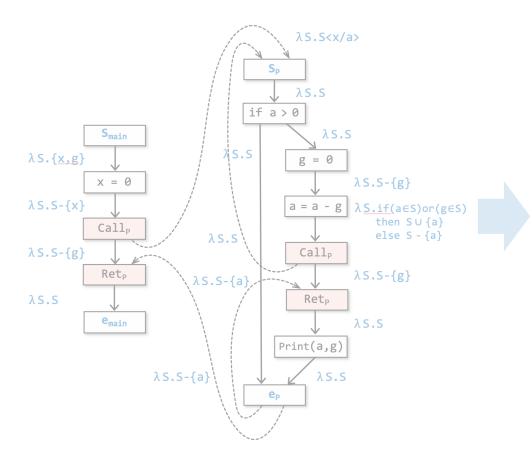
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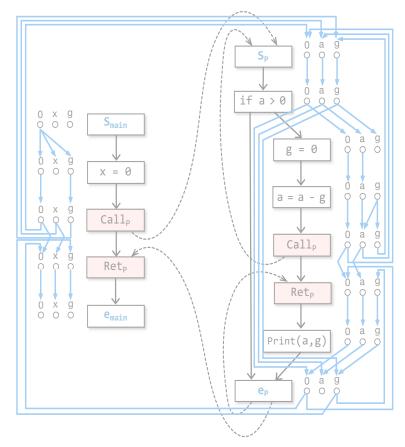
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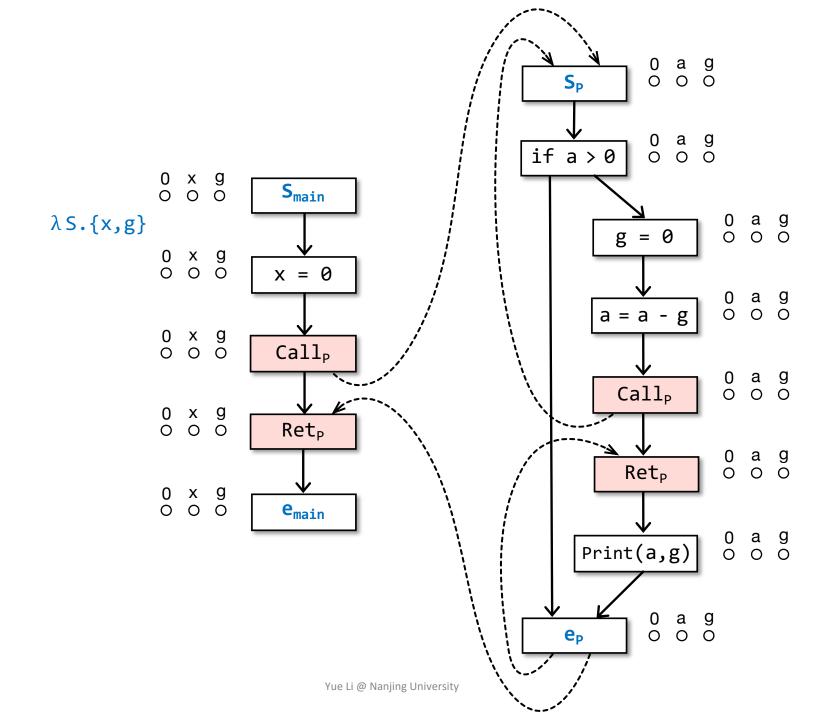
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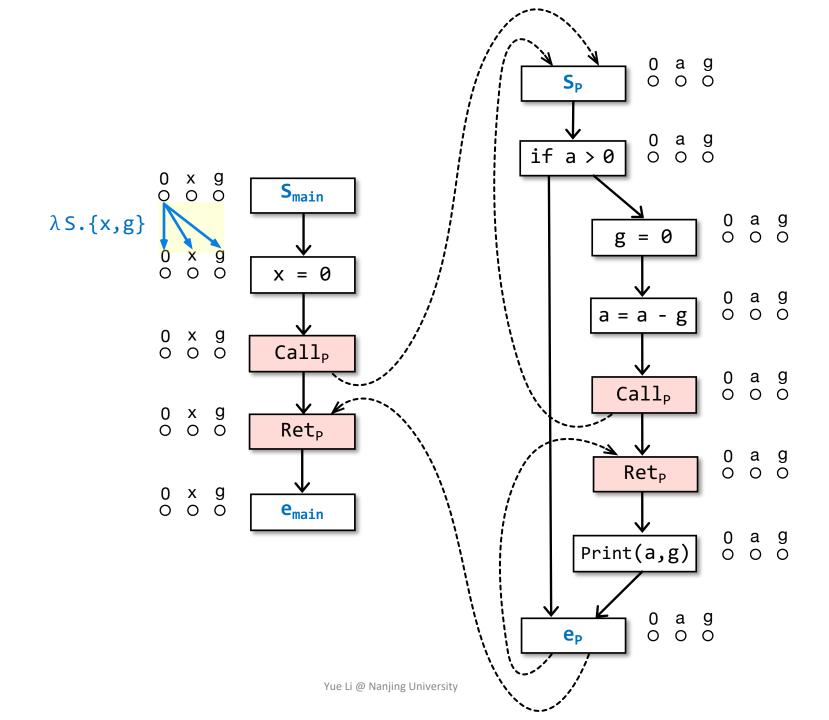
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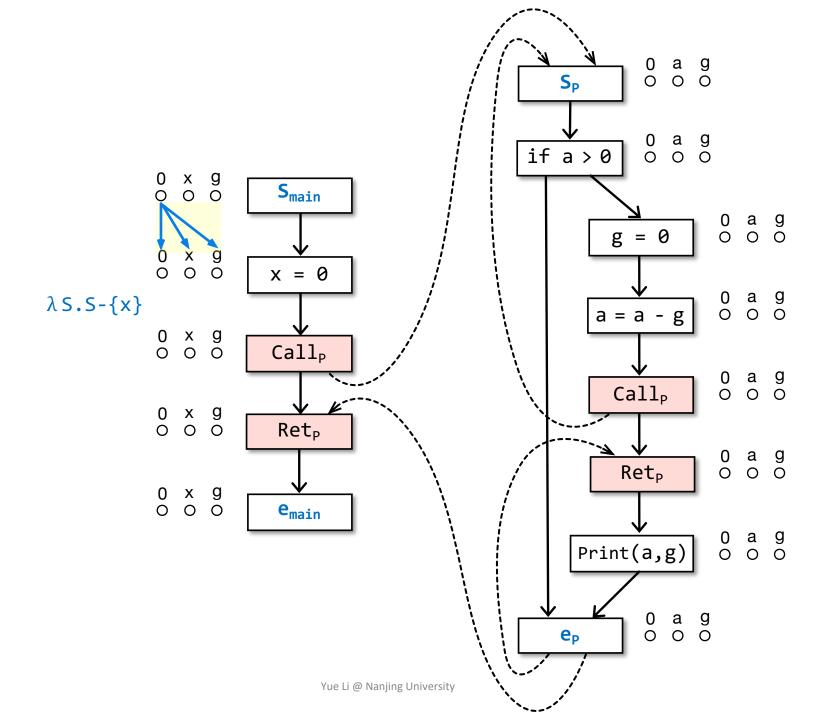
## Now, let's build an exploded supergraph

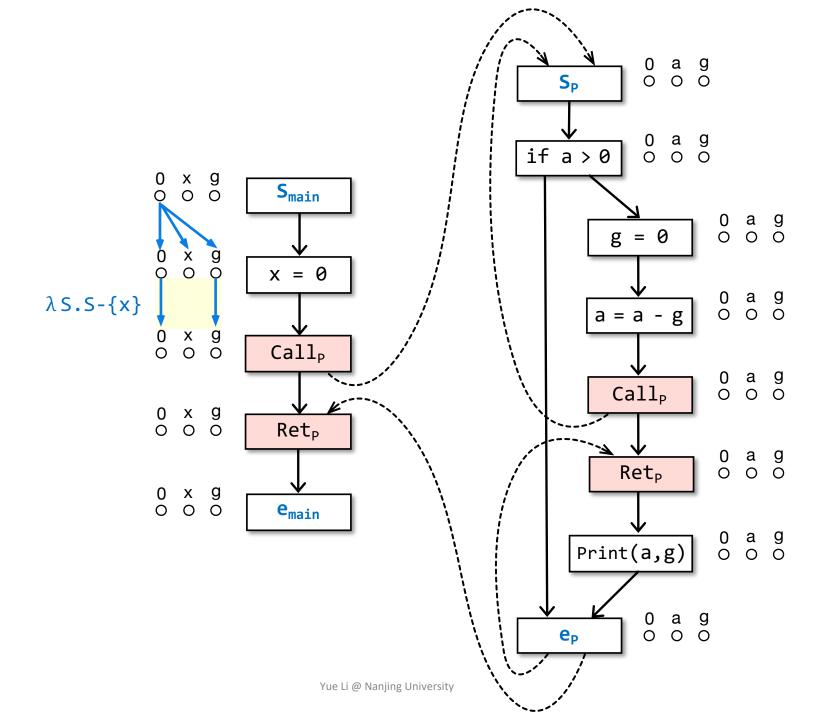


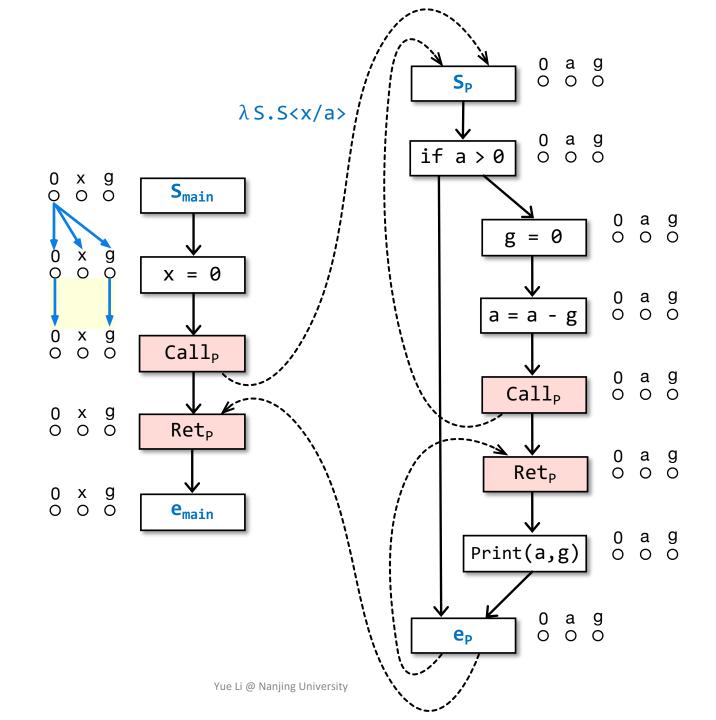


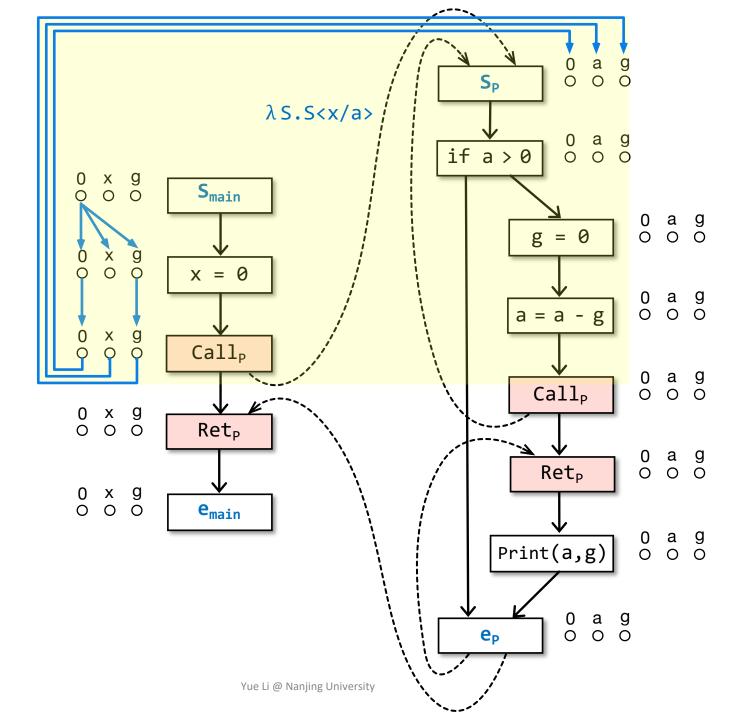


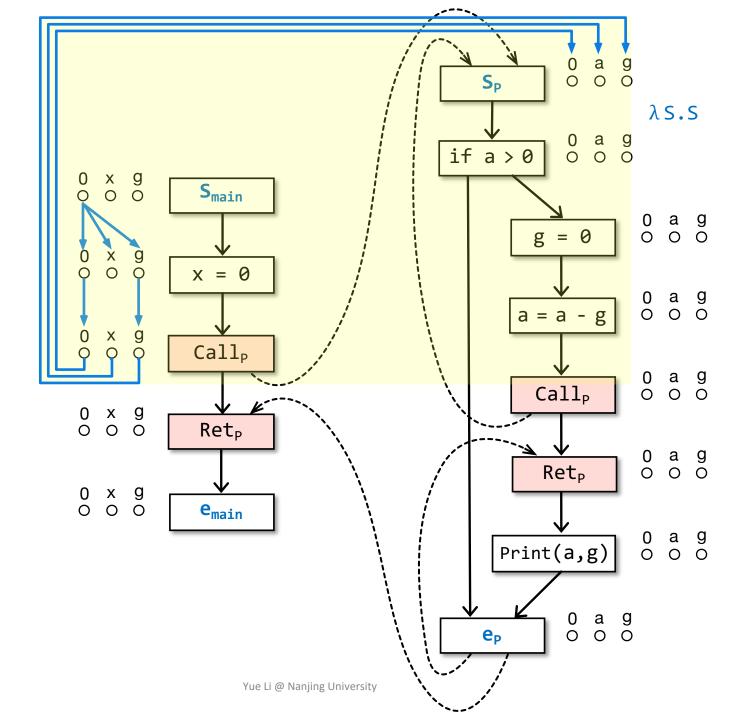


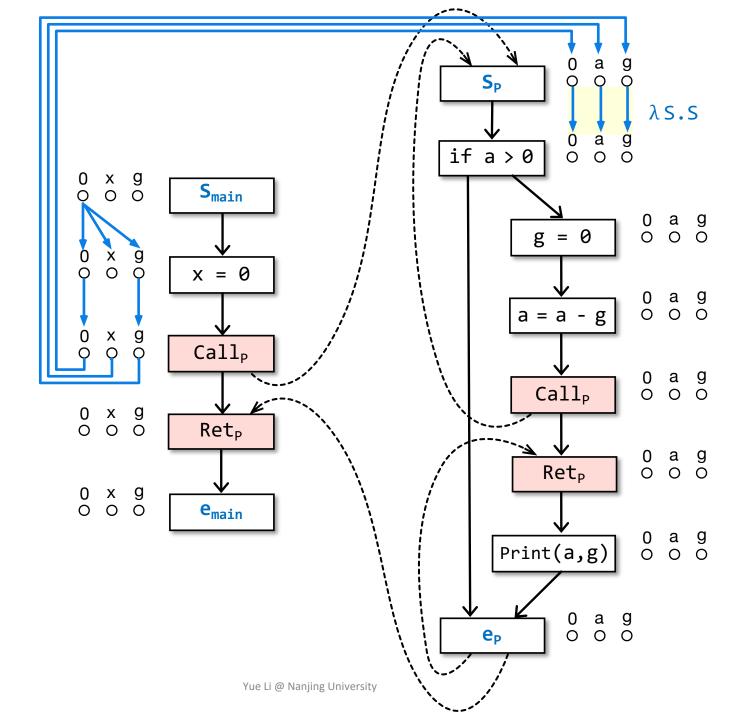


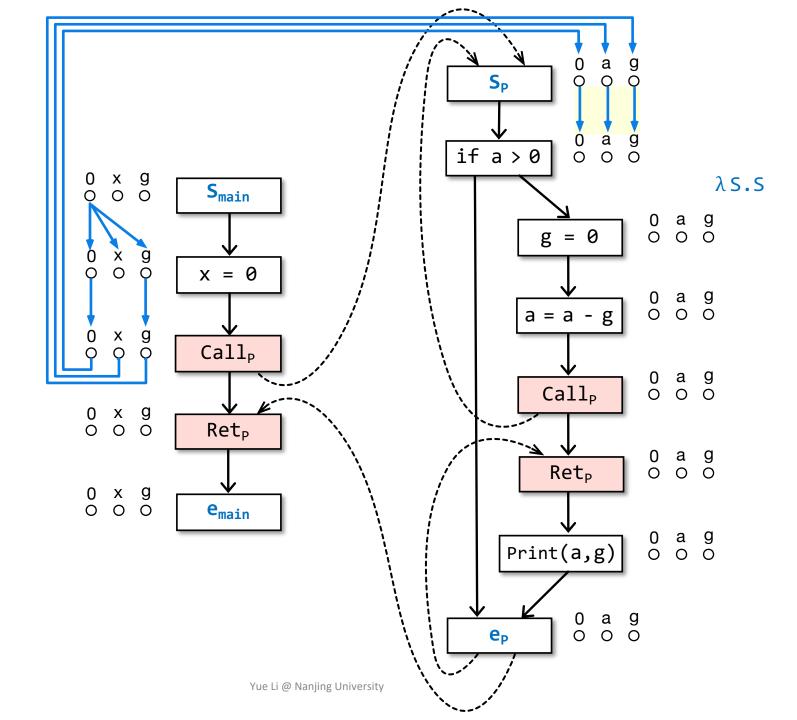


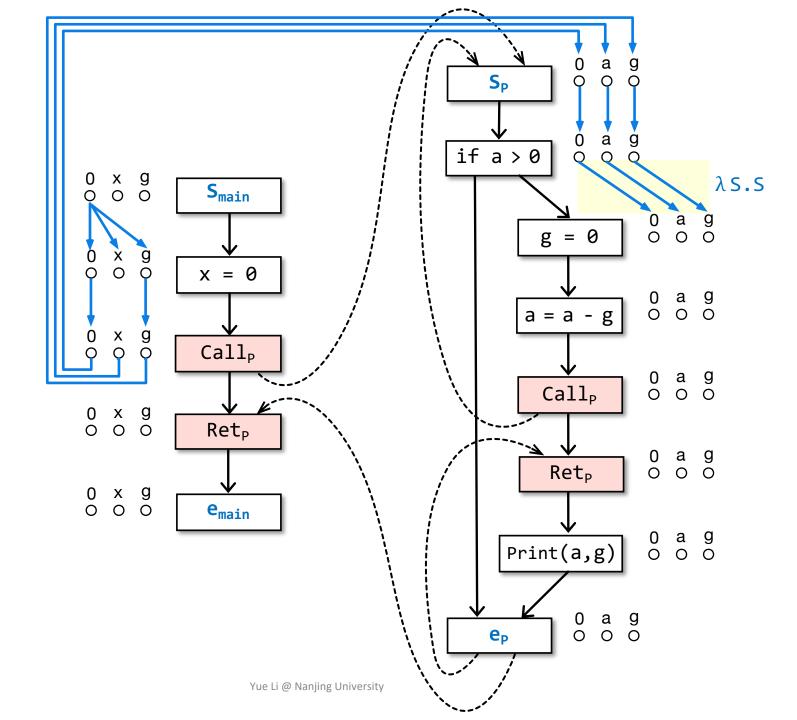


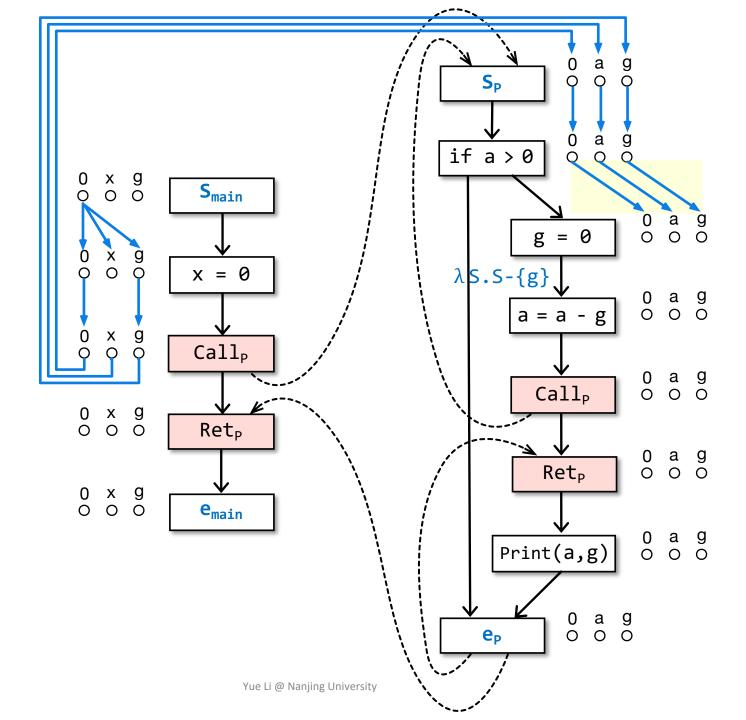


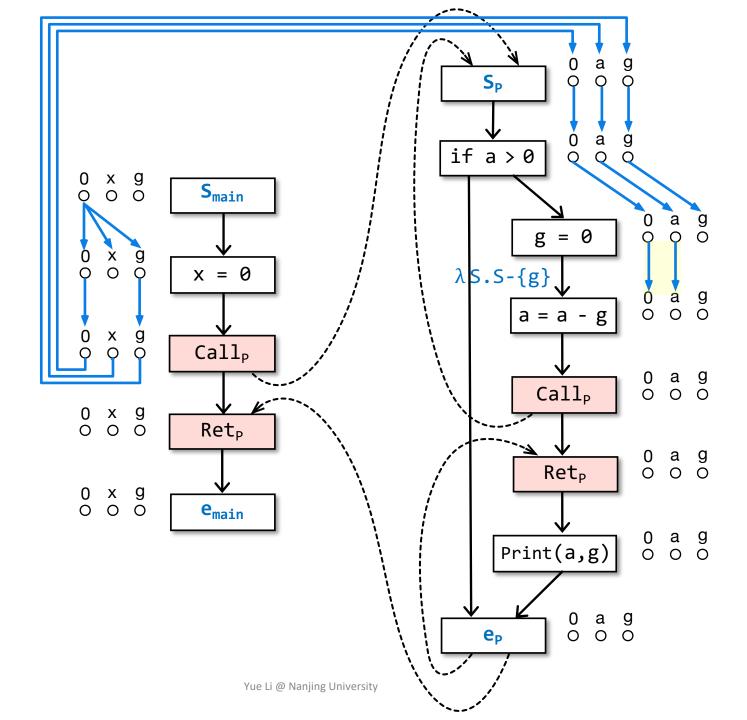


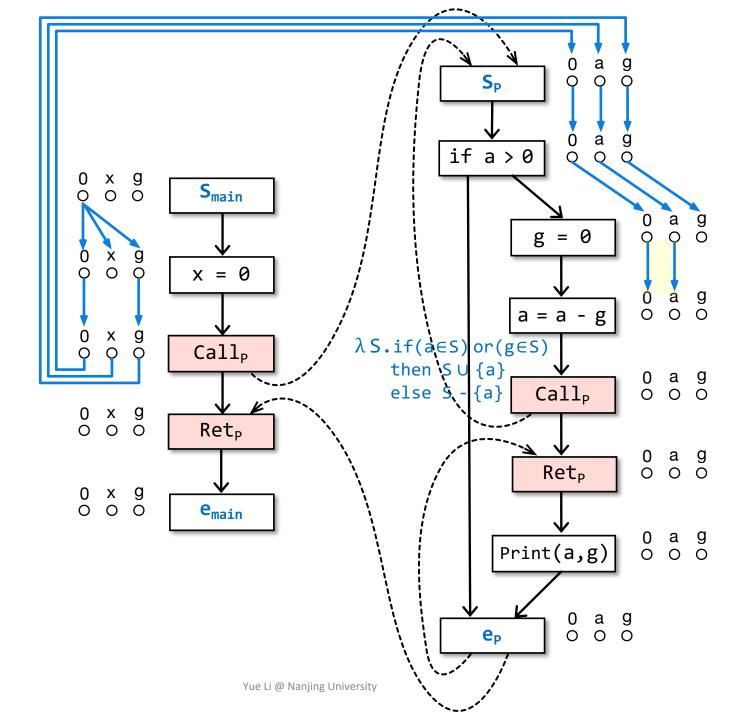


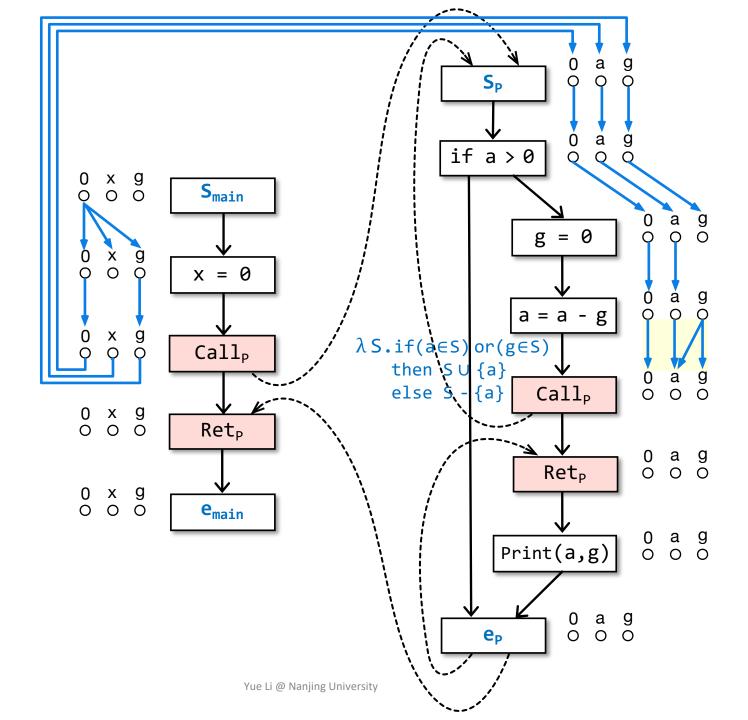


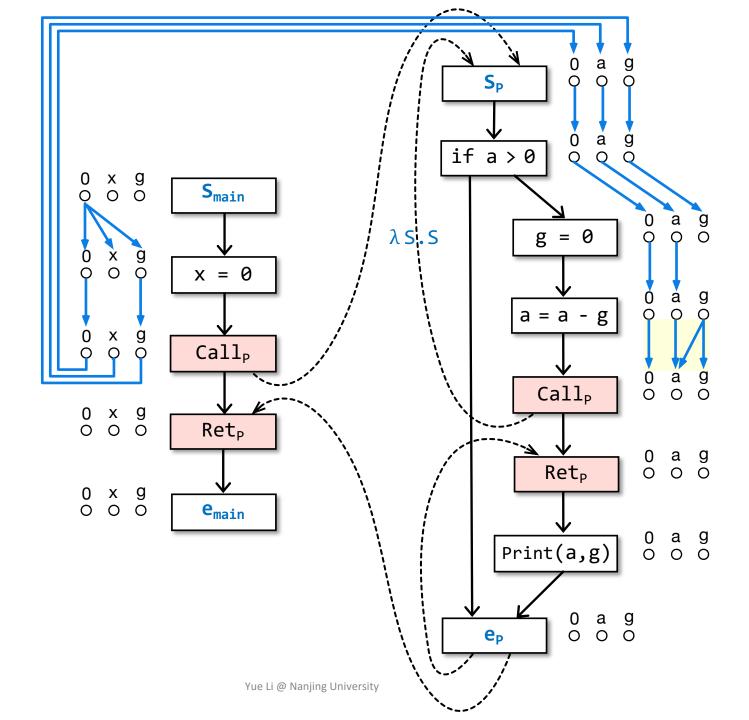


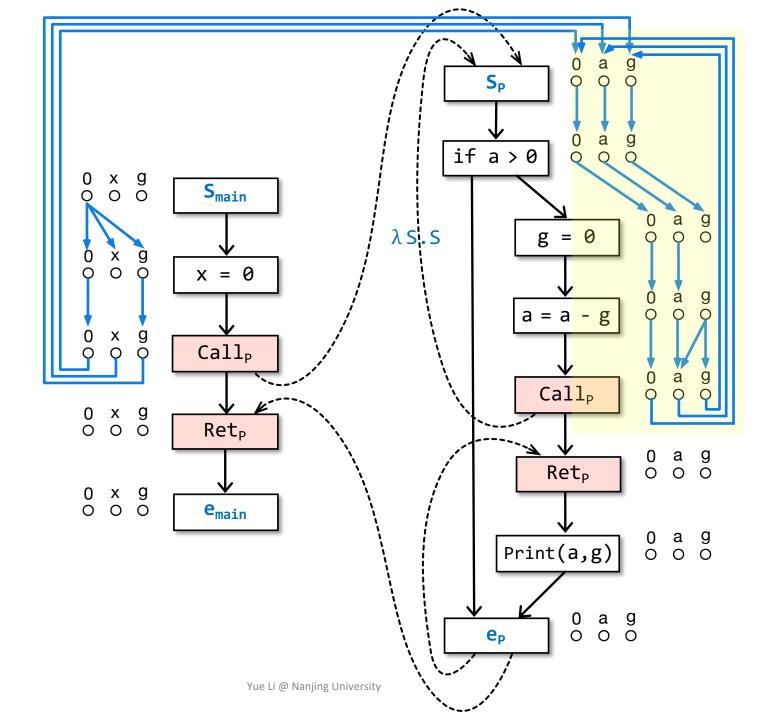


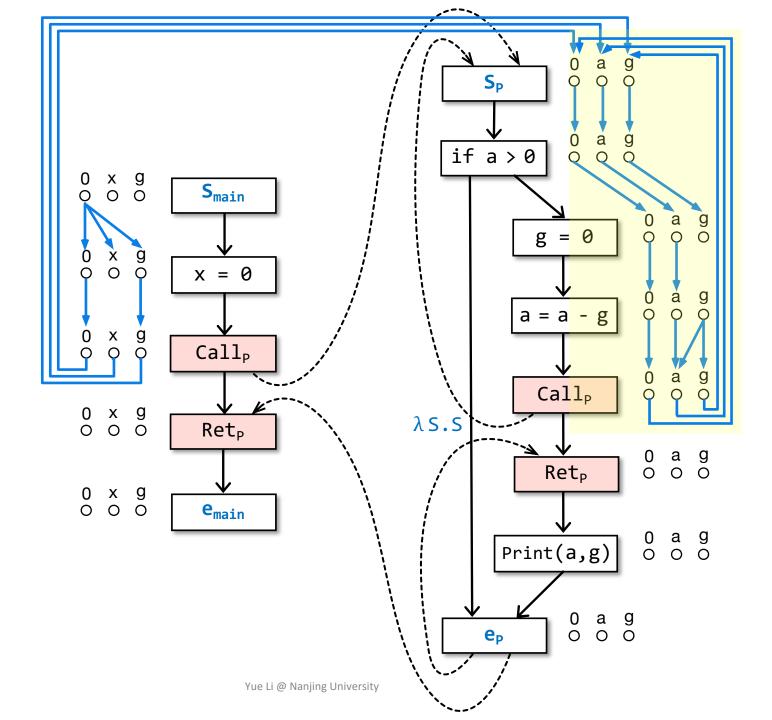


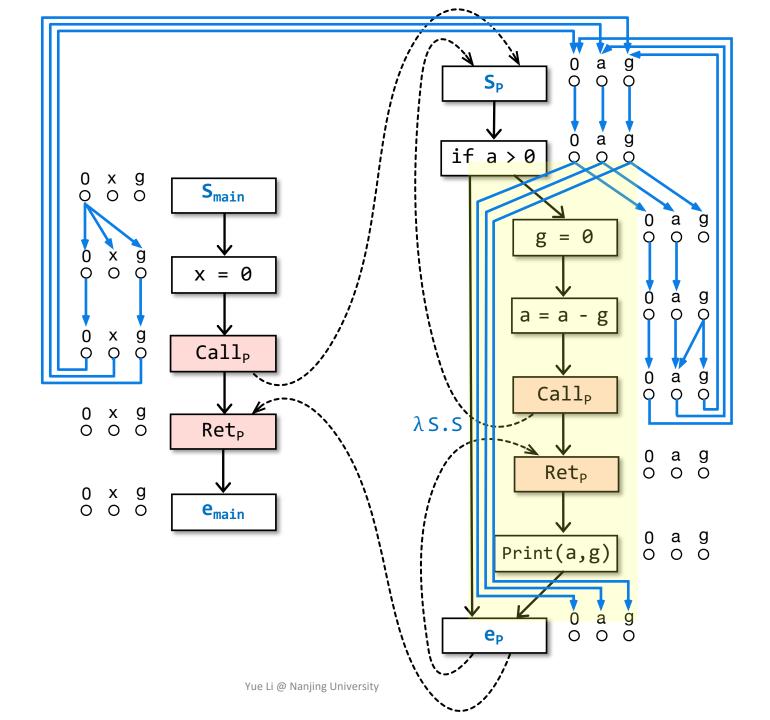


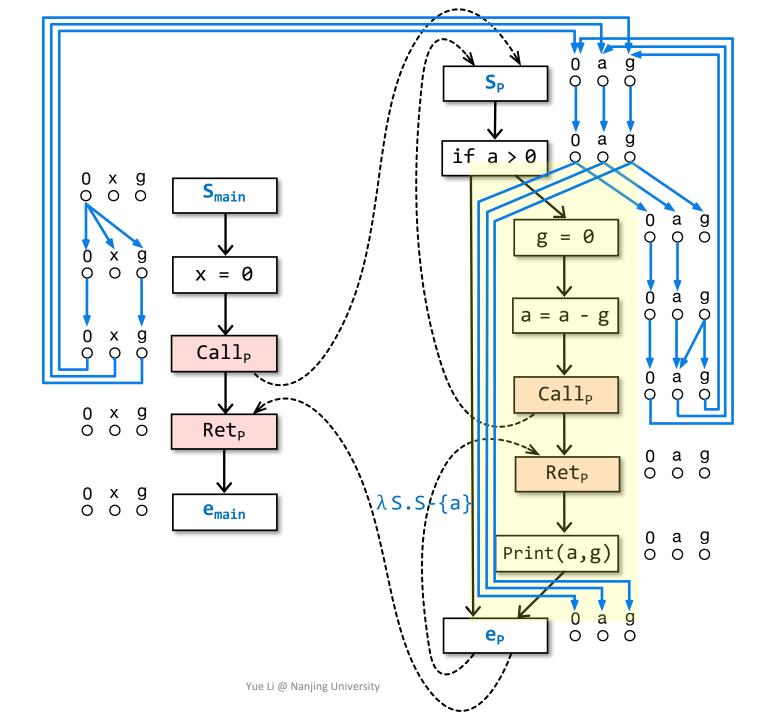


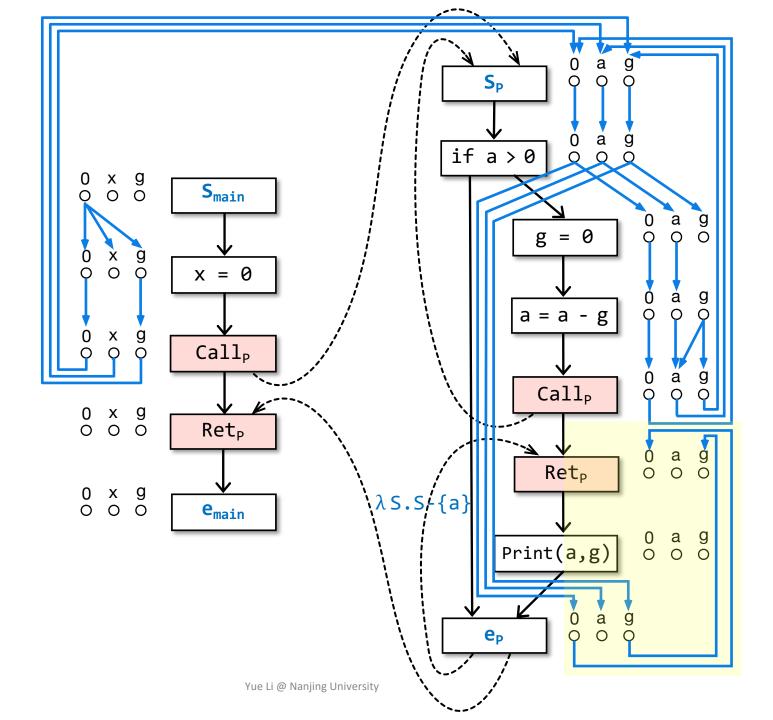


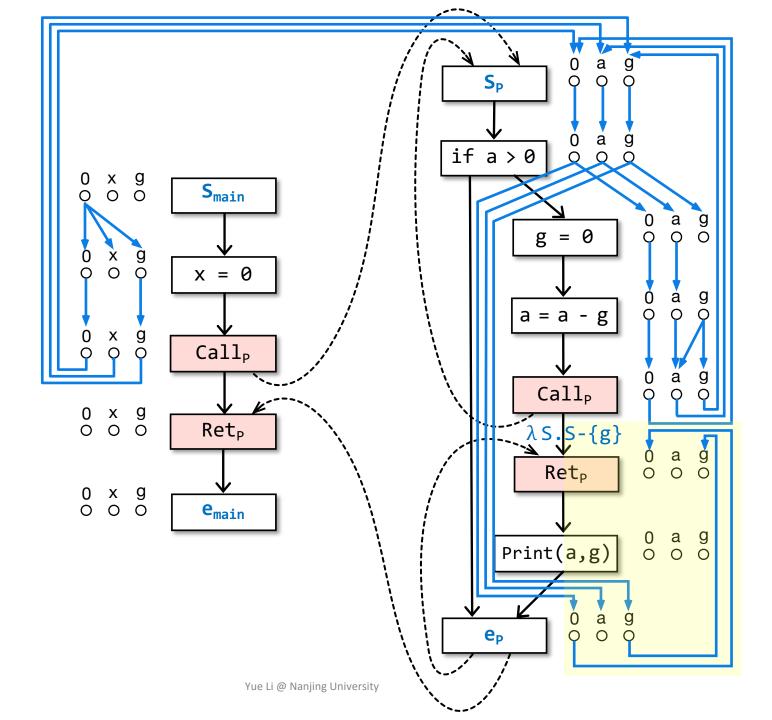


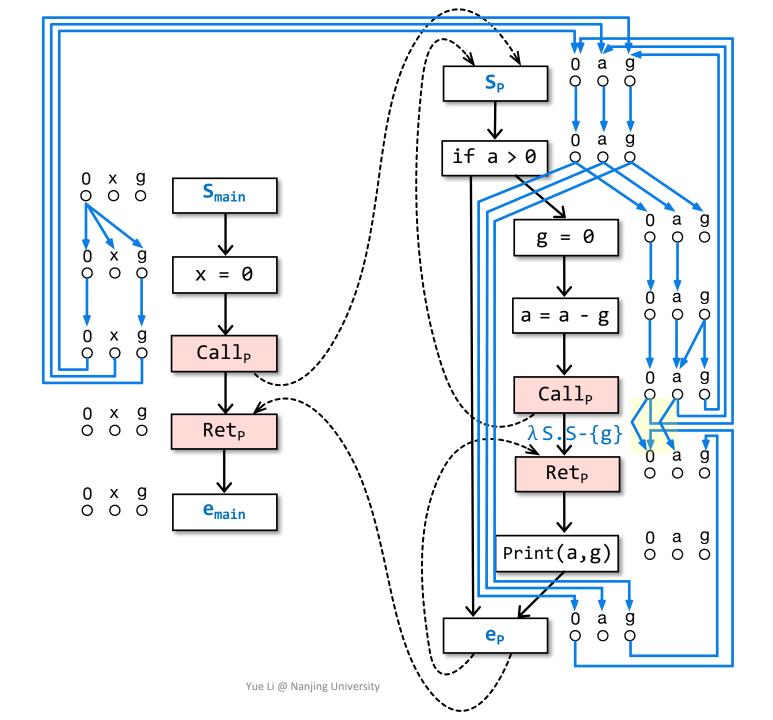


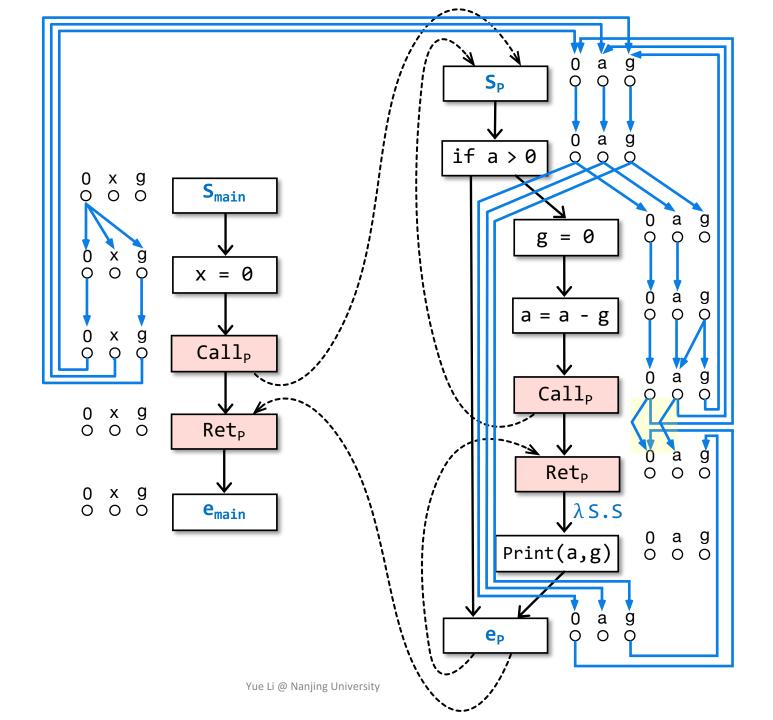


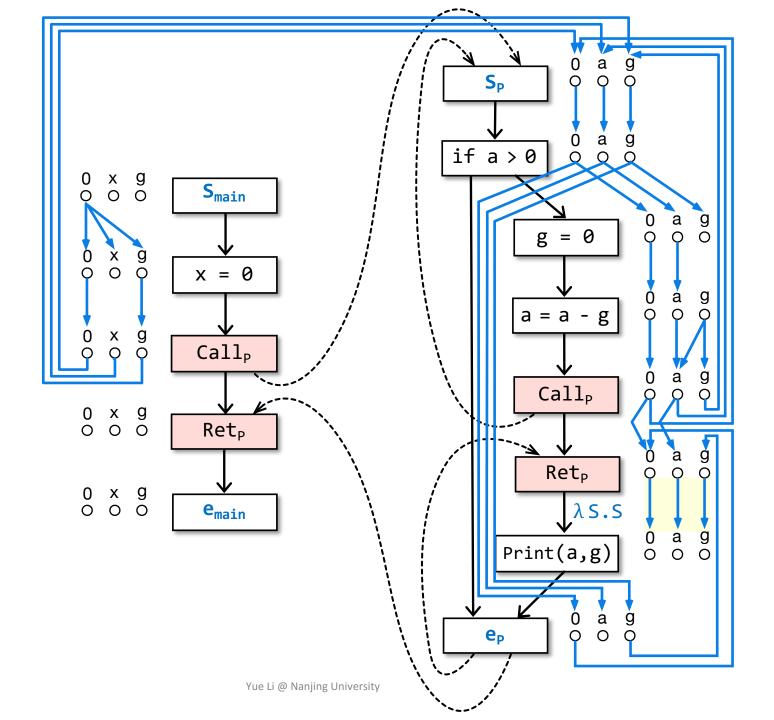


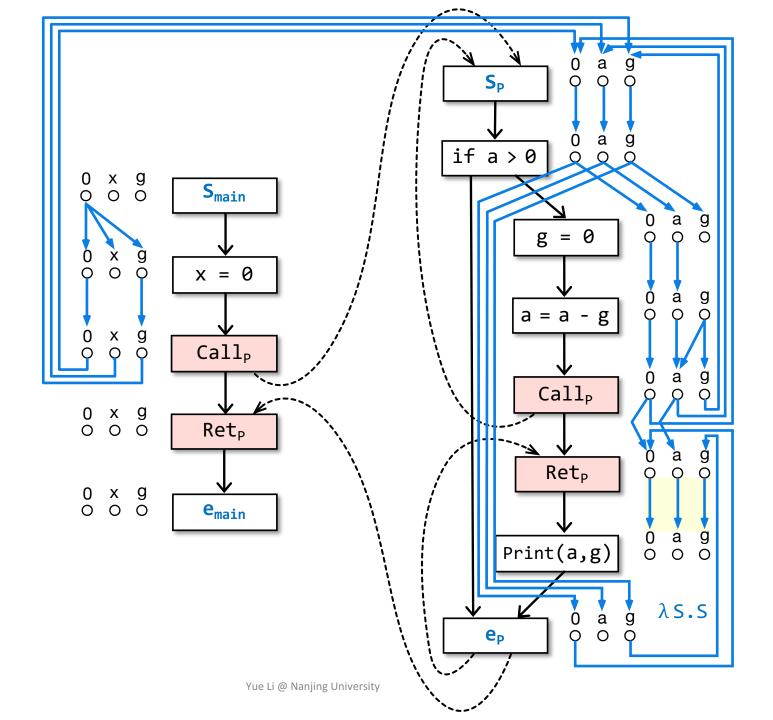


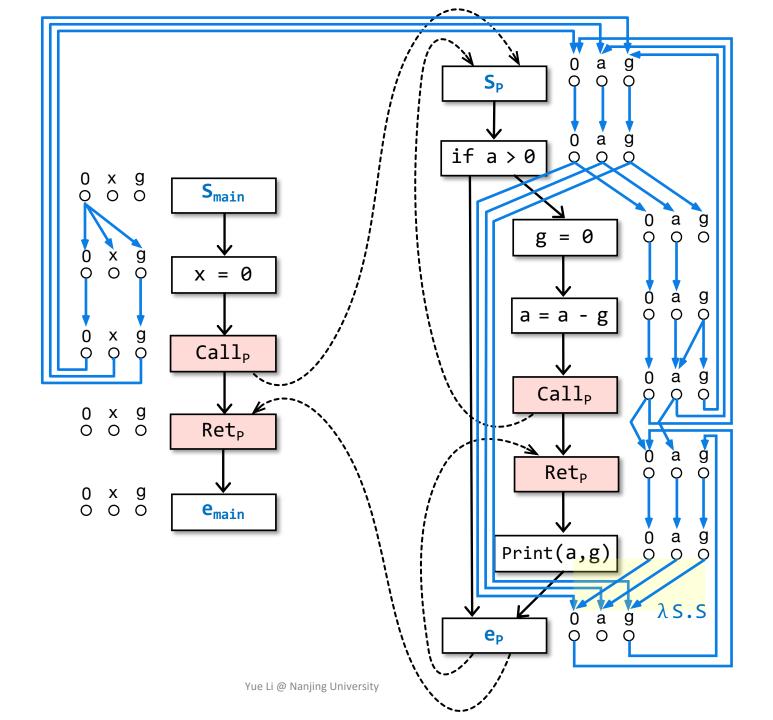


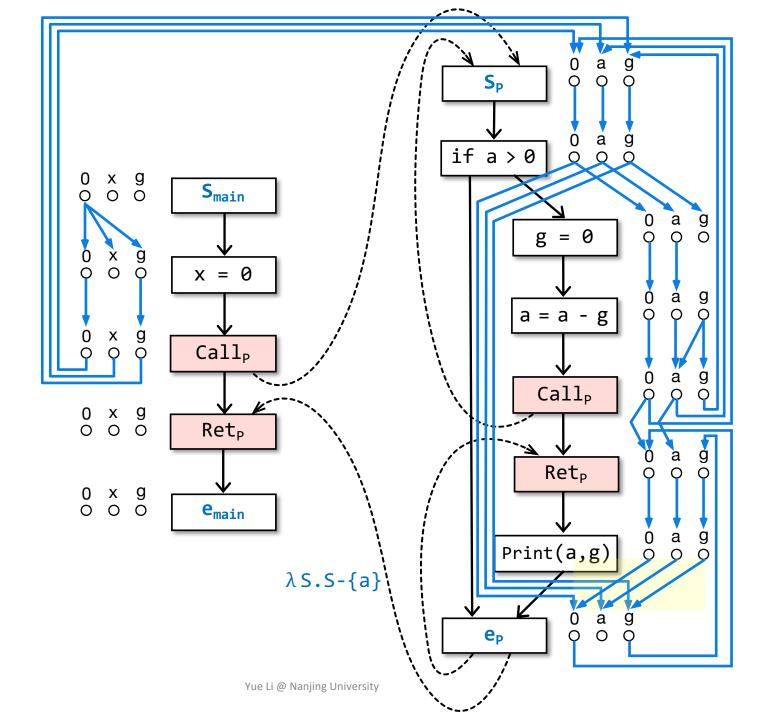


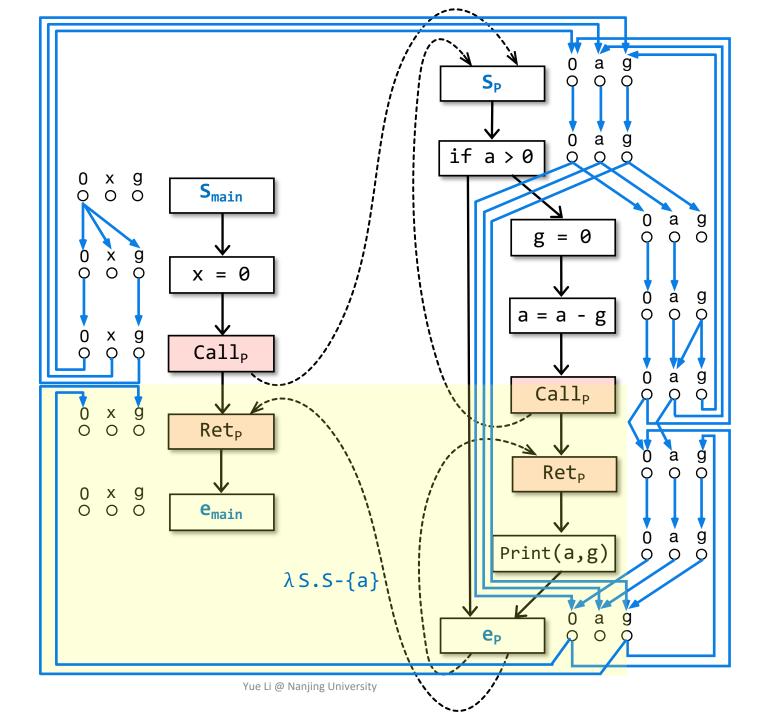


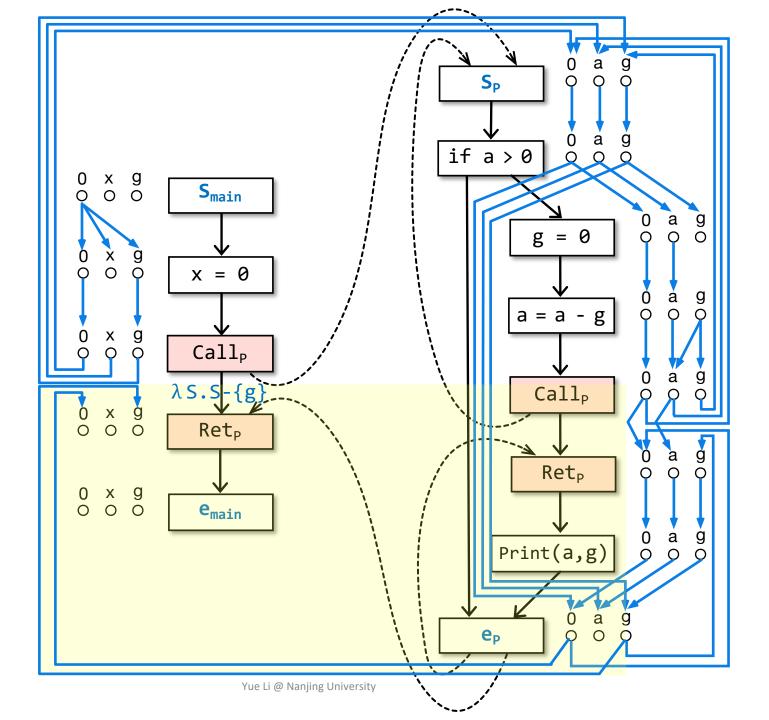


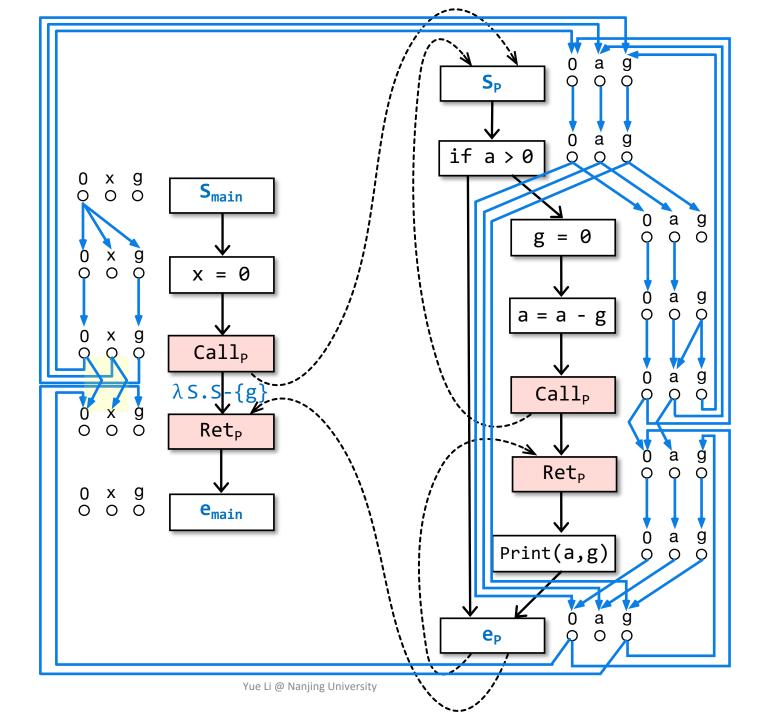


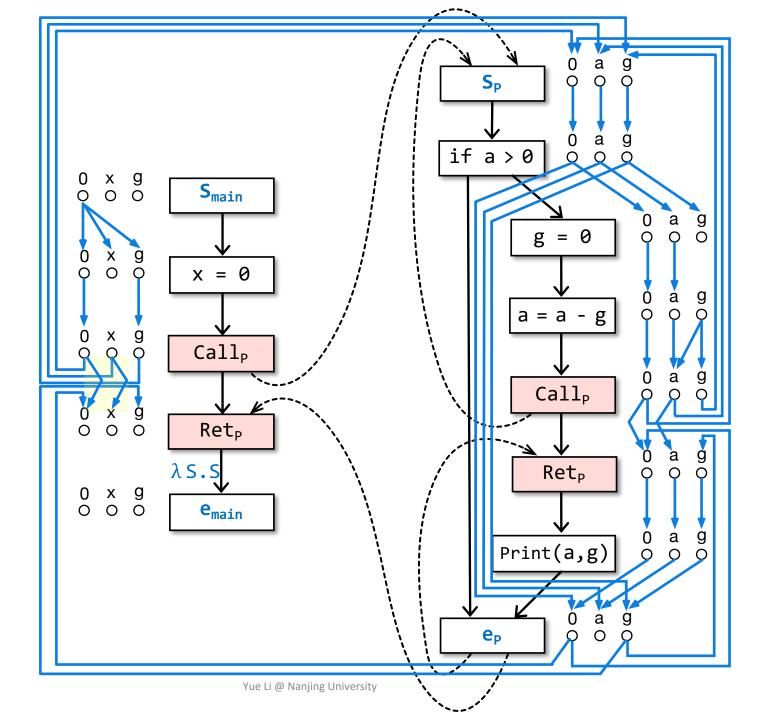


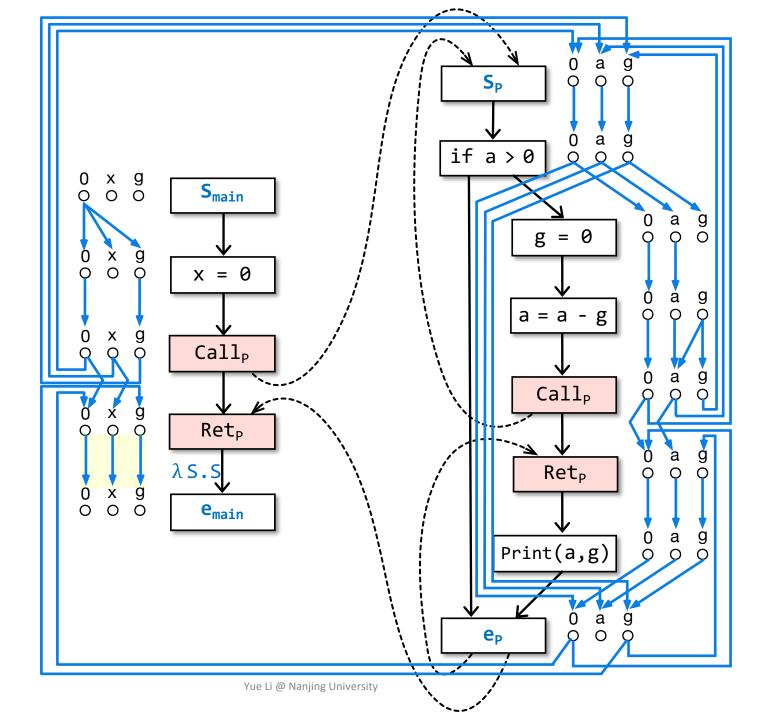


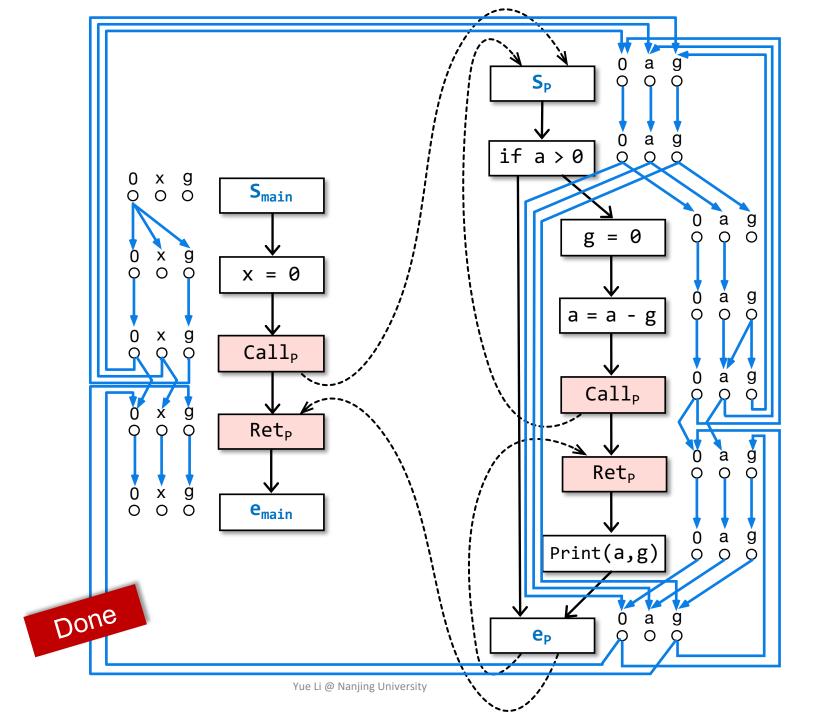


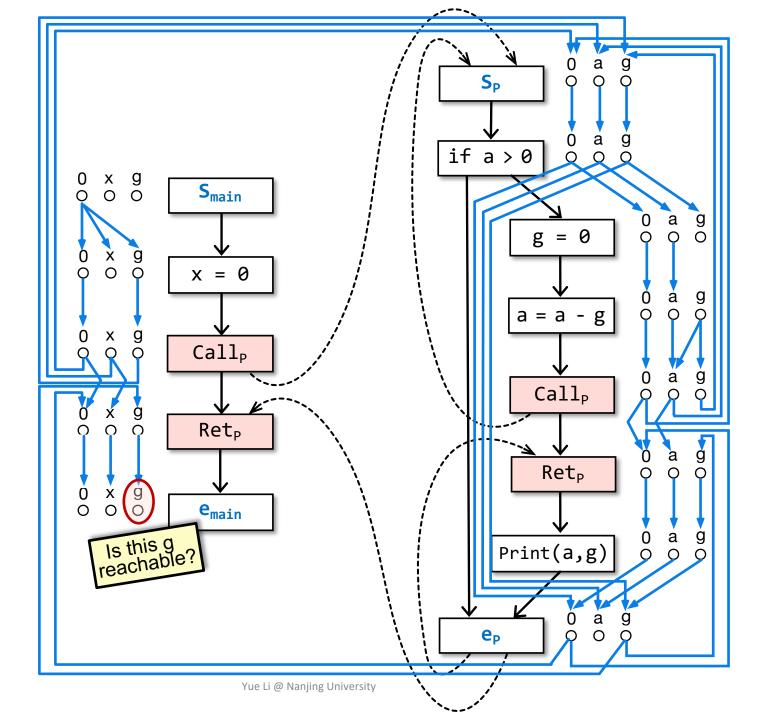


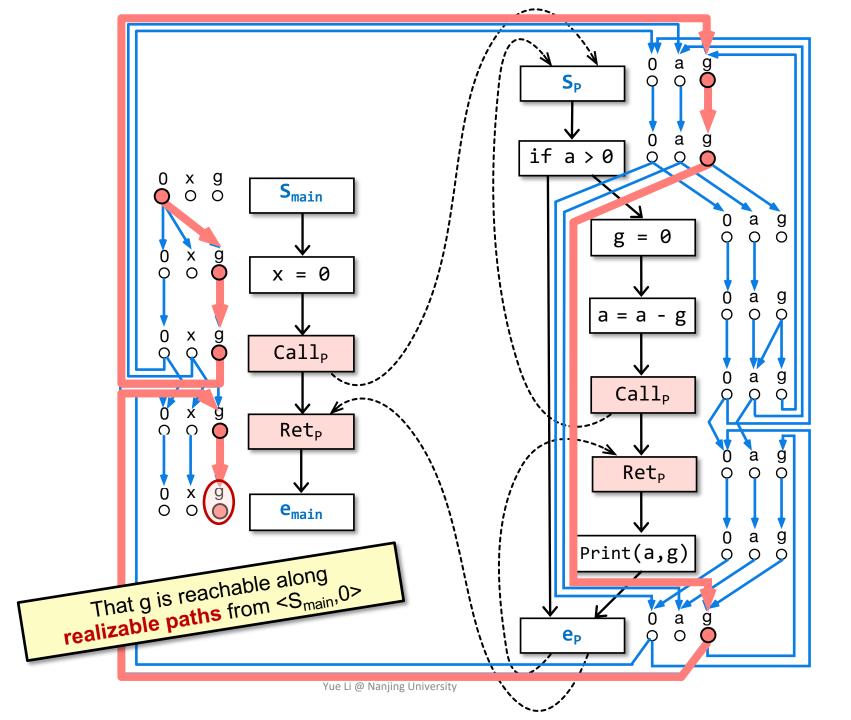


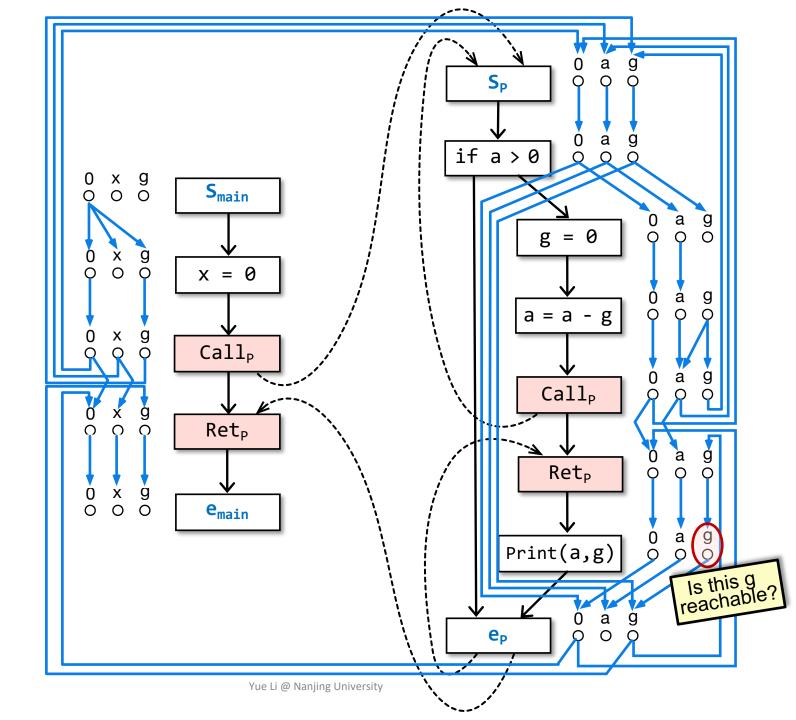


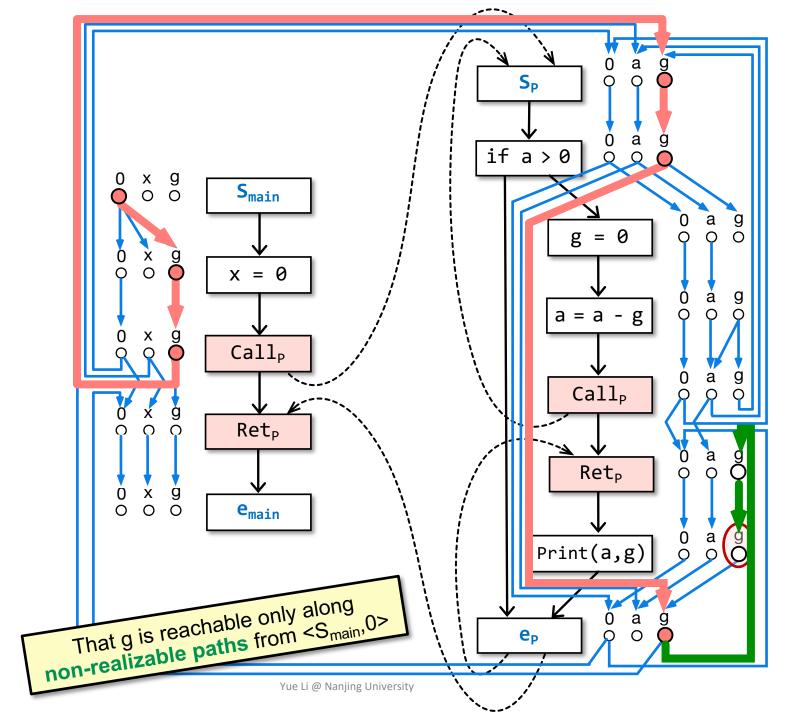


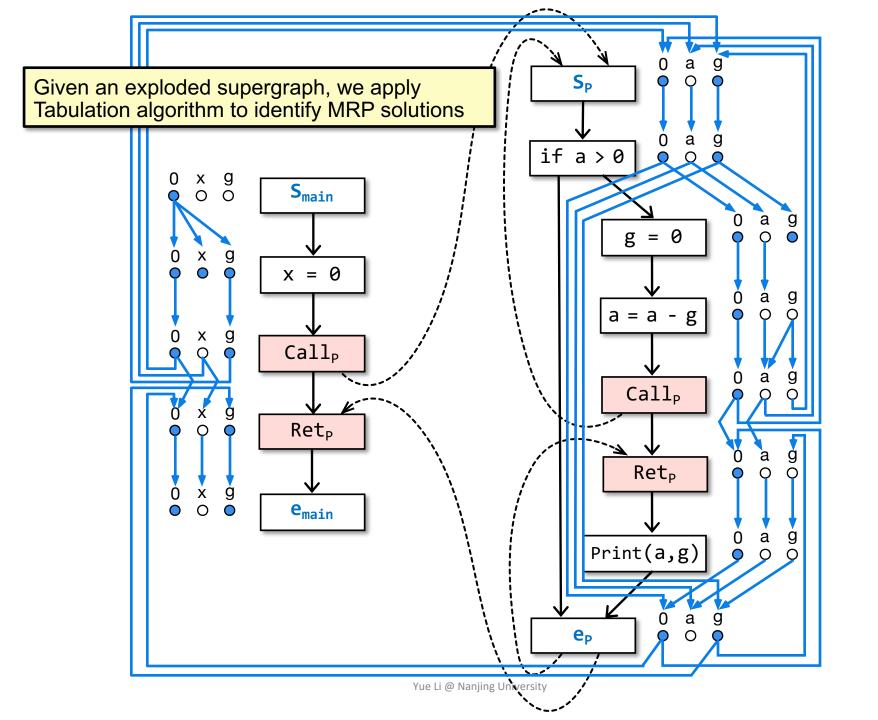


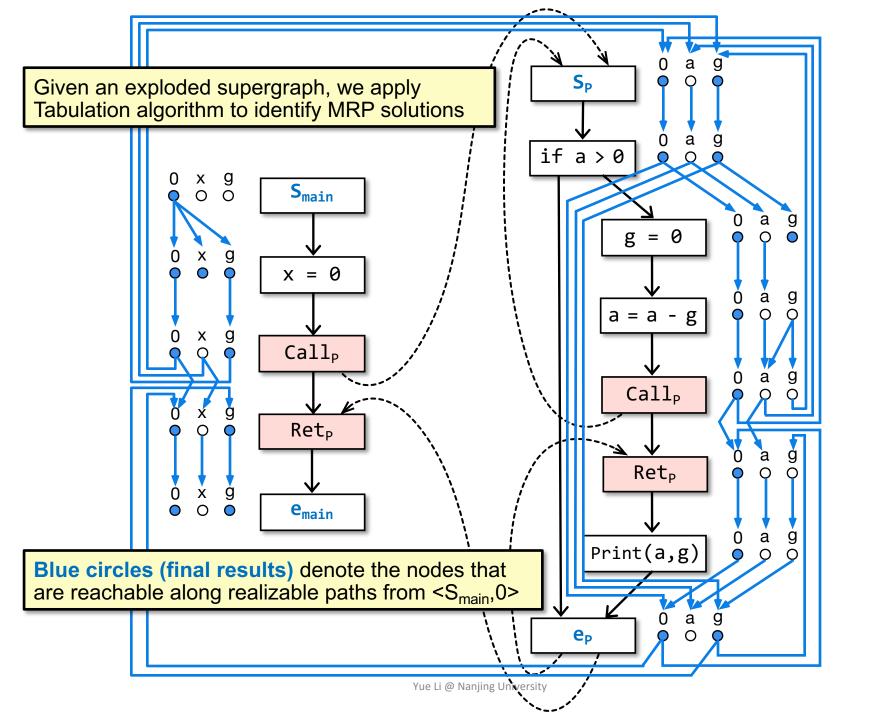


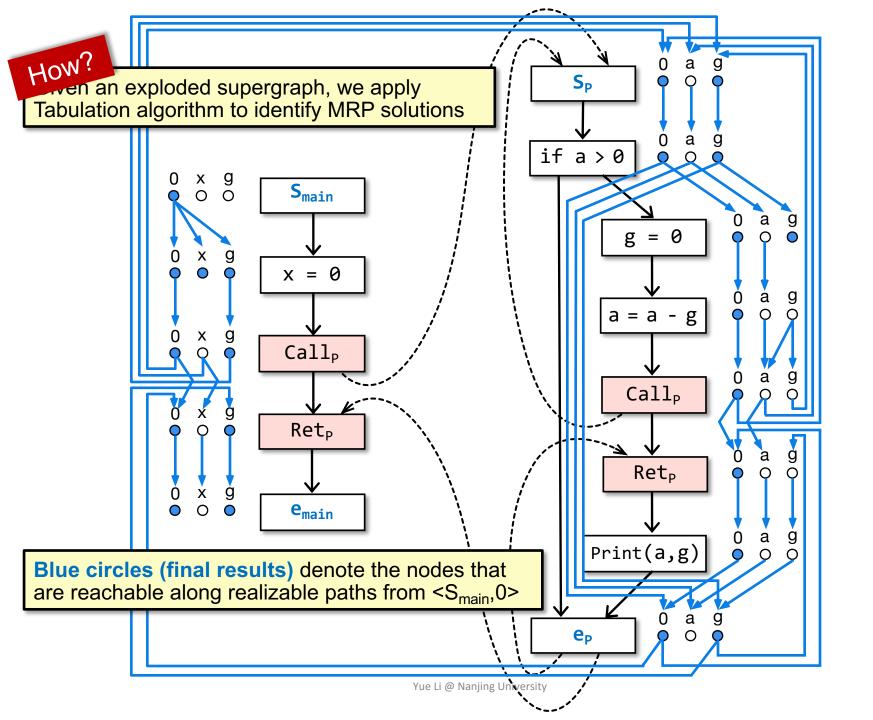








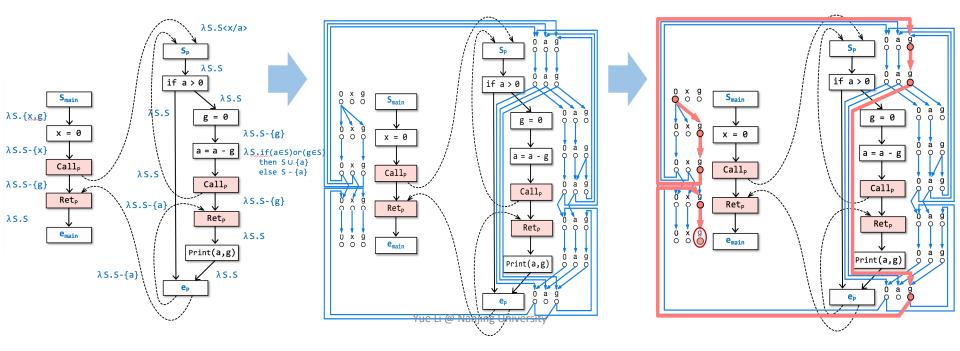




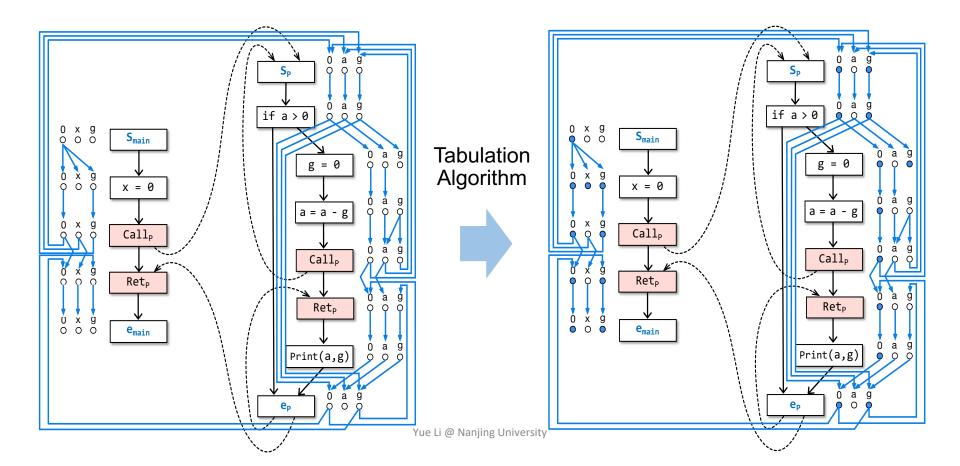
## **Overview of IFDS**

Given a program P, and a dataflow-analysis problem Q

- Build a supergraph G\* for P and define flow functions for edges in G\* based on Q
- Build exploded supergraph G<sup>#</sup> for P by transforming flow functions to representation relations (graphs)
- Q can be solved as graph reachability problems (find out MRP solutions) via applying Tabulation algorithm on G<sup>#</sup>

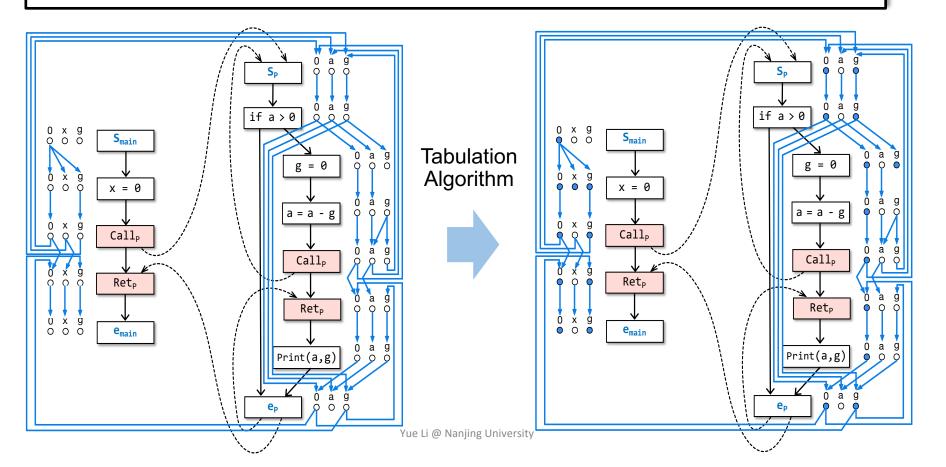


Given an exploded supergraph  $G^{\#}$ , Tabulation algorithm determines the MRP solution by finding out all realizable paths starting from  $< s_{main}$ , 0 >



Given an exploded supergraph  $G^{\#}$ , Tabulation algorithm determines the MRP solution by finding out all realizable paths starting from  $< s_{main}$ , 0 >

Let **n** be a program point, data fact  $d \in MRP_n$ , iff there is a realizable path in G<sup>#</sup> from  $<s_{main}$ , 0> to <n, d>. (then d's white circle turns to blue)



declare PathEdge, WorkList, SummaryEdge: global edge set **algorithm** Tabulate( $G_{IP}^{\#}$ ) begin Let  $(N^{\#}, E^{\#}) = G_{IP}^{\#}$ PathEdge := {  $\langle s_{main}^{r_{tr}}, \mathbf{0} \rangle \rightarrow \langle s_{main}, \mathbf{0} \rangle$  } WorkList := {  $\langle s_{main}, \mathbf{0} \rangle \rightarrow \langle s_{main}, \mathbf{0} \rangle$  } SummaryEdge :=  $\emptyset$ [2] [3] [4] [5] [6] ForwardTabulateSLRPs() for each  $n \in N^*$  do [7]  $X_n := \{ d_2 \in D \mid \exists d_1 \in (D \cup \{0\}) \text{ such that } \langle s_{procOf(n)}, d_1 \rangle \rightarrow \langle n, d_2 \rangle \in \text{PathEdge} \}$ 81 od end procedure Propagate(e) begin if  $e \notin PathEdge$  then Insert e into PathEdge; Insert e into WorkList fi [9] end procedure ForwardTabulateSLRPs() begin [10] while WorkList  $\neq \emptyset$  do Select and remove an edge  $\langle s_p, d_1 \rangle \rightarrow \langle n, d_2 \rangle$  from WorkList [11] [12] switch n [13] case  $n \in Call_p$ : for each  $d_3$  such that  $\langle n, d_2 \rangle \rightarrow \langle s_{calledProc(n)}, d_3 \rangle \in E^{\#}$  do Propagate( $\langle s_{calledProc(n)}, d_3 \rangle \rightarrow \langle s_{calledProc(n)}, d_3 \rangle$ ) [14] [15] [16] od for each  $d_3$  such that  $\langle n, d_2 \rangle \rightarrow \langle returnSite(n), d_3 \rangle \in (E^{\#} \cup \text{SummaryEdge})$  do [17] Propagate( $\langle s_n, d_1 \rangle \rightarrow \langle returnSite(n), d_3 \rangle$ ) [18] [19] od [20] end case [21] case  $n = e_n$ : [22] for each  $c \in callers(p)$  do 23 for each  $d_4$ ,  $d_5$  such that  $\langle c, d_4 \rangle \rightarrow \langle s_p, d_1 \rangle \in E^{\#}$  and  $\langle e_p, d_2 \rangle \rightarrow \langle returnSite(c), d_5 \rangle \in E^{\#}$  do if  $\langle c, d_4 \rangle \rightarrow \langle returnSite(c), d_5 \rangle \notin$  SummaryEdge then 24 25 Insert  $\langle c, d_4 \rangle \rightarrow \langle returnSite(c), d_5 \rangle$  into SummaryEdge for each  $d_3$  such that  $\langle s_{procOf(c)}, d_3 \rangle \rightarrow \langle c, d_4 \rangle \in \text{PathEdge do}$ Propagate( $\langle s_{procOf(c)}, d_3 \rangle \rightarrow \langle returnSite(c), d_5 \rangle$ ) [26] 27 [28] [29] od fi ľ30j od [31] od [32] end case [33] **case**  $n \in (N_p - Call_p - \{e_p\})$ : ້[34] for each  $\langle m, d_3 \rangle$  such that  $\langle n, d_2 \rangle \rightarrow \langle m, d_3 \rangle \in E^{\#}$  do Propagate  $(\langle s_v, d_1 \rangle \rightarrow \langle m, d_3 \rangle)$ [35] [36] od [37] end case [38] end switch Yue Li @ Nanjing University Ī391 od end

#### $O(ED^3)$

declare PathEdge, WorkList, SummaryEdge: global edge set **algorithm** Tabulate( $G_{IP}^{\#}$ ) begin Let  $(N^{\#}, E^{\#}) = G_{IP}^{\#}$ PathEdge := { $\langle s_{main}, \mathbf{0} \rangle \rightarrow \langle s_{main}, \mathbf{0} \rangle$ } WorkList := { $\langle s_{main}, \mathbf{0} \rangle \rightarrow \langle s_{main}, \mathbf{0} \rangle$ } SummaryEdge :=  $\emptyset$ [3] [4] [5] [6] ForwardTabulateSLRPs() for each  $n \in N^*$  do ז ז  $X_n := \{ d_2 \in D \mid \exists d_1 \in (D \cup \{0\}) \text{ such that } \langle s_{procOf(n)}, d_1 \rangle \rightarrow \langle n, d_2 \rangle \in \text{PathEdge} \}$ 81 od end procedure Propagate(e) begin if  $e \notin$  PathEdge then Insert e into PathEdge; Insert e into WorkList fi [9] end procedure ForwardTabulateSLRPs() begin [10] while WorkList  $\neq \emptyset$  do Select and remove an edge  $\langle s_p, d_1 \rangle \rightarrow \langle n, d_2 \rangle$  from WorkList [11] [12] switch n [13] case  $n \in Call_p$ : for each  $d_3$  such that  $\langle n, d_2 \rangle \rightarrow \langle s_{calledProc(n)}, d_3 \rangle \in E^{\#}$  do Propagate( $\langle s_{calledProc(n)}, d_3 \rangle \rightarrow \langle s_{calledProc(n)}, d_3 \rangle$ ) [14] [15] [16] od for each  $d_3$  such that  $\langle n, d_2 \rangle \rightarrow \langle returnSite(n), d_3 \rangle \in (E^{\#} \cup \text{SummaryEdge})$  do [17] Propagate( $\langle s_n, d_1 \rangle \rightarrow \langle returnSite(n), d_3 \rangle$ ) [18] [19] od [20] end case [21] case  $n = e_n$ : ľ22] for each  $c \in callers(p)$  do for each  $d_4$ ,  $d_5$  such that  $\langle c, d_4 \rangle \rightarrow \langle s_p, d_1 \rangle \in E^{\#}$  and  $\langle e_p, d_2 \rangle \rightarrow \langle returnSite(c), d_5 \rangle \in E^{\#}$  do if  $\langle c, d_4 \rangle \rightarrow \langle returnSite(c), d_5 \rangle \notin$  SummaryEdge then 23 24 25 Insert  $\langle c, d_4 \rangle \rightarrow \langle returnSite(c), d_5 \rangle$  into SummaryEdge for each  $d_3$  such that  $\langle s_{procOf(c)}, d_3 \rangle \rightarrow \langle c, d_4 \rangle \in \text{PathEdge do}$ Propagate( $\langle s_{procOf(c)}, d_3 \rangle \rightarrow \langle returnSite(c), d_5 \rangle$ ) [26] 27 28 od 29 fi ľ30j od [31] od [32] end case [33] **case**  $n \in (N_p - Call_p - \{e_p\})$ : for each  $\langle m, d_3 \rangle$  such that  $\langle n, d_2 \rangle \rightarrow \langle m, d_3 \rangle \in E^{\#}$  do [34] Propagate  $(\langle s_n, d_1 \rangle \rightarrow \langle m, d_3 \rangle)$ [35] [36] od [37] end case [38] end switch Yue Li @ Nanjing University Ī391 od end

#### $O(ED^3)$

# No time to cover the whole algorithm

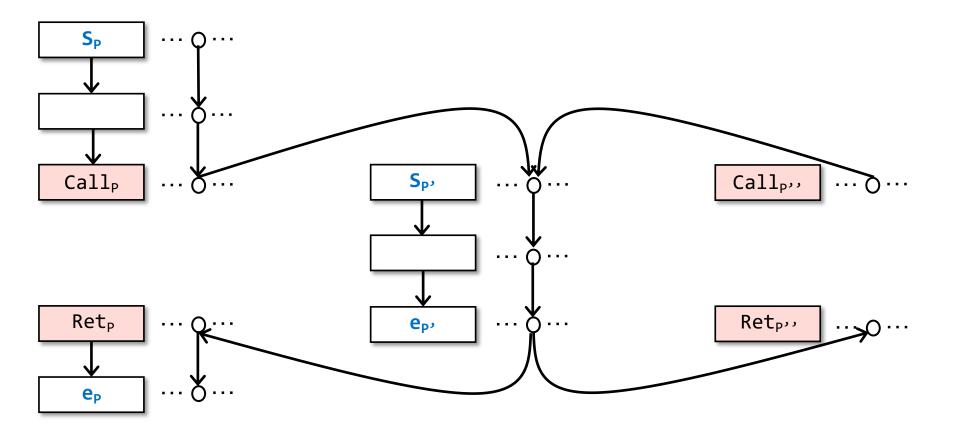
declare PathEdge, WorkList, SummaryEdge: global edge set **algorithm** Tabulate( $G_{IP}^{\#}$ ) begin  $Let (N^{\#}, E^{\#}) = G_{IP}^{\#}$ PathEdge := { $\langle s_{main}, \mathbf{0} \rangle \rightarrow \langle s_{main}, \mathbf{0} \rangle$ } WorkList := { $\langle s_{main}, \mathbf{0} \rangle \rightarrow \langle s_{main}, \mathbf{0} \rangle$ } SummaryEdge :=  $\emptyset$ [3] [4] [5] [6] ForwardTabulateSLRPs() for each  $n \in N^*$  do ז ז  $X_n := \{ d_2 \in D \mid \exists d_1 \in (D \cup \{\mathbf{0}\}) \text{ such that } \langle s_{procOf(n)}, d_1 \rangle \rightarrow \langle n, d_2 \rangle \in \text{PathEdge} \}$ 81 od end procedure Propagate(e) begin if  $e \notin$  PathEdge then Insert e into PathEdge; Insert e into WorkList fi [9] end procedure ForwardTabulateSLRPs() begin [10] while WorkList  $\neq \emptyset$  do Select and remove an edge  $\langle s_v, d_1 \rangle \rightarrow \langle n, d_2 \rangle$  from WorkList [11] [12] switch n [13] case  $n \in Call_p$ : for each  $d_3$  such that  $\langle n, d_2 \rangle \rightarrow \langle s_{calledProc(n)}, d_3 \rangle \in E^{\#}$  do Propagate( $\langle s_{calledProc(n)}, d_3 \rangle \rightarrow \langle s_{calledProc(n)}, d_3 \rangle$ ) [14] [15] [16] od for each  $d_3$  such that  $\langle n, d_2 \rangle \rightarrow \langle returnSite(n), d_3 \rangle \in (E^{\#} \cup \text{SummaryEdge})$  do [17] Propagate( $\langle s_n, d_1 \rangle \rightarrow \langle returnSite(n), d_3 \rangle$ ) [18] [19] od [20] end case [21] case  $n = e_n$ : [22] for each  $c \in callers(p)$  do 23 for each  $d_4$ ,  $d_5$  such that  $\langle c, d_4 \rangle \rightarrow \langle s_p, d_1 \rangle \in E^{\#}$  and  $\langle e_p, d_2 \rangle \rightarrow \langle returnSite(c), d_5 \rangle \in E^{\#}$  do if  $\langle c, d_4 \rangle \rightarrow \langle returnSite(c), d_5 \rangle \notin$  SummaryEdge then 24 25 Insert  $\langle c, d_4 \rangle \rightarrow \langle returnSite(c), d_5 \rangle$  into SummaryEdge for each  $d_3$  such that  $\langle s_{procOf(c)}, d_3 \rangle \rightarrow \langle c, d_4 \rangle \in \text{PathEdge do}$ Propagate( $\langle s_{procOf(c)}, d_3 \rangle \rightarrow \langle returnSite(c), d_5 \rangle$ ) [26] [27 28 od 29 fi Ī30Ī od [31] od [32] end case [33] **case**  $n \in (N_p - Call_p - \{e_p\})$ : for each  $\langle m, d_3 \rangle$  such that  $\langle n, d_2 \rangle \rightarrow \langle m, d_3 \rangle \in E^{\#}$  do [34] Propagate  $(\langle s_v, d_1 \rangle \rightarrow \langle m, d_3 \rangle)$ [35] [36] od Ī37Ī end case [38] end switch Yue Li @ Nanjing University Ī391 od end

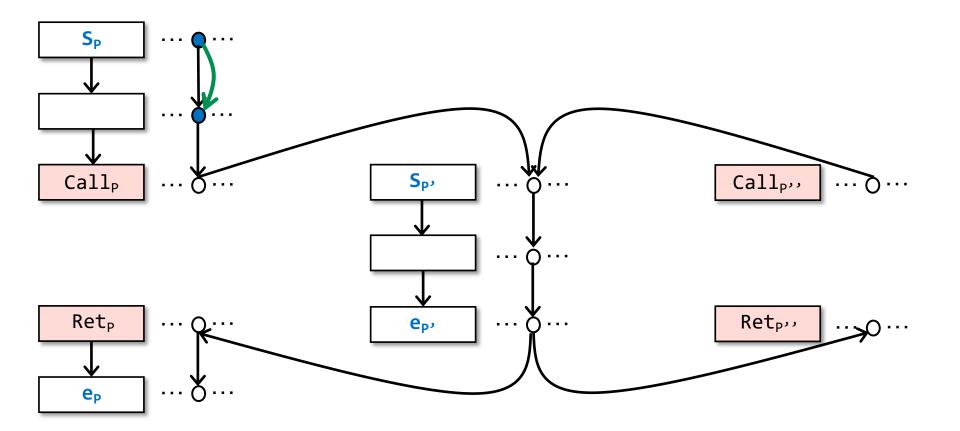
#### $O(ED^3)$

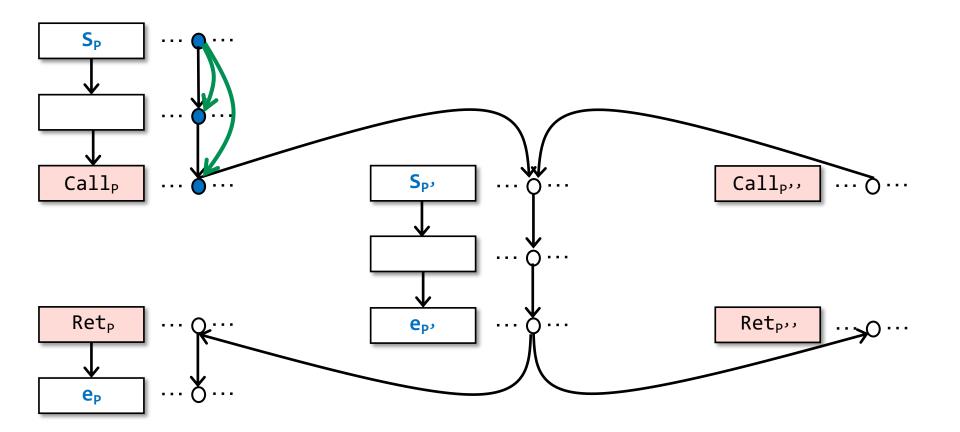
No time to cover the whole algorithm

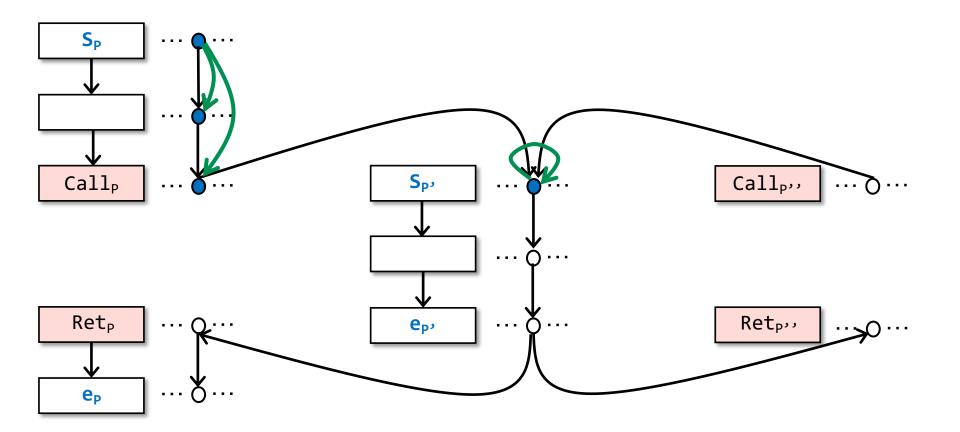
But we will introduce its core working mechanism by a simple example

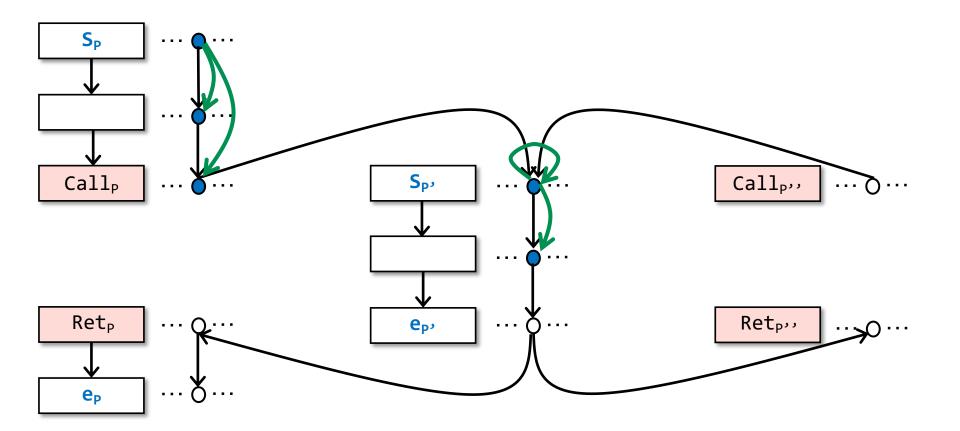
### Core Working Mechanism of Tabulation Algorithm

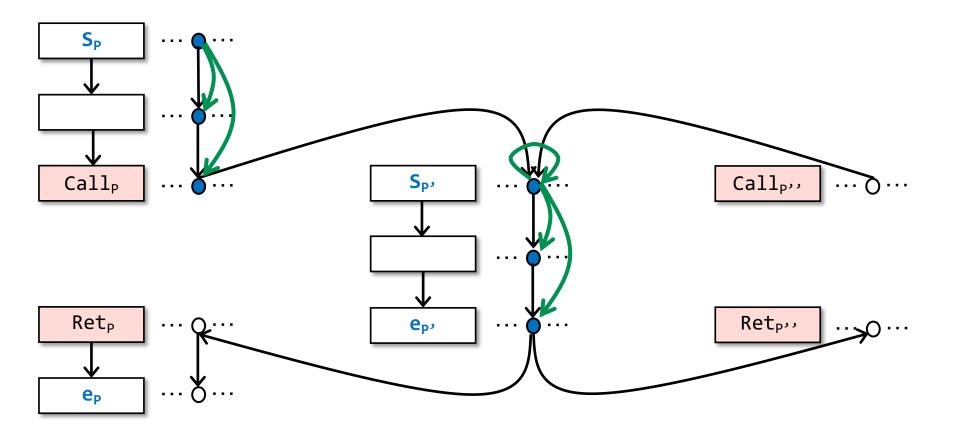


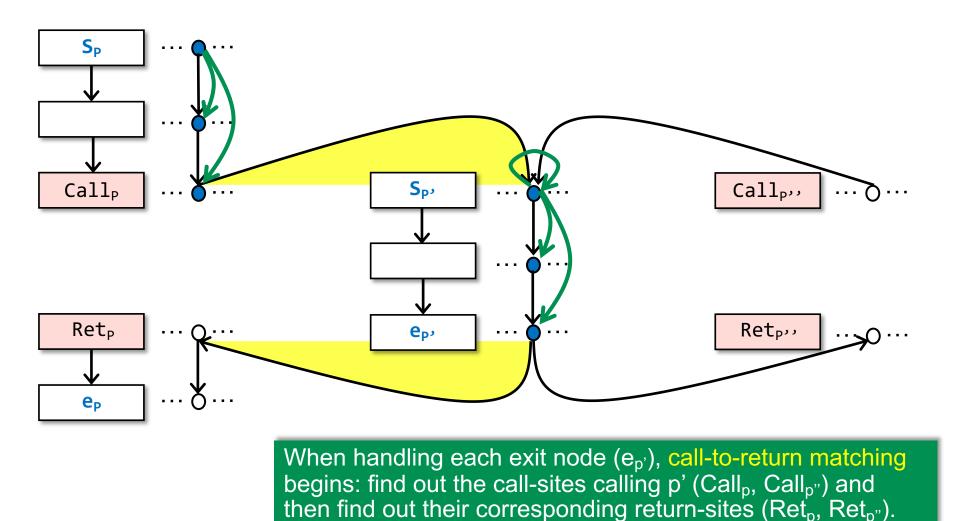












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**S**<sub>₽</sub>,

•e

Sp

Call<sub>P</sub>

Ret<sub>₽</sub>

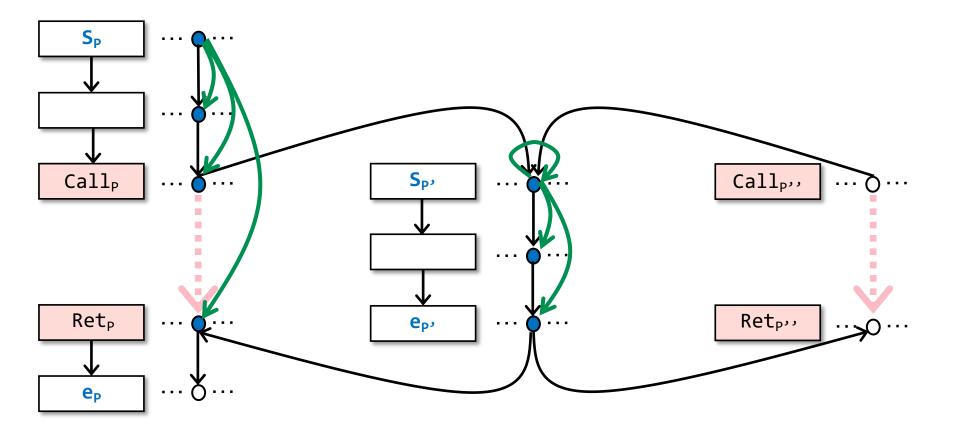
**e**<sub>P</sub>

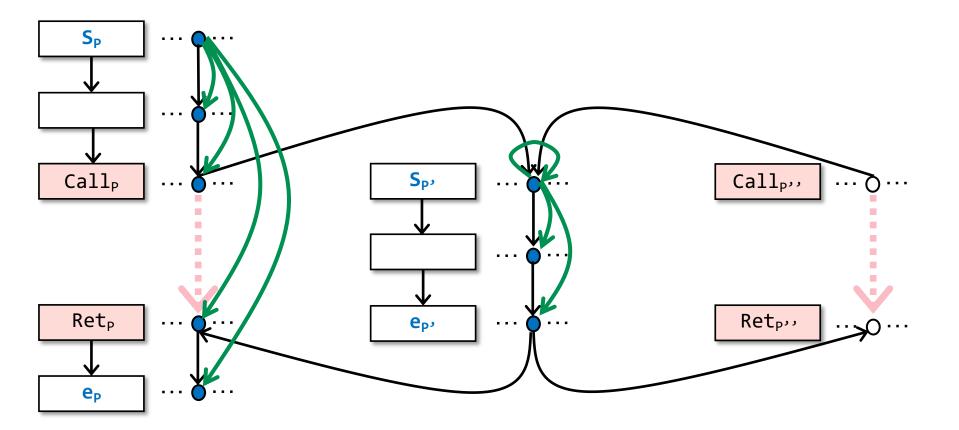
Actually, here **a summary edge** from  $<Call,d_m > to <Ret,d_n >$  is added to indicate that  $d_n$  is **reachable** from  $d_m$  through the called method p'. At the moment, some methods (like p'') may not be handled yet, so when handling p'' later, redundant work could be avoided for **such reachable path**.

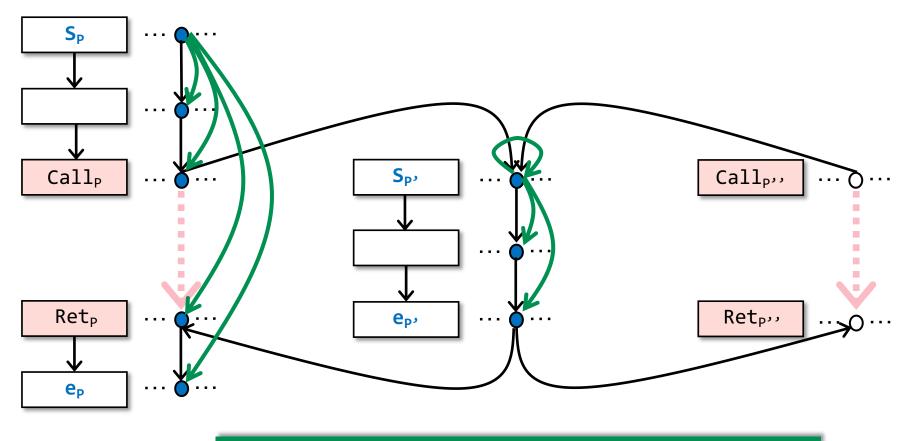
Call<sub>p</sub>,,

Ret<sub>P</sub>,,

When handling each exit node  $(e_{p'})$ , call-to-return matching begins: find out the call-sites calling p'  $(Call_p, Call_{p''})$  and then find out their corresponding return-sites  $(Ret_p, Ret_{p''})$ .







When a data fact (at node n) d's circle is turned to blue, it means that <n, d> is reachable from  $<S_{main}$ , 0>

• Can we do constant propagation using IFDS?

Constant propagation has infinite domain, but what if we only deal with finite constant values? Can we still do it using IFDS?

• Can we do pointer analysis using IFDS?

Can we do constant propagation using IFDS?

Constant propagation has infinite domain, but what if we only deal with finite constant values? Can we still do it using IFDS?

Can we do pointer analysis using IFDS?



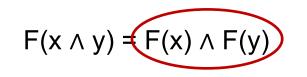
Distributivity
 Constant Propagation

 $F(x \land y) = F(x) \land F(y)$ 

$$\begin{bmatrix} z = x + y \end{bmatrix} \begin{bmatrix} x & y & z \\ 0 & 0 \end{bmatrix} \begin{bmatrix} z = x + y \end{bmatrix}$$

z's value depends on both y's and x's

• Distributivity



Each flow function in IFDS handles one input data fact per time

z's value depends on both y's and x's

٠	Distributivity	Ea	ach flow functio one input data				
	$F(x \land y) = F(x) \land F(y)$		z = x + y	X O	y O	Z O	
		"if x e But w	n representation exists, then …", hen we need "it o draw the repr	"if y exi f both x	sts th and y	nen …" / exist"	, ,

<ul> <li>Distributivity</li> </ul>		ch flow functio one input data			
For constant propagation, we cannot d F if we only know x's (or y's) value		z = x + y	X O	у О	z O
، B	if x ex ut wh	representation ists, then", en we need "if draw the repr	"if y ex both x	ists th and y	nen …" / exist",

<ul> <li>Distributivity</li> </ul>			Each flow function in IFDS handles one input data fact per time				
	nstant propagation, we cannot o if we only know x's (or y's) value		z = x + y	x O	y O	Z O	
		"if x ex But whe	representatior ists, then …", en we need "if draw the repre	"if y exi f both x	ists th and y	nen …" y exist",	
	Given a statement S, besiden <b>multiple</b> input data facts to analysis is not distributive a	create	e correct out	<mark>puts</mark> , th	nen tl	he	
	In IFDS, each data fact (cir	,	· · · ·	•	•	,	

be handled independently, and doing so will not affect the correctness of the final results.

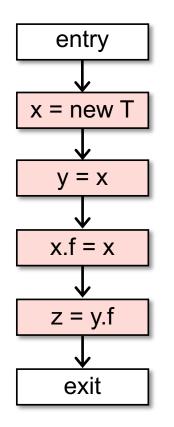
Distributivity	Each flow function in IFDS handles one input data fact per time
For constant propagation, we cannot de F if we only know x's (or y's) value	finexyz $z = x + y$ OO
"imple rule to determine analysis could Bu	Each representation relation indicates f x exists, then", "if y exists then" at when we need "if both x and y exist", ow to draw the representation relation?
Given a statement S, besides multiple input data facts to c analysis is not distributive an In IFDS, each data fact (circl	s S itself, if we need to consider reate correct outputs, then the d should not be expressed in IFDS. e) and its propagation (edges) could and doing so will not affect the s.

Distributivity	Each flow function in IFDS handles one input data fact per time		
For constant propagation, we cannot de F if we only know x's (or y's) value	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		
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	e) and its propagation (edges) could and doing so will not affect the ts.		
Regardless of the infinite domain issue think about whether we could do			

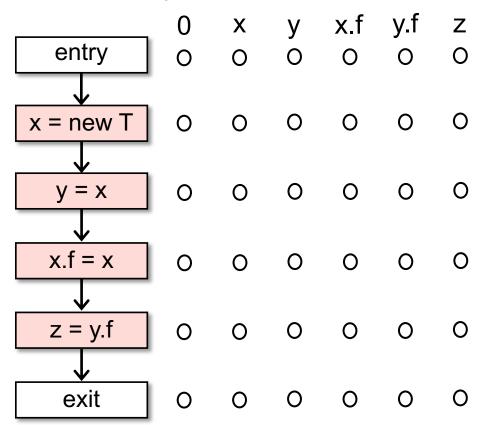
Regardless of the infinite domain issue, think about whether we could do *linear constant propagation*, e,g., y = 2x + 3, or *copy constant propagation*, e.g., x = 2, y = x, using IFDS-style analysis?

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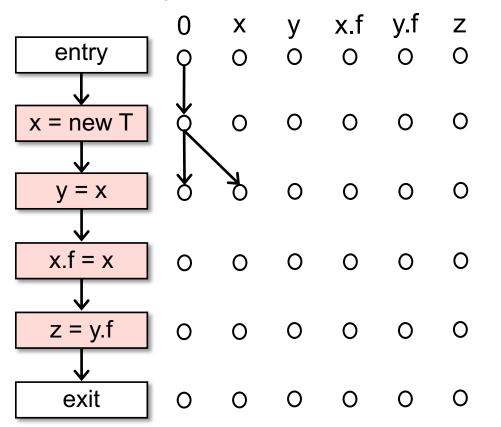
• Pointer Analysis



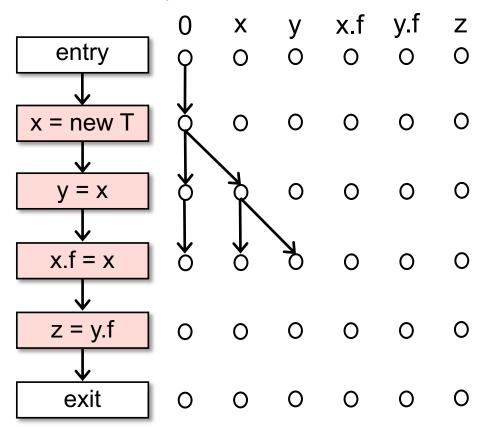
• Pointer Analysis



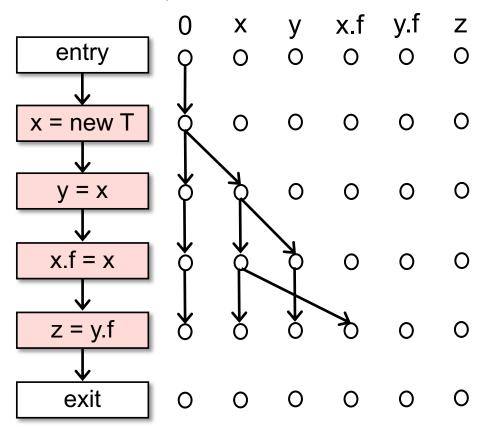
• Pointer Analysis



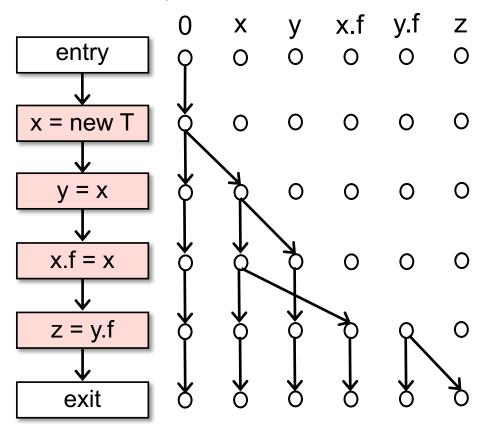
• Pointer Analysis



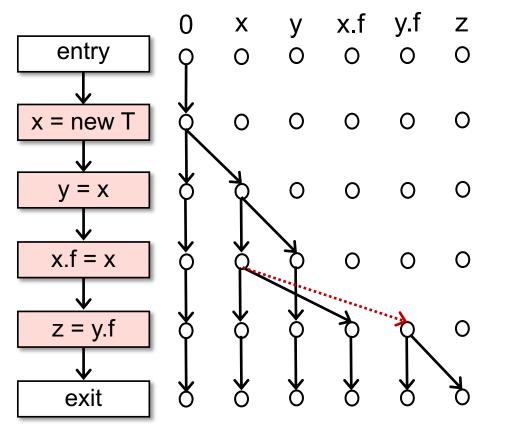
• Pointer Analysis



• Pointer Analysis



• Pointer Analysis



For simplicity, assume we know the program only contains these four statements when designing flow functions

z and y.f should have pointed to object [new T]. However, flow function's input data facts lack of the alias information, alias(x,y), alias(x.f,y.f), and we need alias information to produce correct outputs.

• Pointer Analysis

designing flow functions y x.f y.f z () Χ entry 0 Note: If we want to obtain alias information in IFDS. say alias(x,y), to produce correct outputs, we need x = new T0 to consider multiple input data facts, x and y, which cannot be done in standard IFDS as flow functions handle input facts independently (one fact per time). y = xThus pointer analysis is non-distributive. x.f = x $\cap$  $\cap$ z = y.fΟ exit

For simplicity, assume we know the program only contains these four

statements when

z and y.f should have pointed to object [new T]. However, flow function's input data facts lack of the alias information, alias(x,y), alias(x.f,y.f), and we need alias information to produce correct outputs.

Contents

- 1. Feasible and Realizable Paths
- 2. CFL-Reachability
- 3. Overview of IFDS
- 4. Supergraph and Flow Functions
- 5. Exploded Supergraph and Tabulation Algorithm
- 6. Understanding the Distributivity of IFDS

# The X You Need To Understand in This Lecture

- Understand CFL-Reachability
- Understand the basic idea of IFDS
- Understand what problems can be solved by IFDS



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软件分析