

# 软件分析

南京大学

计算机科学与技术系

程序设计语言与

静态分析研究组

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谭添

# Static Program Analysis

## Pointer Analysis

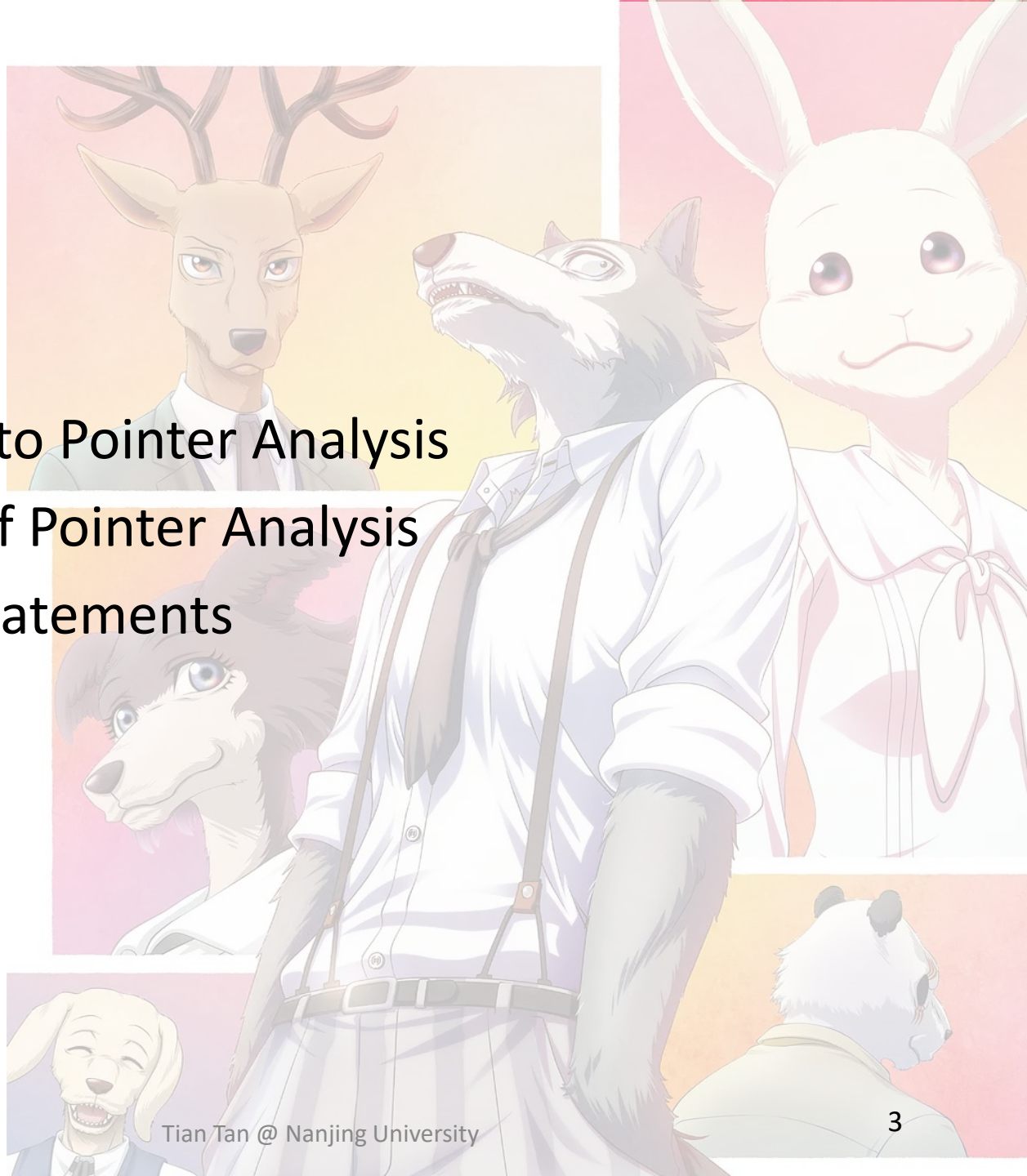
Nanjing University

Tian Tan

2021

# Contents

1. Motivation
2. Introduction to Pointer Analysis
3. Key Factors of Pointer Analysis
4. Concerned Statements



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1. **Motivation**
2. Introduction to Pointer Analysis
3. Key Factors of Pointer Analysis
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# Problem of CHA

```
void foo() {  
    Number n = new One();  
    → int x = n.get();  
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```
interface Number {  
    int get();  
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class Zero implements Number {  
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CHA:

- ? call targets

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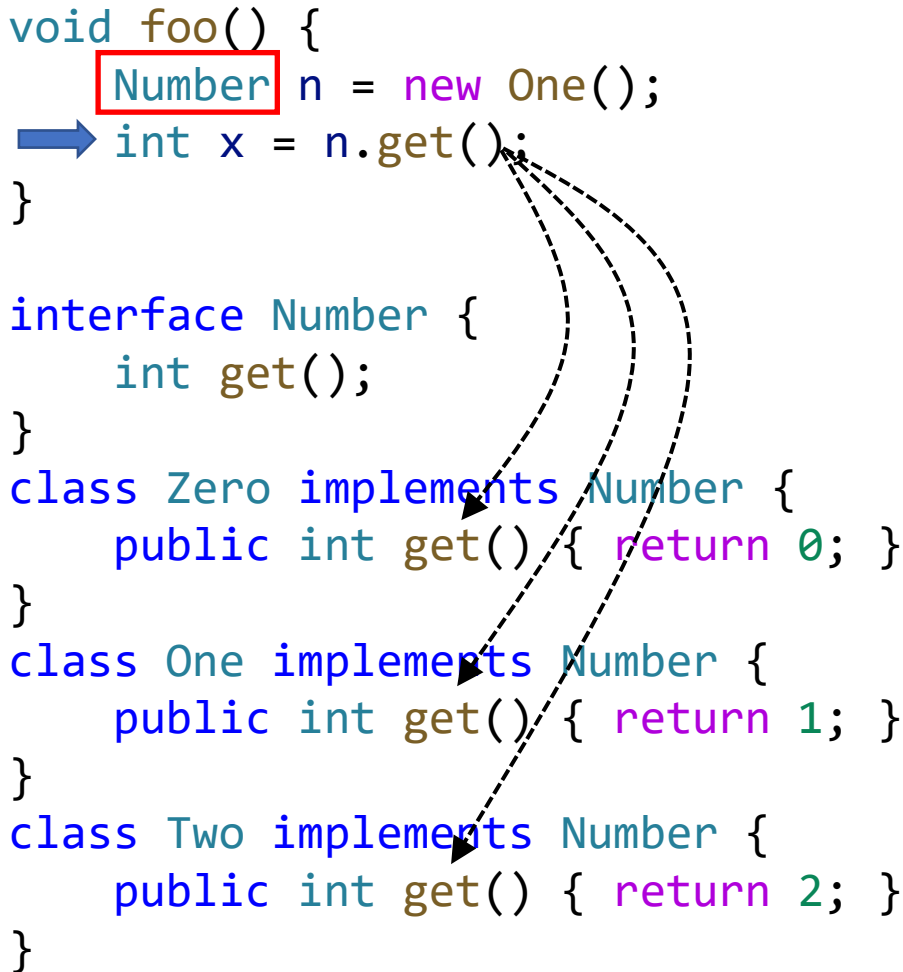
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CHA: based on  
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Constant propagation

- $x = ?$



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- $x = \text{NAC}$

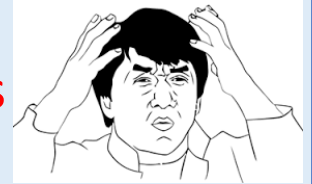
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Diagram illustrating the problem of CHA (Class Hierarchy Analysis) in the provided code. A blue arrow points to the assignment `int x = n.get();` in the `foo()` method. Three dashed red arrows originate from the `n.get()` call and point to the `get()` method in the `Number` interface, `Zero` class, and `Two` class. Two of these arrows are marked with a red 'X', indicating false positives where CHA incorrectly identifies the target class.

CHA: based on only considers **class hierarchy**

- 3 call targets
- 2 false positives



Constant propagation

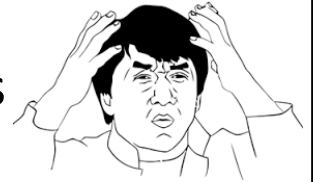
- `x = NAC` **imprecise**

# Via Pointer Analysis

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n points to new One  
  
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Pointer analysis: based on  
**points-to relation**

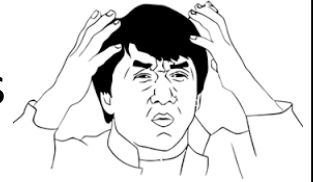
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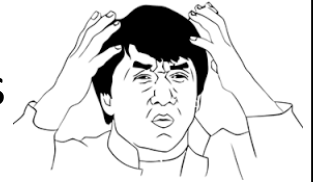
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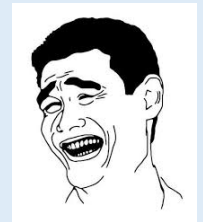


Constant propagation

- $x = \text{NAC}$  **imprecise**

Pointer analysis: based on **points-to relation**

- 1 call target
- 0 false positive

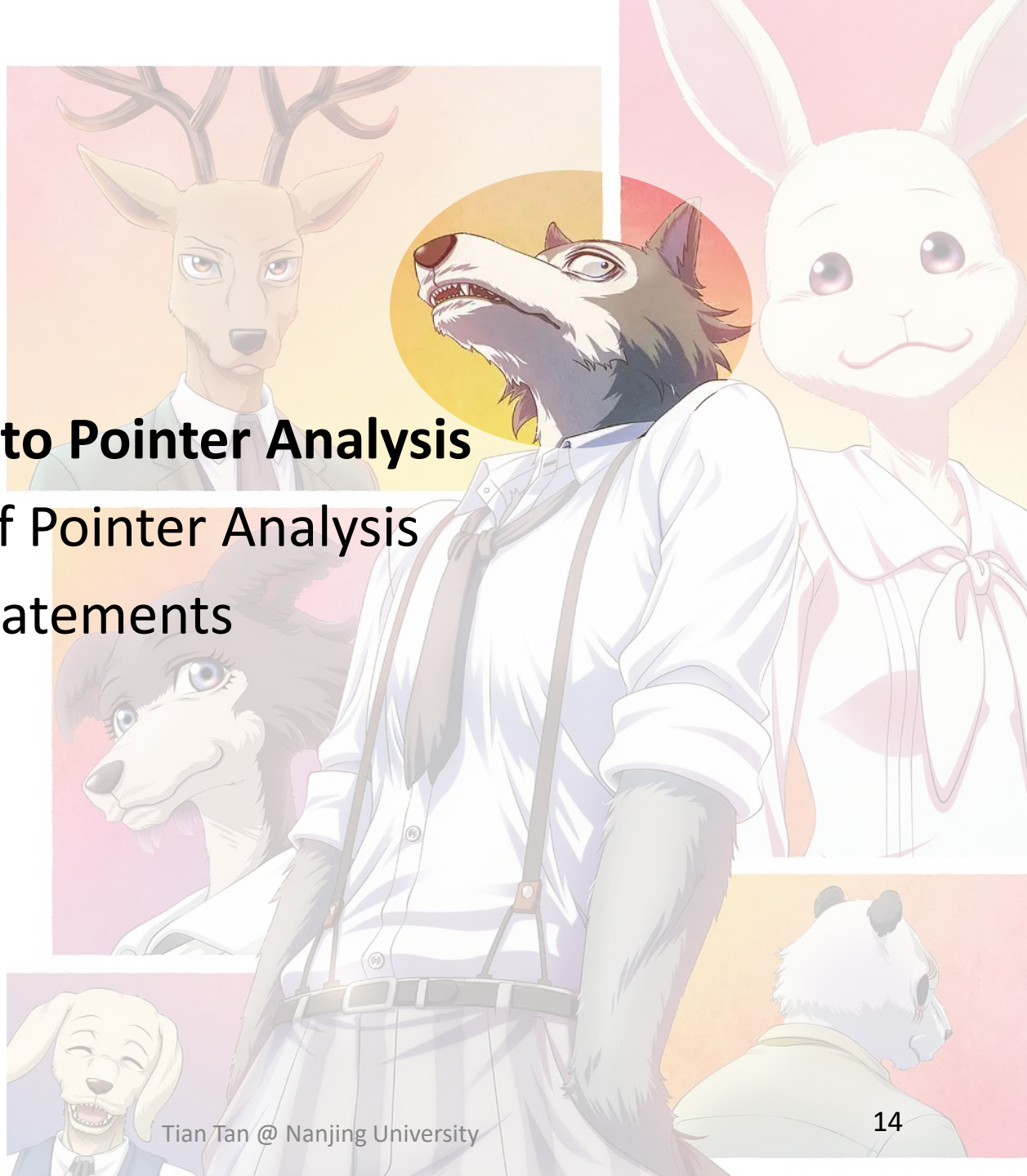


Constant propagation

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## A research area with 40+ years of history

- William E. Weihl, “*Interprocedural Data Flow Analysis in the Presence of Pointers, Procedure Variables, and Label Variables*”. POPL 1980.

## Still an active area today

- OOPSLA’18, FSE’18, TOPLAS’19, OOPSLA’19, TOPLAS’20, OOPSLA’21 ...

# Example

“Which **objects** a **pointer** can point to?”

Program

Points-to relations

```
void foo() {  
    A a = new A();  
    B x = new B();  
    a.setB(x);  
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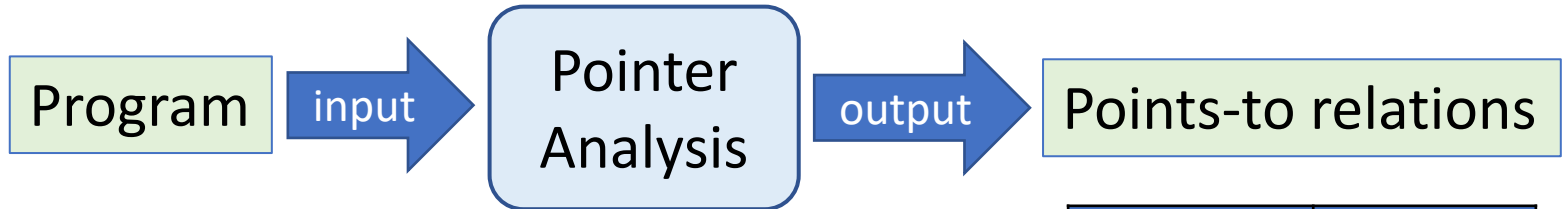
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Alias information can be derived from points-to relations

# Applications of Pointer Analysis

- Fundamental information
  - Call graph, aliases, ...
- Compiler optimization
  - Virtual call inlining, ...
- Bug detection
  - Null pointer detection, ...
- Security analysis
  - Information flow analysis,
- And many more ...

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\*Pointer Analysis - Report from Dagstuhl Seminar 13162. 2013.

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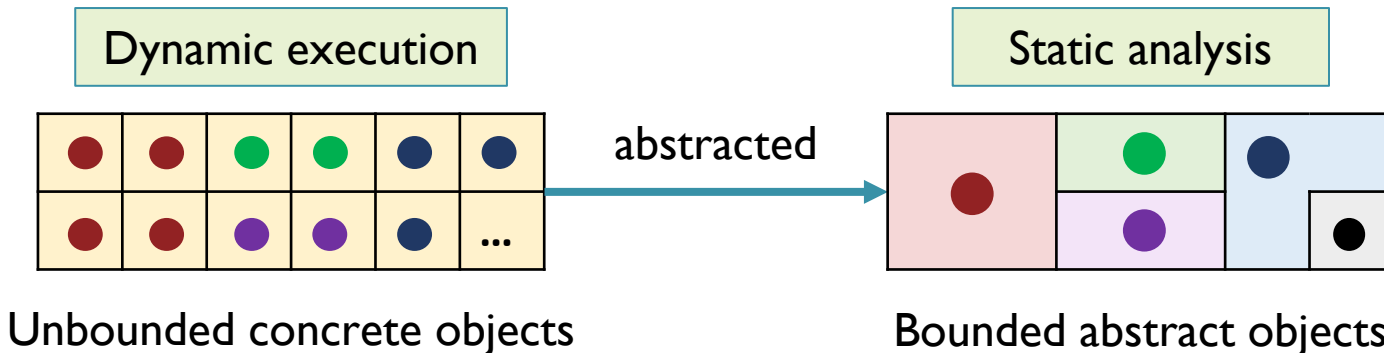
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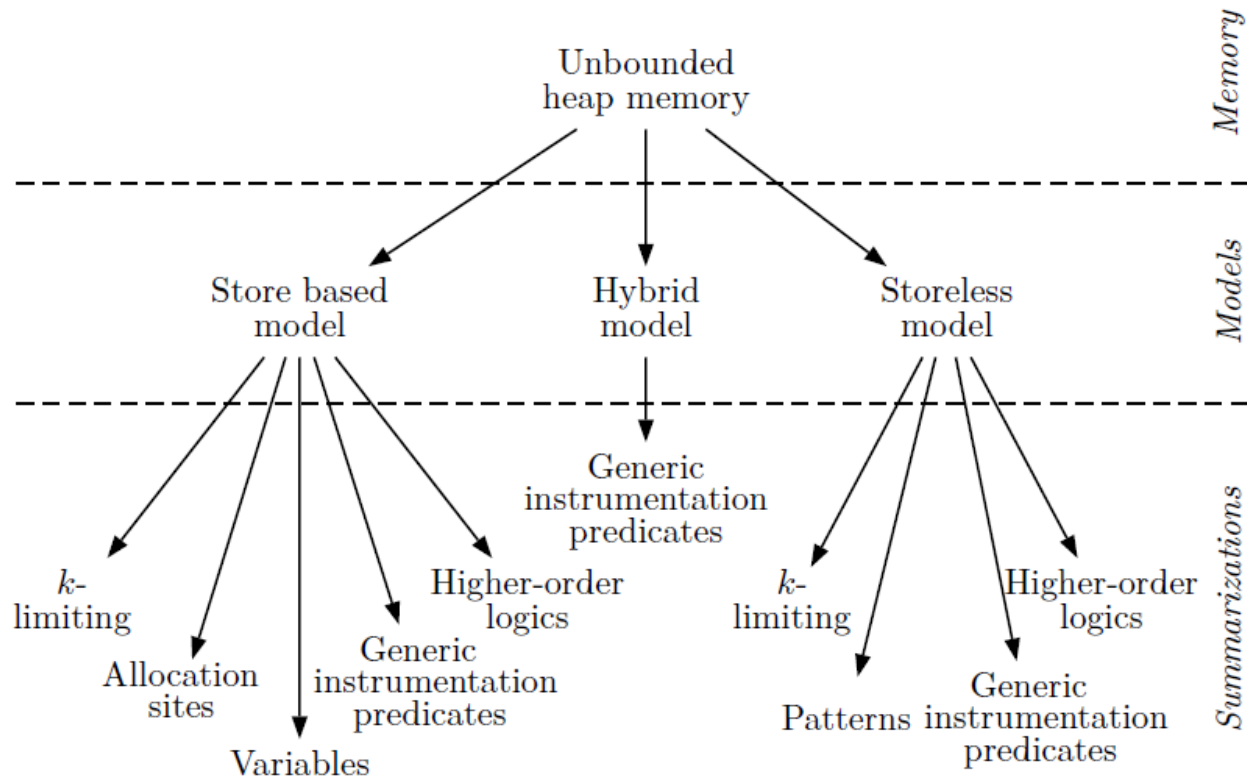
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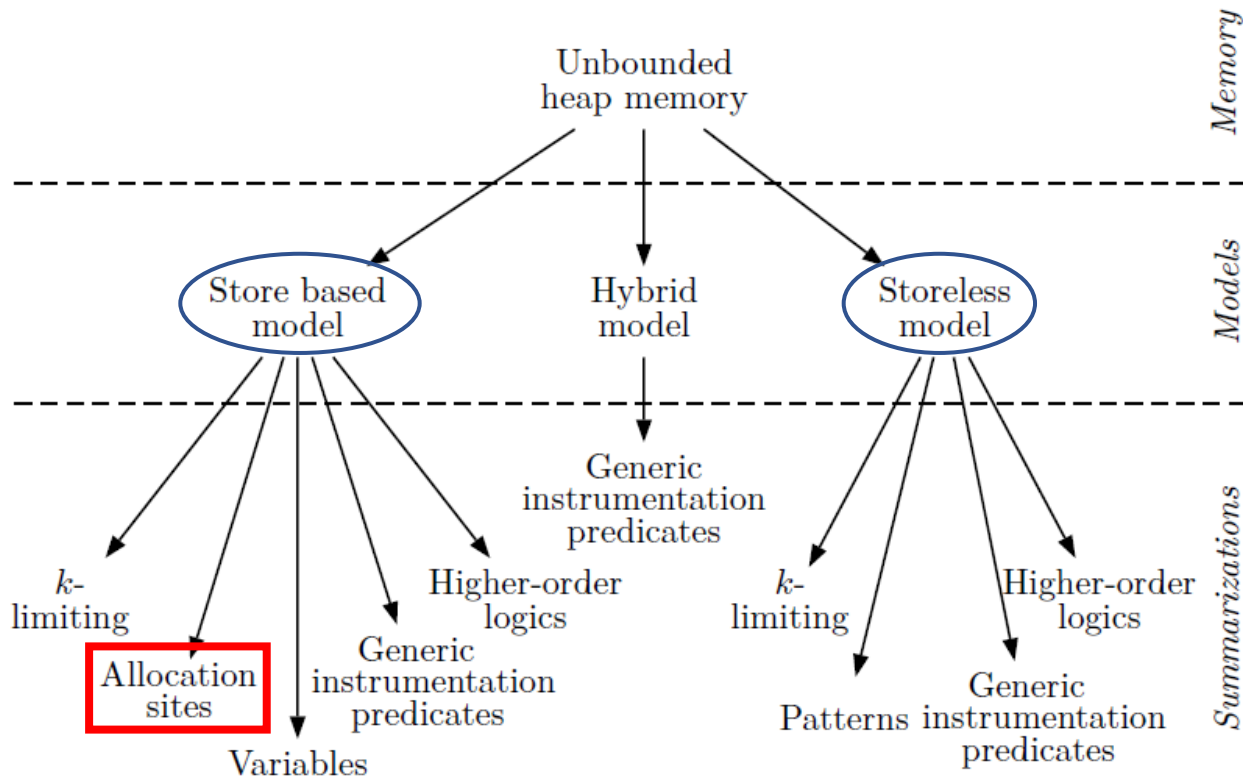


# Heap Abstraction



**Figure 2.** Heap memory can be modeled as storeless, store based, or hybrid. These models are summarized using allocation sites,  $k$ -limiting, patterns, variables, other generic instrumentation predicates, or higher-order logics.

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1 for (i = 0; i < 3; ++i) {  
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3   ...  
4 }
```

$o_2$ , iteration  $i = 0$   
 $o_2$ , iteration  $i = 1$   
 $o_2$ , iteration  $i = 2$

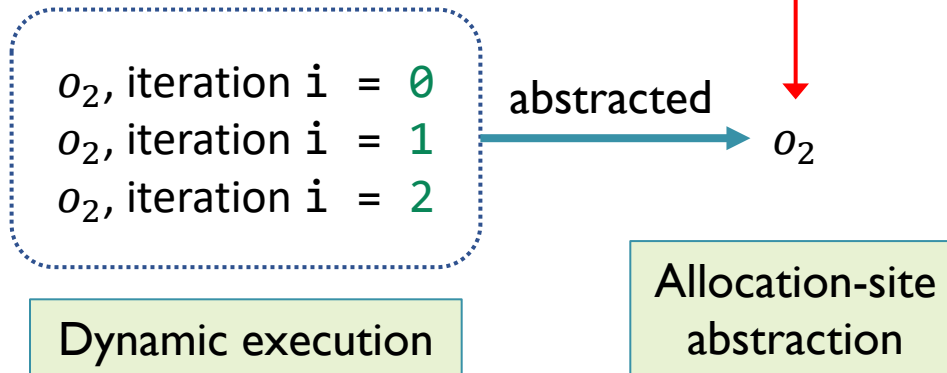
Dynamic execution

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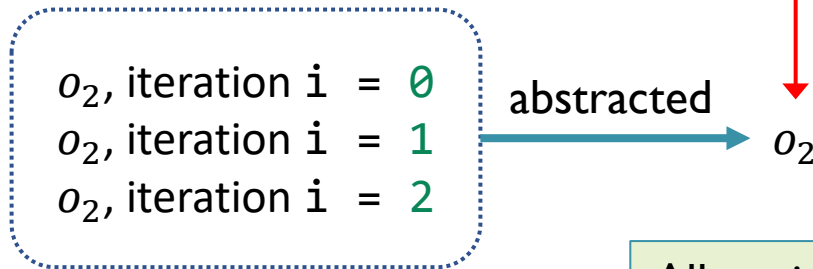


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The number of allocation sites in a program is bounded, thus the abstract objects must be finite.

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# Context Sensitivity

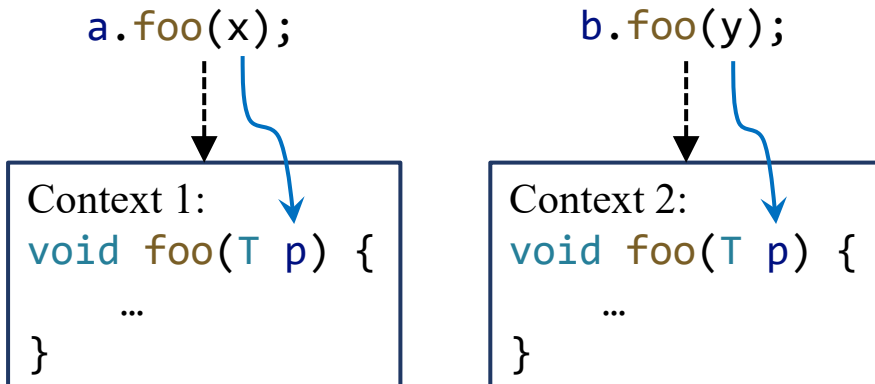
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Distinguish different calling contexts of a method	Merge all calling contexts of a method
Analyze each method multiple times, once for each context	Analyze each method once

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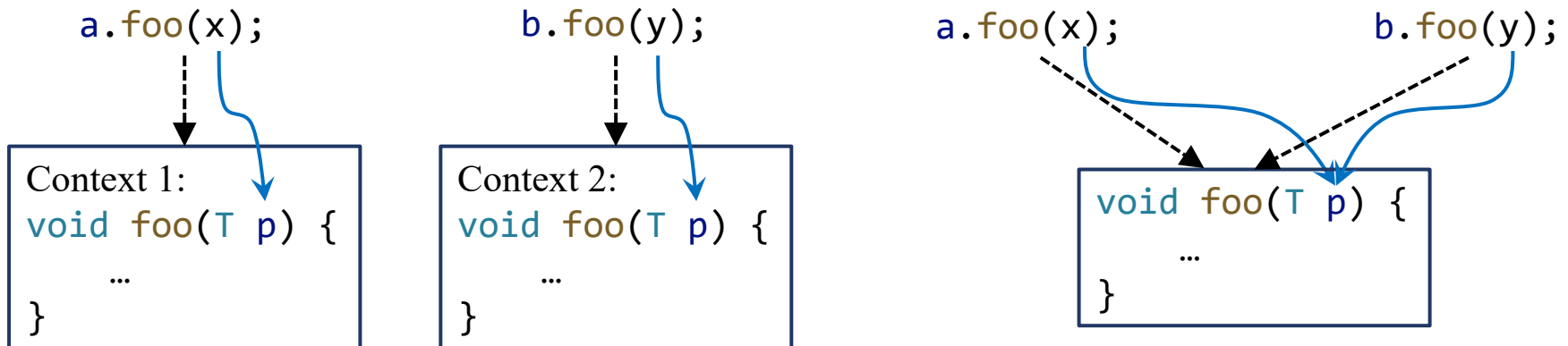
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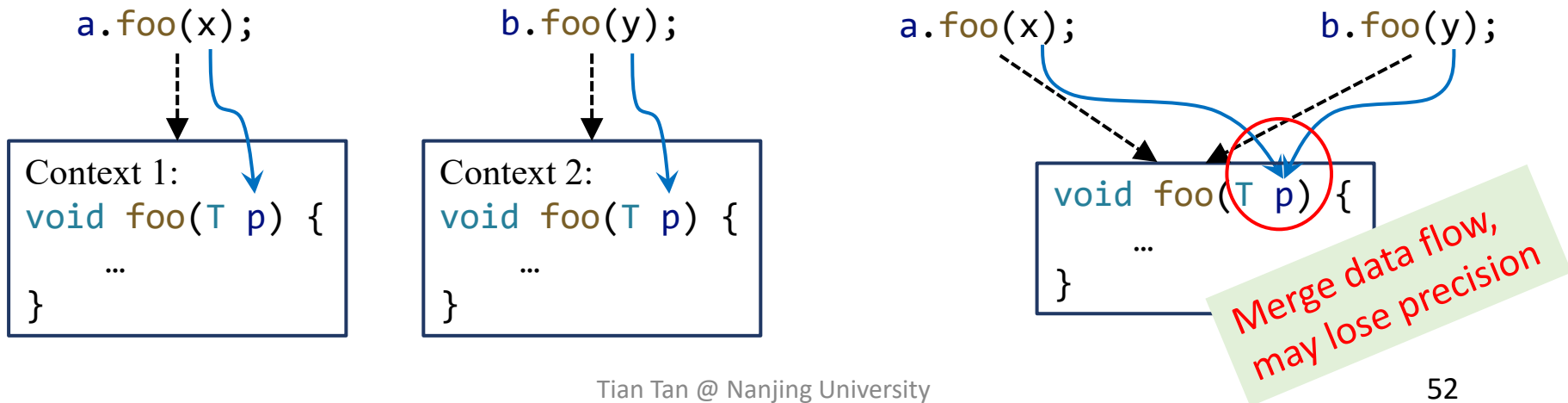
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## How to model calling contexts?

Context-sensitive	Context-insensitive
Distinguish different calling contexts of a method	<b>Merge</b> all calling contexts of a method
Analyze each method multiple times, once for each context	Analyze each method once



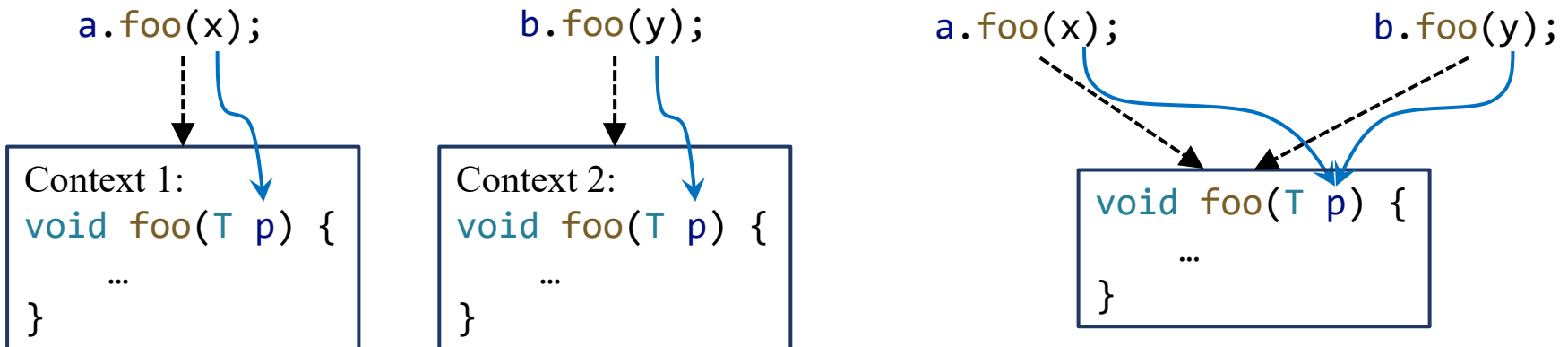
# Context Sensitivity

## How to model calling contexts?

Context-sensitive	Context-insensitive
Distinguish different calling contexts of a method	<b>Merge</b> all calling contexts of a method
Analyze each method multiple times, once for each calling context	Analyze each method once

Very useful technique  
Significantly improve precision  
More details in **later lectures**

We start with **this**



# Key Factors in Pointer Analysis

- Pointer analysis is a complex system
- Multiple factors affect the **precision** and **efficiency** of the system

Factor	Problem	Choice
Heap abstraction	How to model heap memory?	<ul style="list-style-type: none"><li>• Allocation-site</li><li>• Storeless</li></ul>
Context sensitivity	How to model calling contexts?	<ul style="list-style-type: none"><li>• Context-sensitive</li><li>• Context-insensitive</li></ul>
Flow sensitivity	How to model control flow?	<ul style="list-style-type: none"><li>• Flow-sensitive</li><li>• Flow-insensitive</li></ul>
Analysis scope	Which parts of program should be analyzed?	<ul style="list-style-type: none"><li>• Whole-program</li><li>• Demand-driven</li></ul>

# Flow Sensitivity

## How to model control flow?

Flow-sensitive	Flow-insensitive
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So far, all data-flow analyses we have learnt are **flow-sensitive**



# Flow Sensitivity

## How to model control flow?

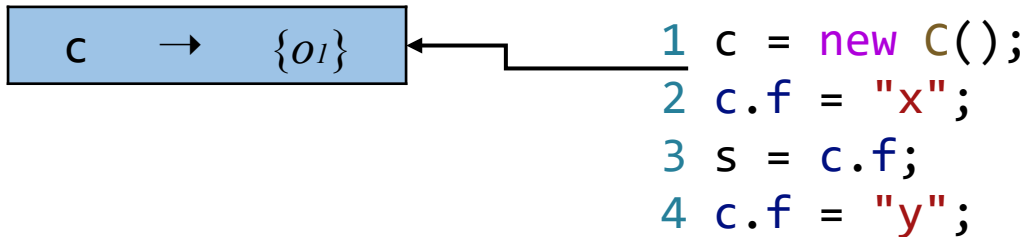
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```
1 c = new C();  
2 c.f = "x";  
3 s = c.f;  
4 c.f = "y";
```

# Flow Sensitivity

## How to model control flow?

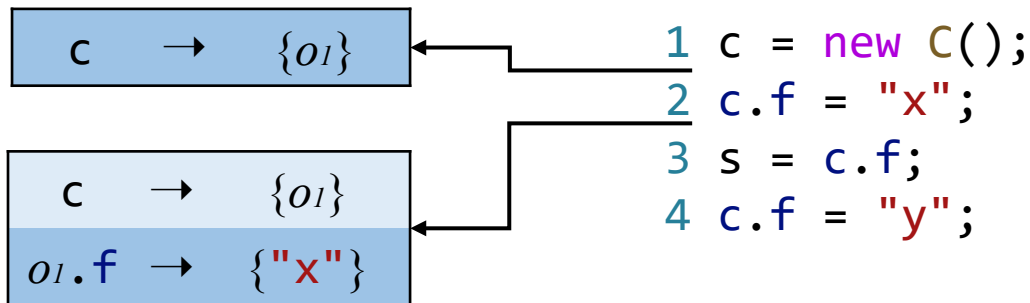
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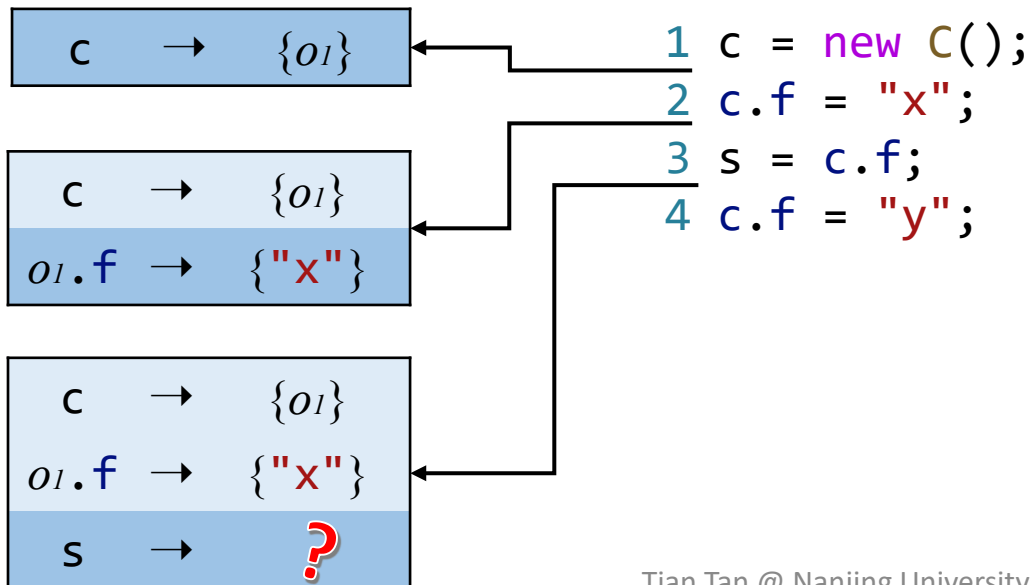
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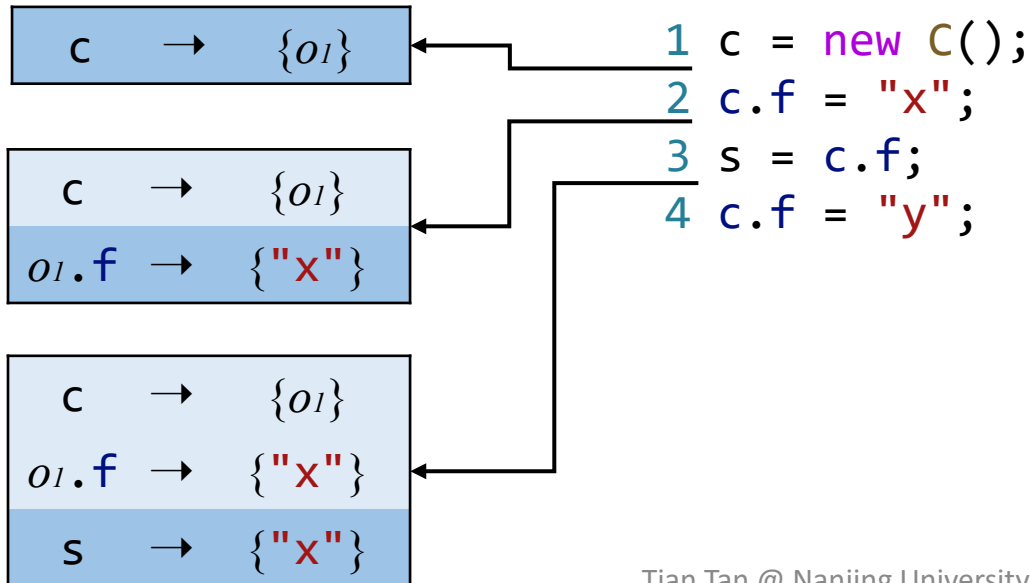
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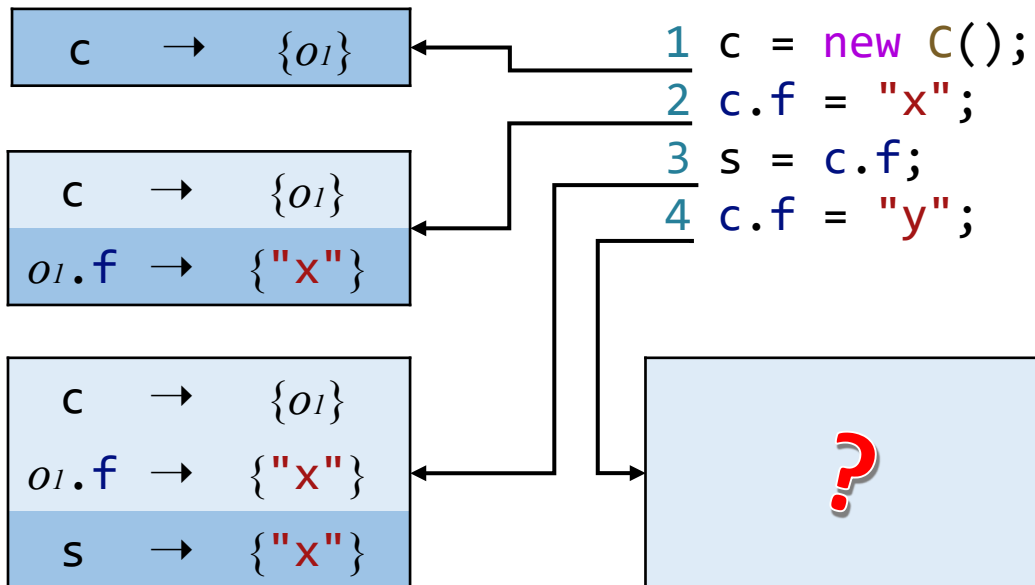
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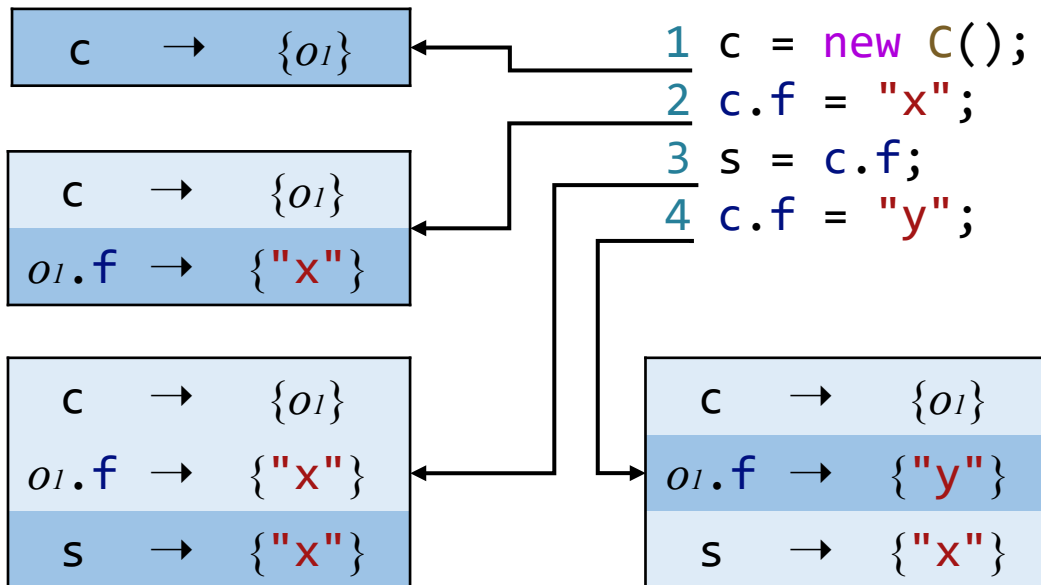
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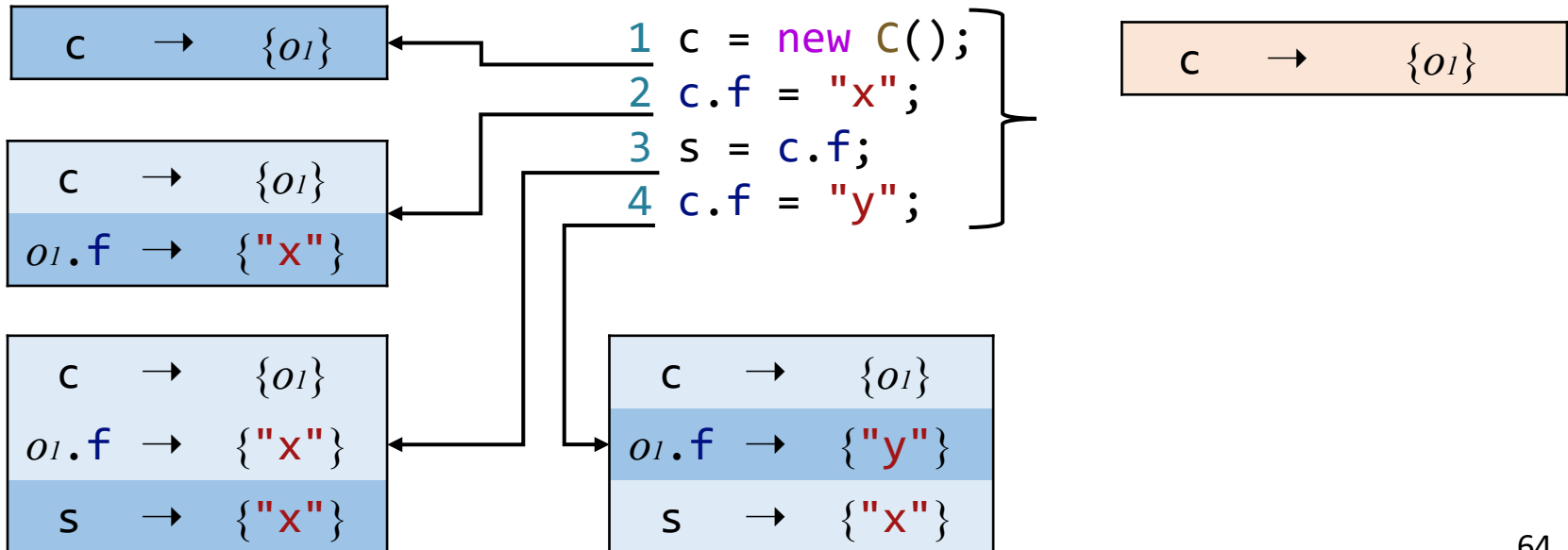
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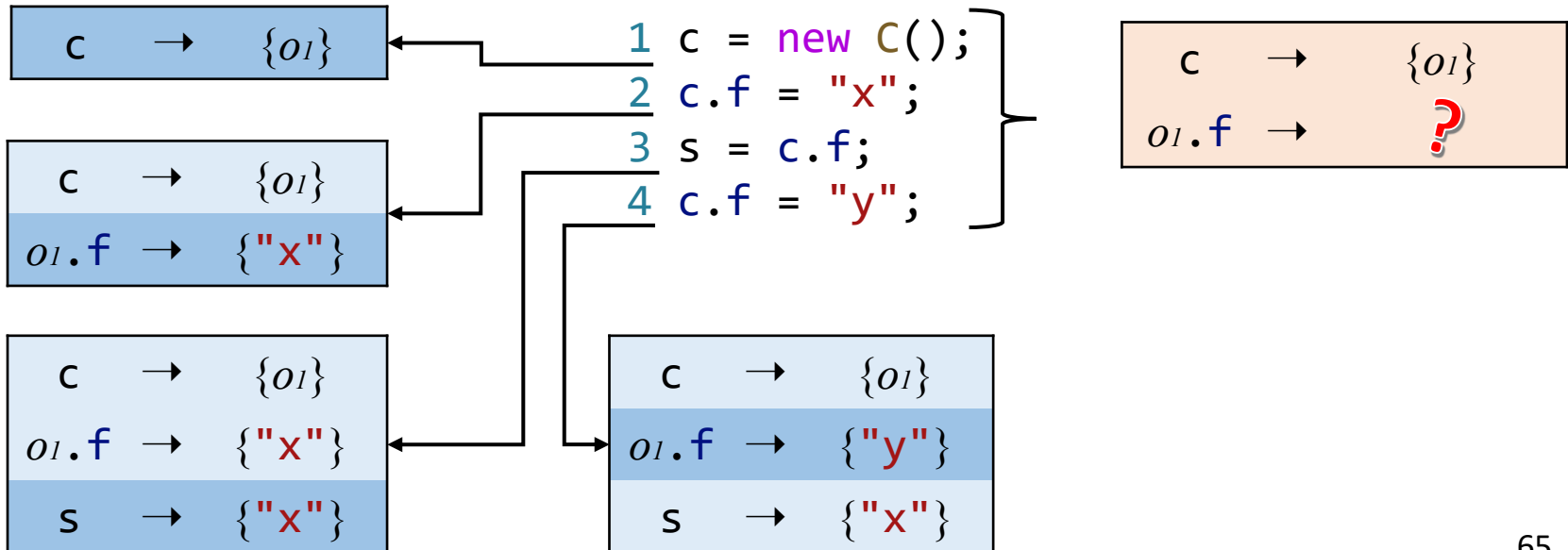




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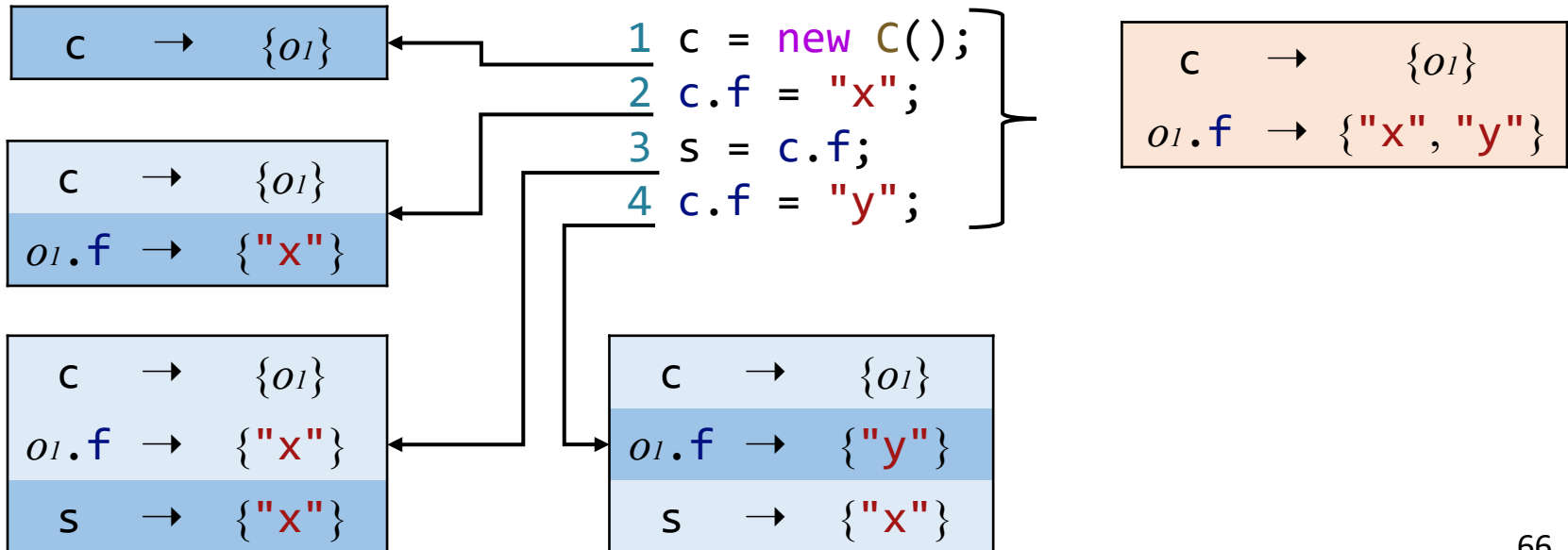
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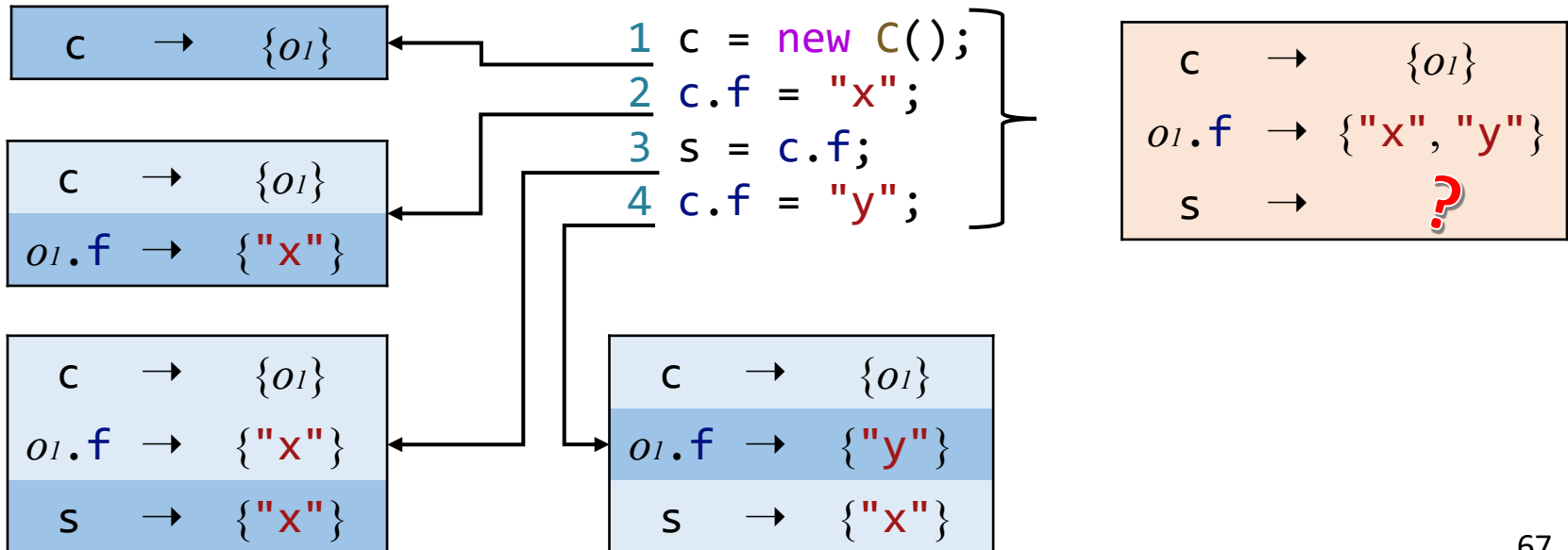
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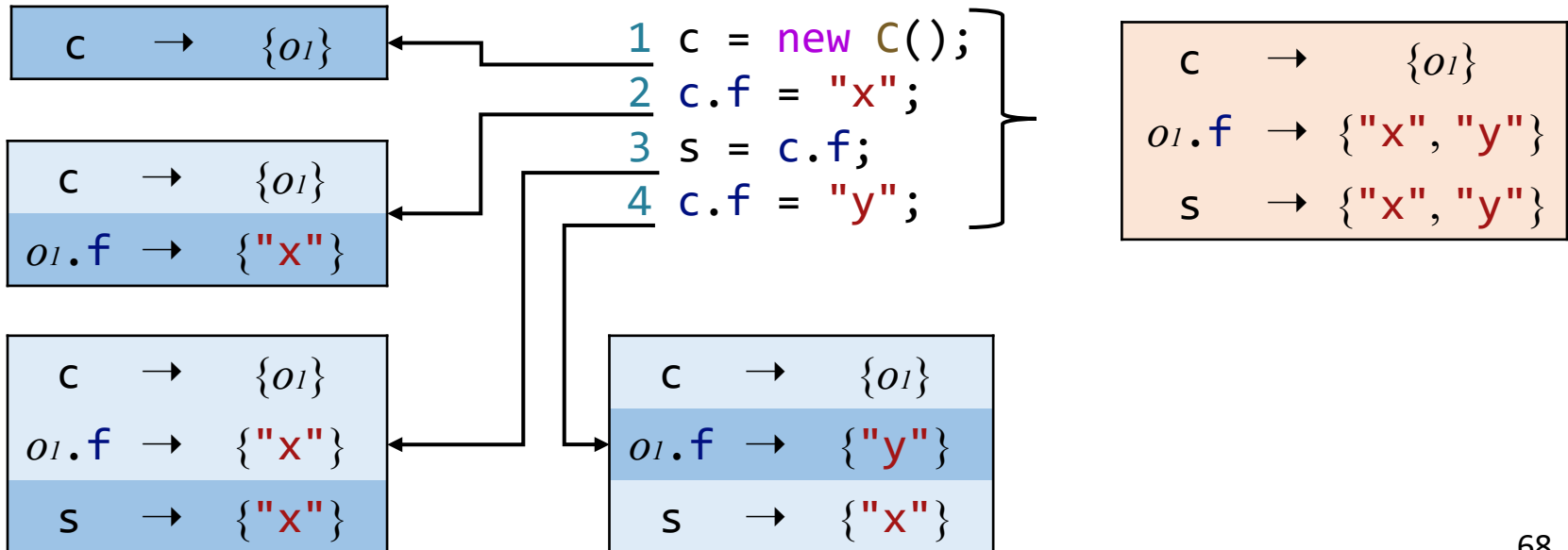
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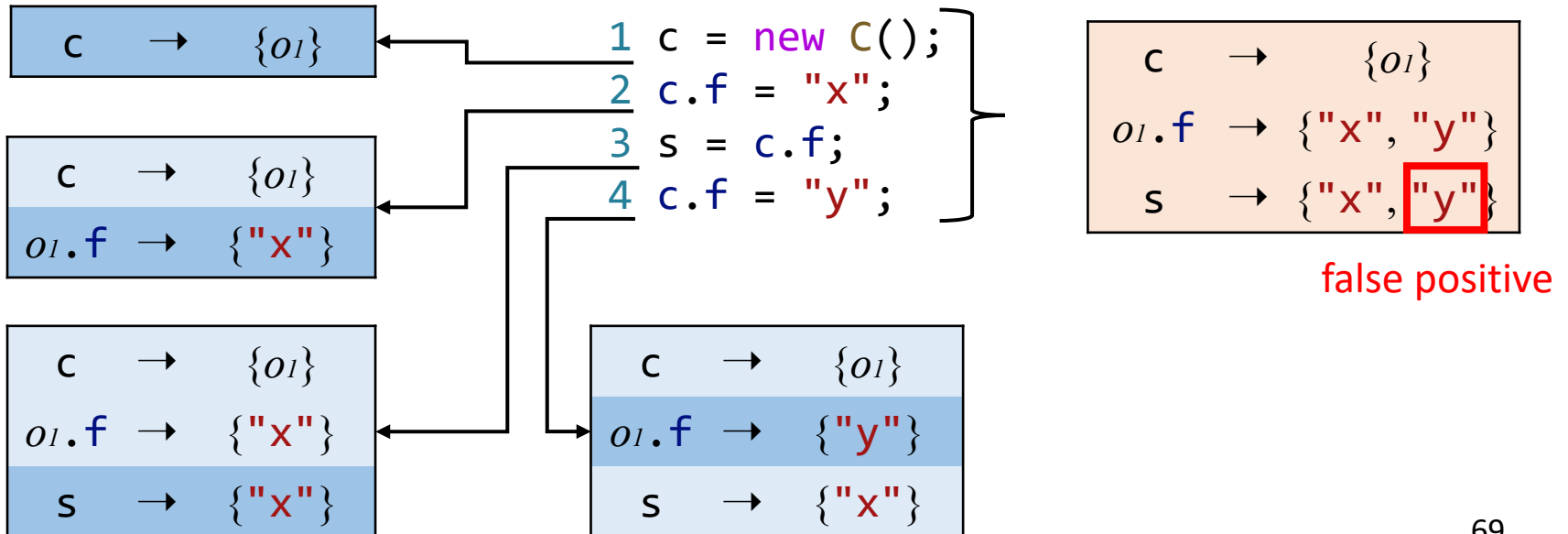
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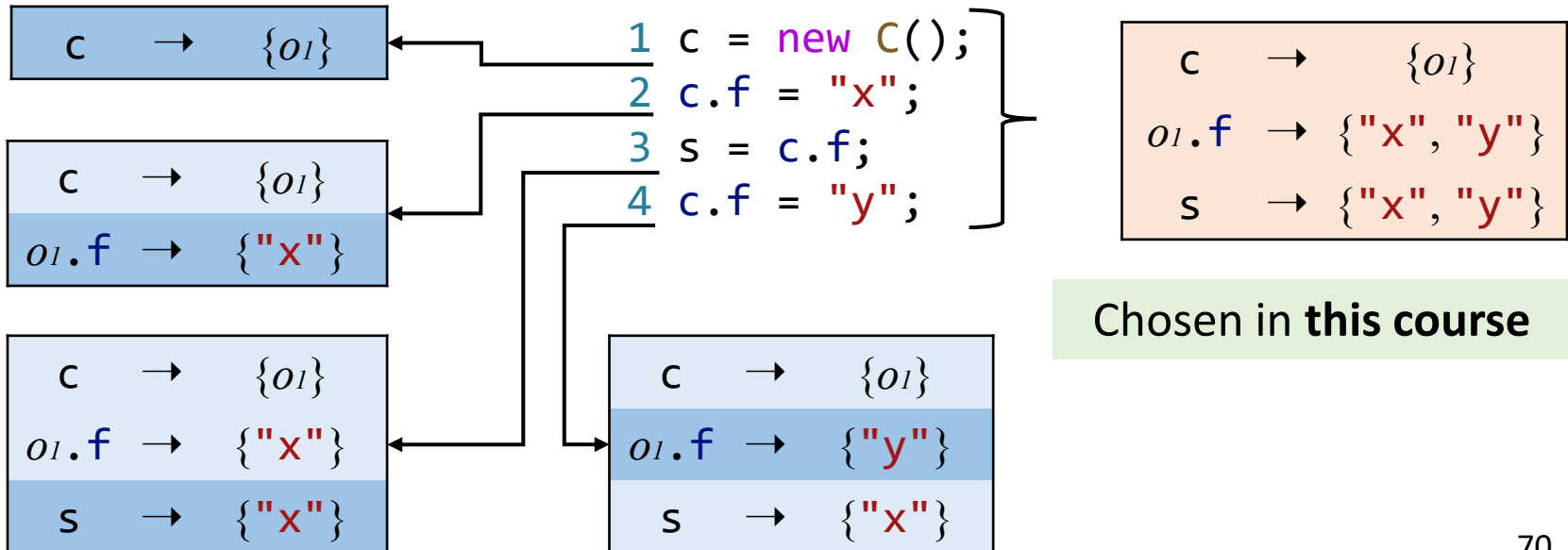
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# Analysis Scope

## Which parts of program should be analyzed?

Whole-program	Demand-driven
Compute points-to information for all pointers in the program	Only compute points-to information for the pointers that may affect specific sites of interest (on demand)
Provide information for all possible clients	Provide information for specific clients



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1 x = new A();  
2 y = x;  
3 ...  
4 z = new T();  
5 z.bar();
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x	→	{01}
y	→	{01}
z	→	{04}

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What points-to information  
do we need ?

**Client:** call graph construction  
**Site of interest:** line 5

# Analysis Scope

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---	---	------

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### Chosen in **this course**

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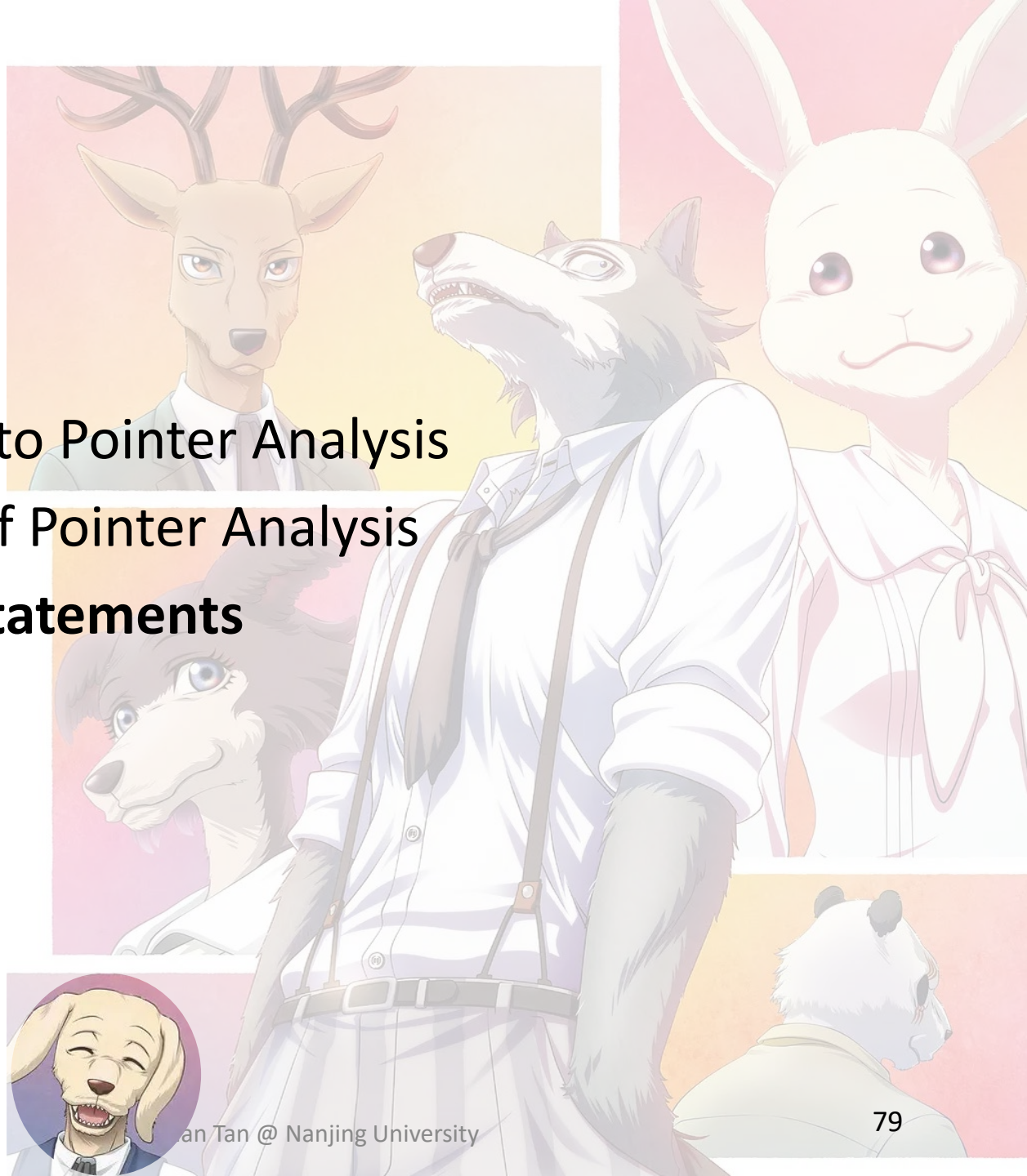
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# Pointer Analysis in This Course

Factor	Problem	Choice
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# Contents

1. Motivation
2. Introduction to Pointer Analysis
3. Key Factors of Pointer Analysis
- 4. Concerned Statements**



# What Do We Analyze?

- Modern languages typically have many kinds of statements
  - if-else
  - switch-case
  - for/while/do-while
  - break/continue
  - ...



# What Do We Analyze?


- Modern languages typically have many kinds of statements
  - ~~if else~~
  - ~~switch case~~
  - ~~for/while/do while~~
  - ~~break/continue~~
  - ...
- We only focus on **pointer-affecting statements**

Do not directly affect pointers  
Ignored in pointer analysis


# Pointers in Java

- Local variable: `x`
- Static field: `C.f`
- Instance field: `x.f`
- Array element: `array[i]`

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# Pointers in Java


- Local variable: `x`
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# Pointers in Java

- Local variable: `x`
- Static field: `C.f`
- Instance field: `x.f` ←
- Array element: `array[i]`

Modeled as an object  
(pointed by `x`) with a field `f`

# Pointers in Java

- Local variable: `x`
- Static field: `C.f`
- Instance field: `x.f`
- Array element: `array[i]` 

**Ignore indexes.** Modeled as an object (pointed by array) with a **single field**, say `arr`, which may point to any value stored in array

```
array = new String[10];  
array[0] = "x";  
array[1] = "y";  
s = array[0];
```

Real code

```
array = new String[];  
array.arr = "x";  
array.arr = "y";  
s = array.arr;
```

Perspective of pointer analysis

# Pointers in Java

- Local variable: `x`
- Static field: `C.f`
- Instance field: `x.f`
- Array element: `array[i]`

# Pointer-Affecting Statements

New             $x = \text{new } T()$

Assign             $x = y$

Store             $x.f = y$

Load             $y = x.f$

Call             $r = x.k(a, \dots)$



# Pointer-Affecting Statements

New	$x = \text{new } T()$
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Complex memory-accesses will be converted to **three-address code** by introducing temporary variables

$x.f.g.h = y;$



$t1 = x.f$   
 $t2 = t1.g$   
 $t2.h = y;$

# Pointer-Affecting Statements


New            `x = new T()`

Assign            `x = y`

Store            `x.f = y`

Load            `y = x.f`

Call            `r = x.k(a, ...)`

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- Static call        `C.foo()`
  - Special call      `super.foo()/x.<init>()/this.privateFoo()`
  - Virtual call      `x.foo()`

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- 
- Static call        `C.foo()`
  - Special call      `super.foo()/x.<init>()/this.privateFoo()`
  - Virtual call      `x.foo()` **focus**

# The X You Need To Understand in This Lecture

- What is pointer analysis?
- Understand the key factors of pointer analysis
- Understand what we analyze in pointer analysis

注意注意!  
划重点了!



# Static Program Analysis

## Pointer Analysis Foundations (I)

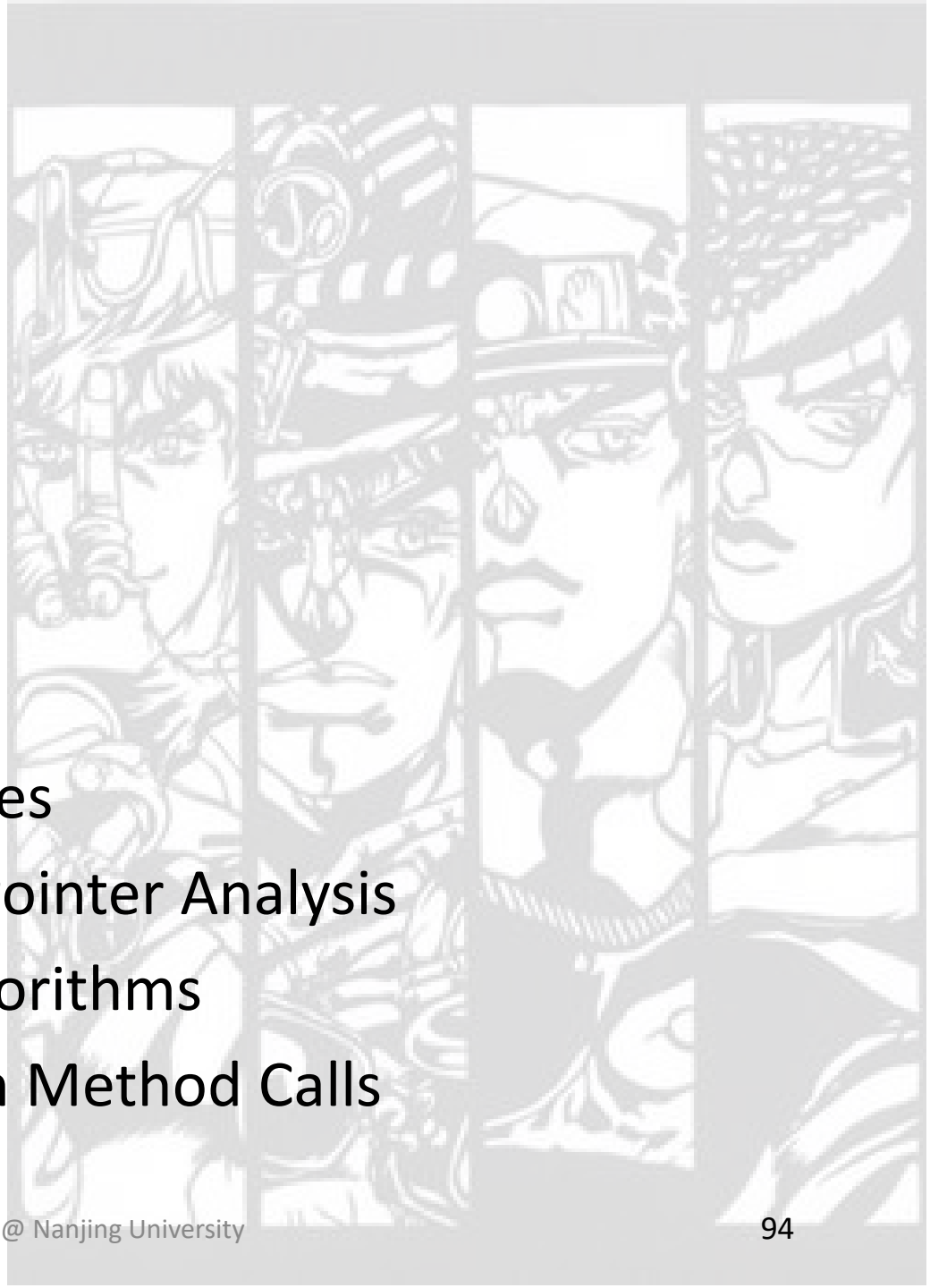
Nanjing University

Tian Tan

2020

# Contents



1. Pointer Analysis: Rules
2. How to Implement Pointer Analysis
3. Pointer Analysis: Algorithms
4. Pointer Analysis with Method Calls



# Contents

- 1. Pointer Analysis: Rules**
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# Pointer-Affecting Statements

New	<code>x = new T()</code>	 <p>First focus on these statements (suppose the program has just one method)</p>
Assign	<code>x = y</code>	
Store	<code>x.f = y</code>	
Load	<code>y = x.f</code>	
Call	<code>r = x.k(a, ...)</code>	 <p>Will come back to this in pointer analysis with method calls</p>



# Domain and Notations

**Variables:**  $x, y \in V$

**Fields:**  $f, g \in F$

**Objects:**  $o_i, o_j \in O$

**Instance fields:**  $o_i.f, o_j.g \in O \times F$

**Pointers:**  $\text{Pointer} = V \cup (O \times F)$

**Points-to relations:**  $pt : \text{Pointer} \rightarrow \mathcal{P}(O)$

- $\mathcal{P}(O)$  denotes the powerset of  $O$
- $pt(p)$  denotes the points-to set of  $p$

# Rules

Kind	Statement	Rule
New	$i: x = \text{new } T()$	$\overline{o_i \in pt(x)}$
Assign	$x = y$	$\frac{o_i \in pt(y)}{o_i \in pt(x)}$
Store	$x.f = y$	$\frac{o_i \in pt(x), o_j \in pt(y)}{o_j \in pt(o_i.f)}$
Load	$y = x.f$	$\frac{o_i \in pt(x), o_j \in pt(o_i.f)}{o_j \in pt(y)}$

# Rules

Kind	Statement	Rule
New	$i: x = \text{new } T()$	$\frac{}{o_i \in pt(x)}$ ← unconditional
Assign	$x = y$	$\frac{o_i \in pt(y)}{o_i \in pt(x)}$ ← premises ← conclusion
Store	$x.f = y$	$\frac{o_i \in pt(x), o_j \in pt(y)}{o_j \in pt(o_i.f)}$
Load	$y = x.f$	$\frac{o_i \in pt(x), o_j \in pt(o_i.f)}{o_j \in pt(y)}$

# Rule: New

$$\overline{o_i \in pt(x)}$$

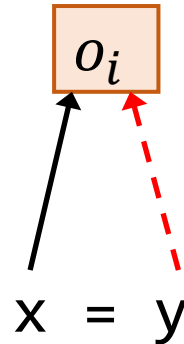
→ Conclusion

$$i: x = \text{new } T() \quad \uparrow \quad o_i$$

# Rule: Assign

$$\frac{o_i \in pt(y)}{o_i \in pt(x)}$$

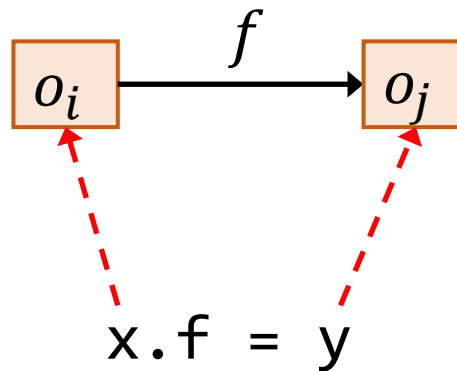
-----> Premises  
-----> Conclusion



# Rule: Store

$$\frac{o_i \in pt(x), o_j \in pt(y)}{o_j \in pt(o_i.f)}$$

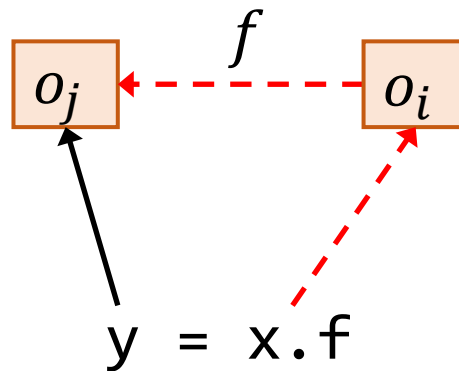
-----> Premises  
-----> Conclusion



# Rule: Load

$$\frac{o_i \in pt(x), o_j \in pt(o_i.f)}{o_j \in pt(y)}$$

-----> Premises  
-----> Conclusion



# Rules

-----> Premises

—————> Conclusion

Kind	Rule	Illustration
New	$\frac{}{o_i \in pt(x)}$	<p><math>i: x = \text{new } T()</math></p>
Assign	$\frac{o_i \in pt(y)}{o_i \in pt(x)}$	<p><math>x = y</math></p>
Store	$\frac{o_i \in pt(x), o_j \in pt(y)}{o_j \in pt(o_i.f)}$	<p><math>x.f = y</math></p>
Load	$\frac{o_i \in pt(x), o_j \in pt(o_i.f)}{o_j \in pt(y)}$	<p><math>y = x.f</math></p>